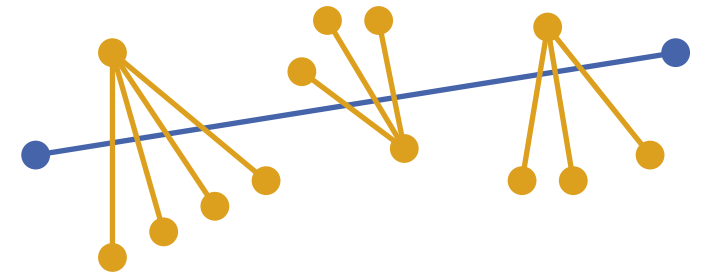
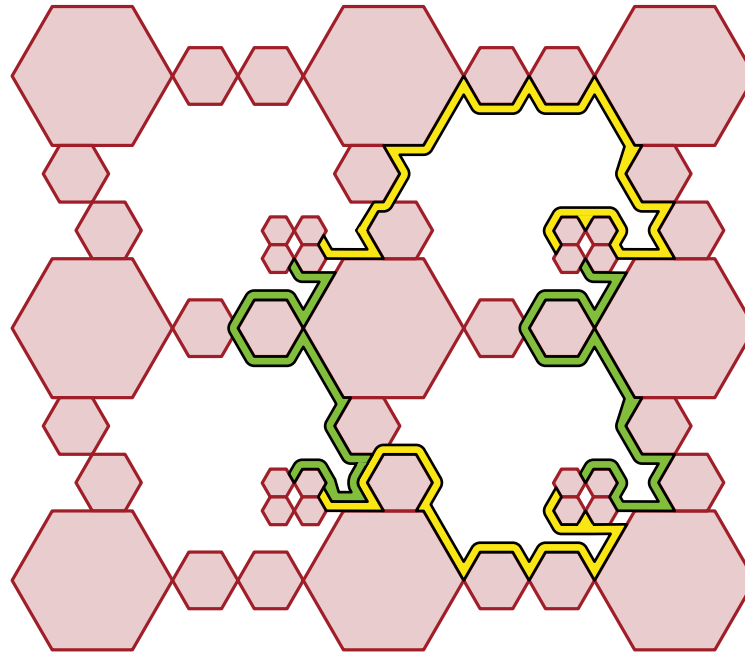
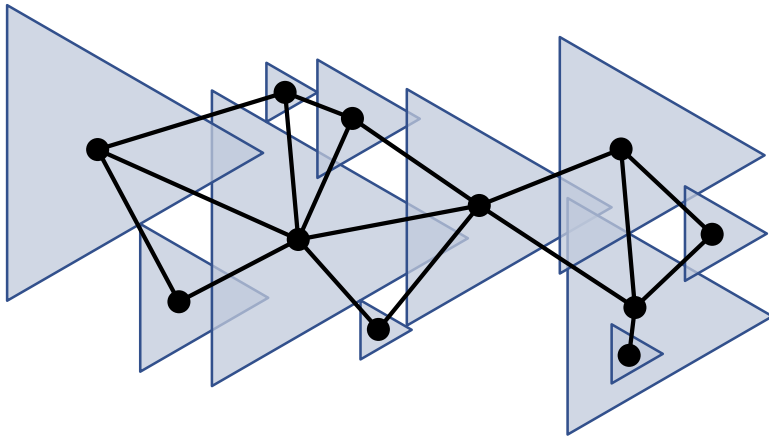


Intersection Graphs with and without Product Structure

GD 2024 · 19.09.2024

Laura Merker, Lena Scherzer, **Samuel Schneider**, Torsten Ueckerdt

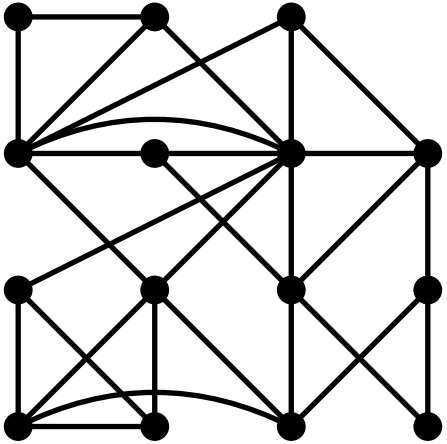


Product Structure

A graph class $\mathcal{G}$ has product structure if there exists a $c \in \mathbb{N}$ such that:

Product Structure

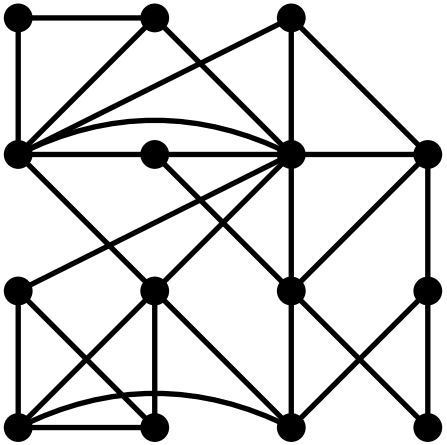
A graph class $\mathcal{G}$ has product structure if there exists a $c \in \mathbb{N}$ such that:



For every $G \in \mathcal{G}$

Product Structure

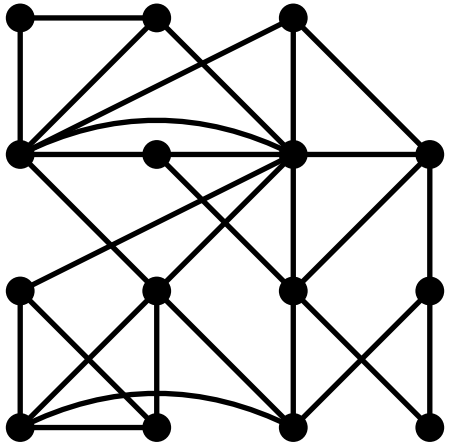
A graph class $\mathcal{G}$ has product structure if there exists a $c \in \mathbb{N}$ such that:



For every $G \in \mathcal{G}$ there are H and P

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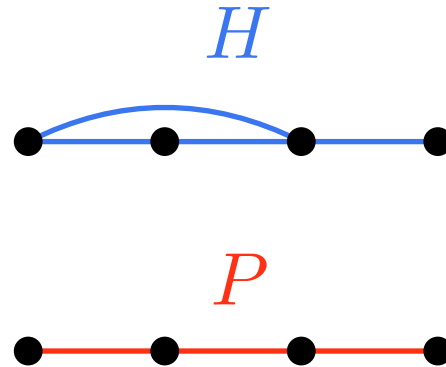
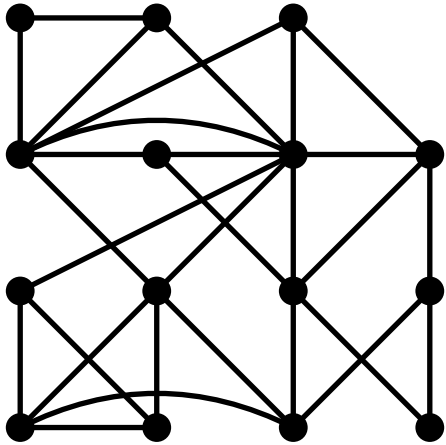
there are H and P

treewidth c

path

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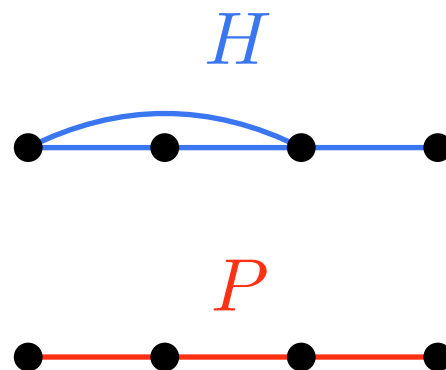
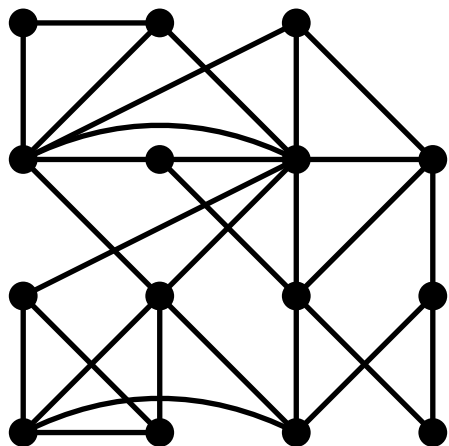
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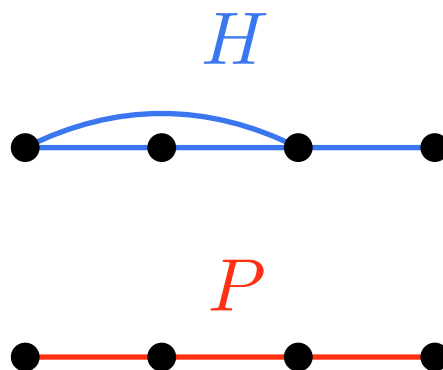
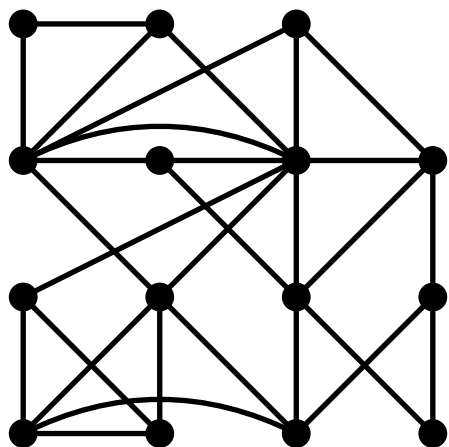
For every $G \in \mathcal{G}$ there are H and P such that $G \subseteq H \boxtimes P$.

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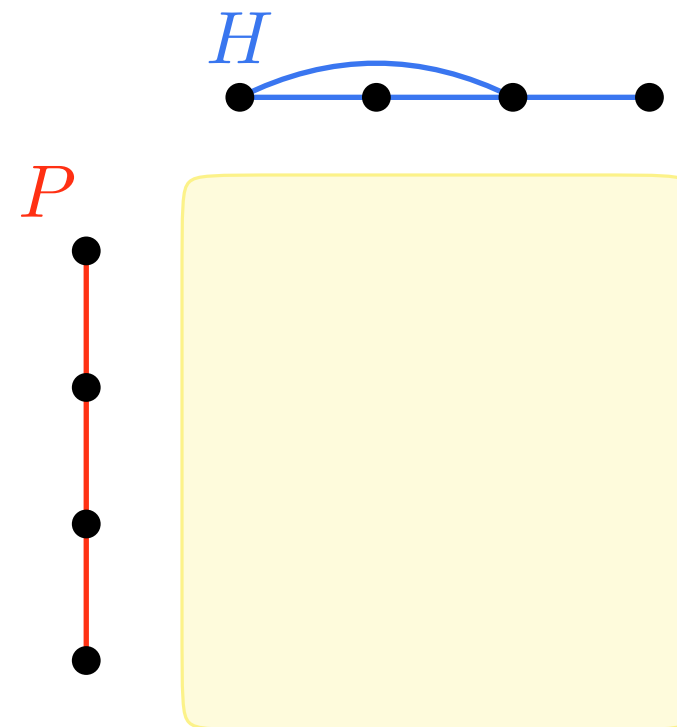
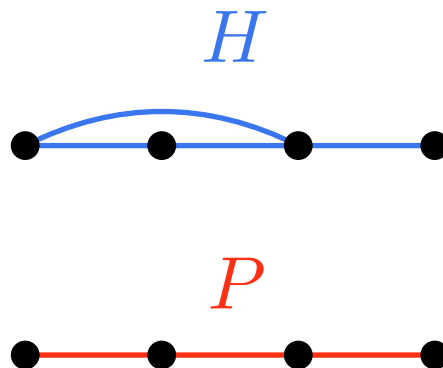
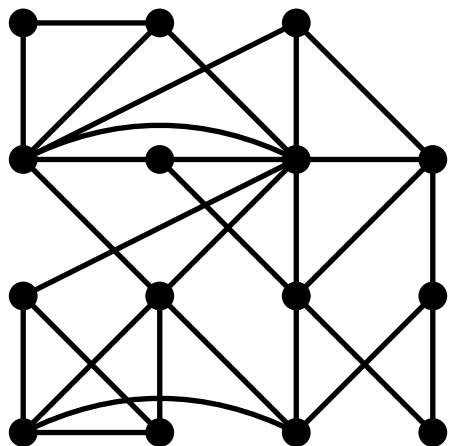
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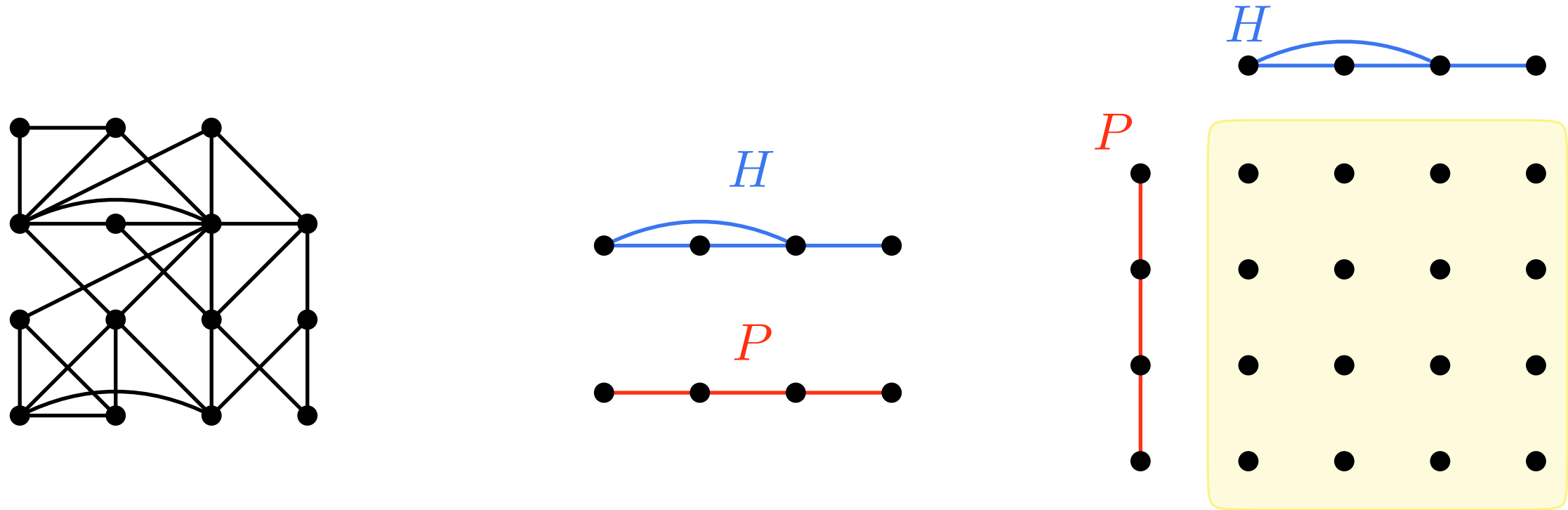
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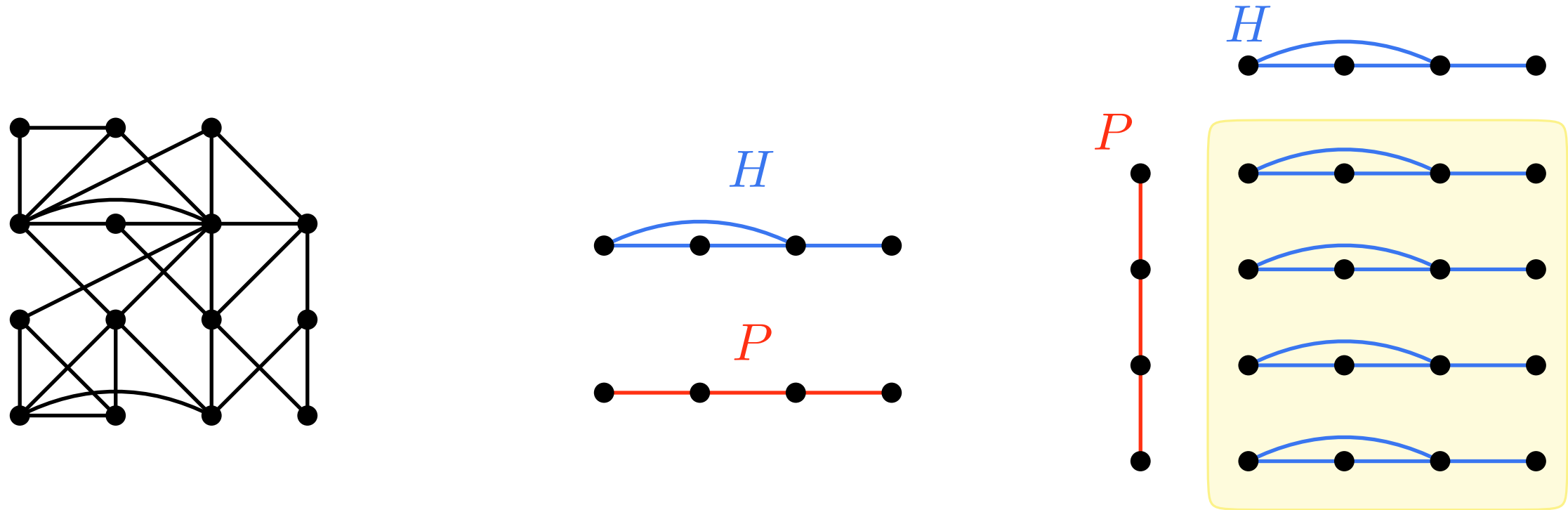
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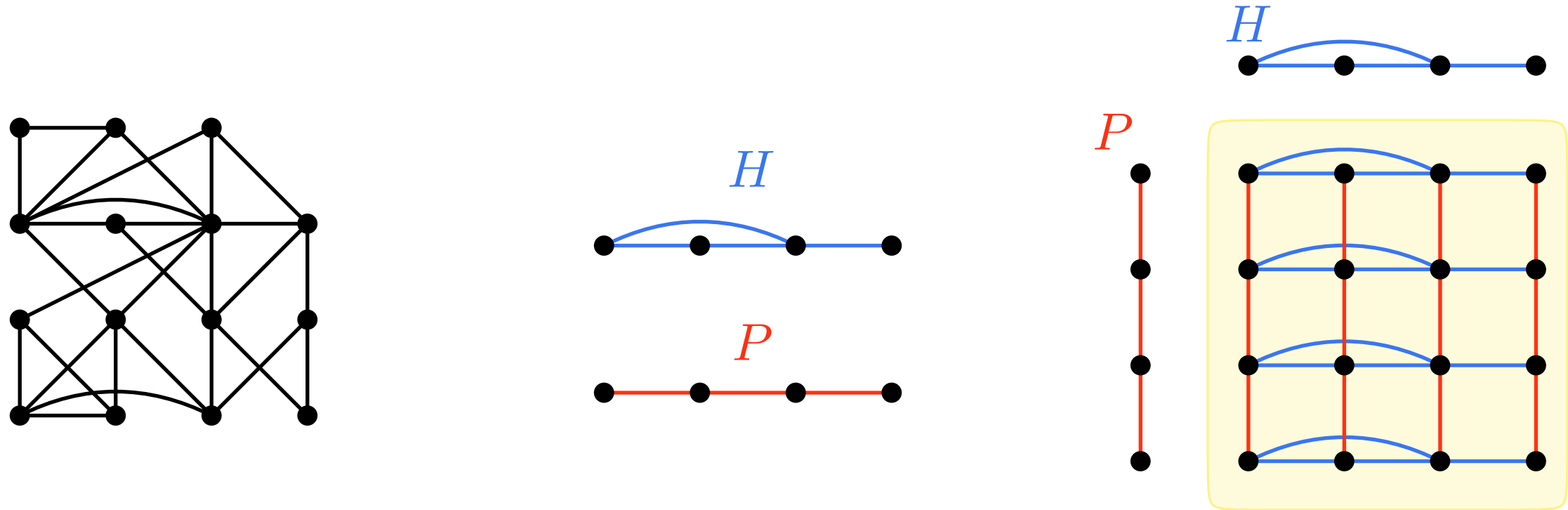
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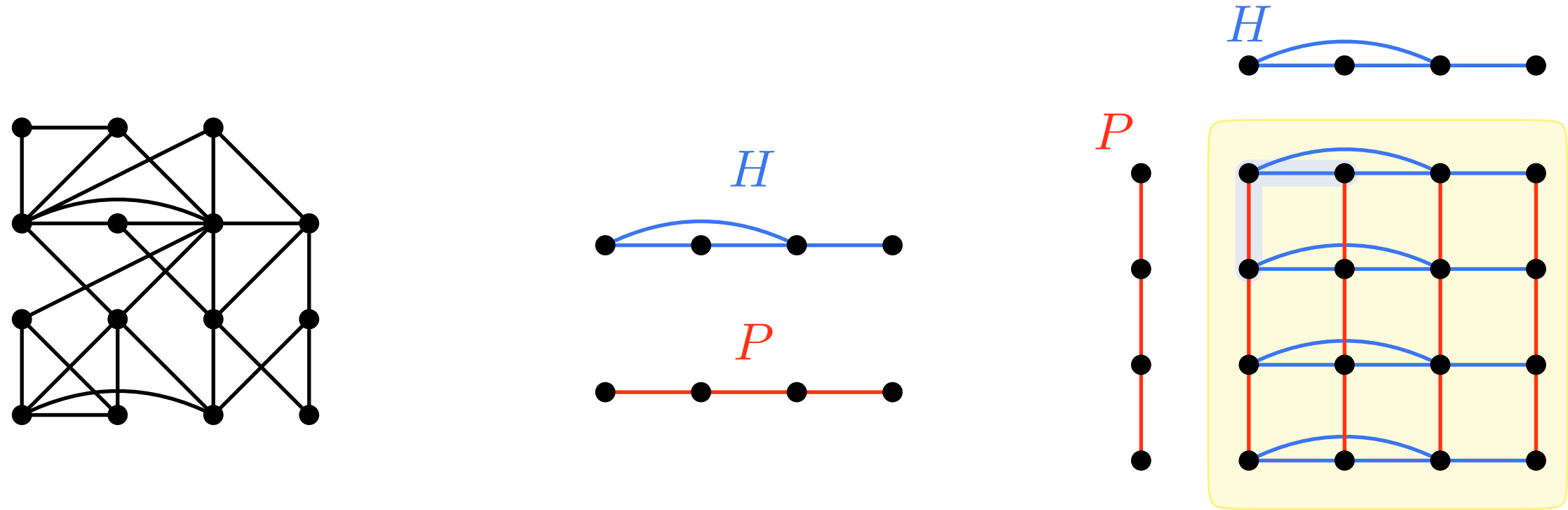
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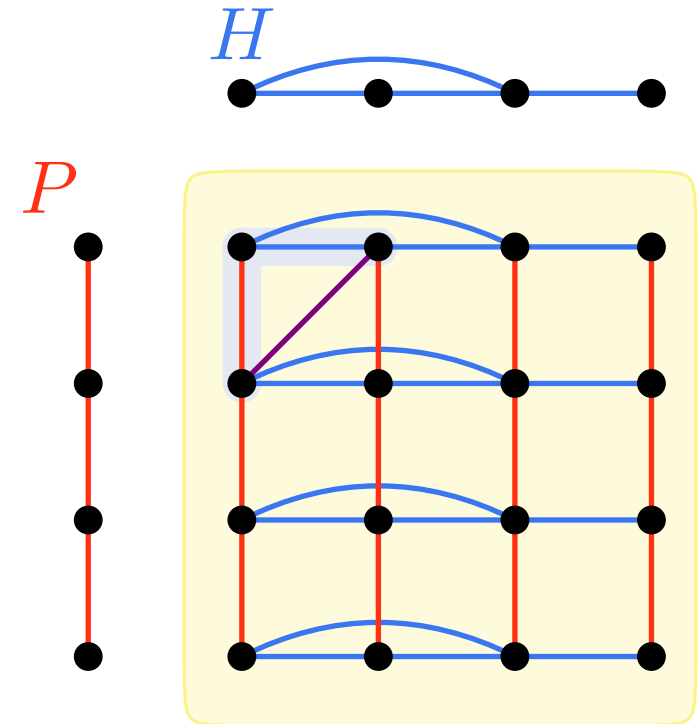
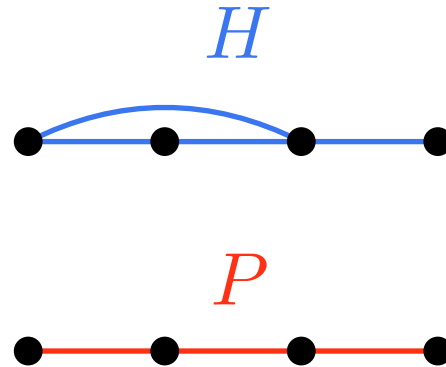
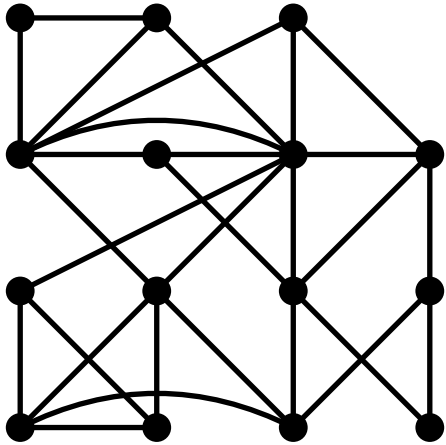
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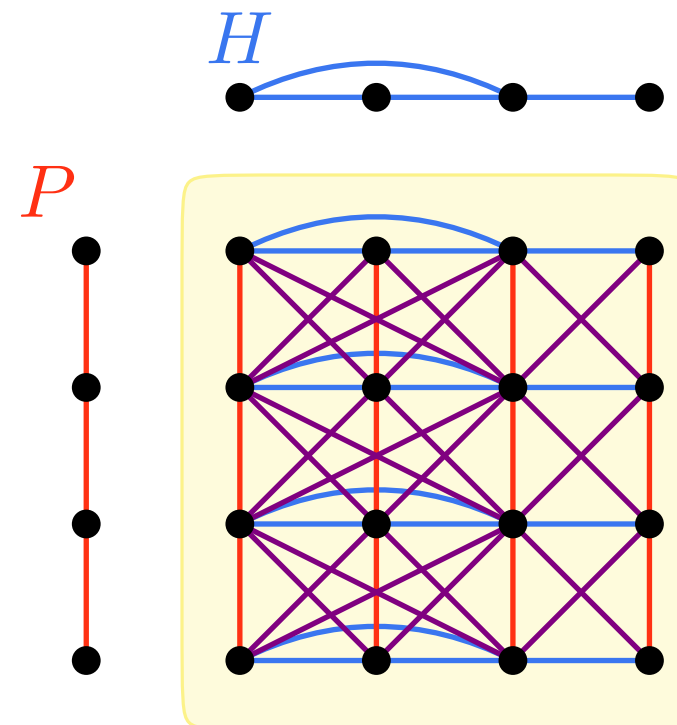
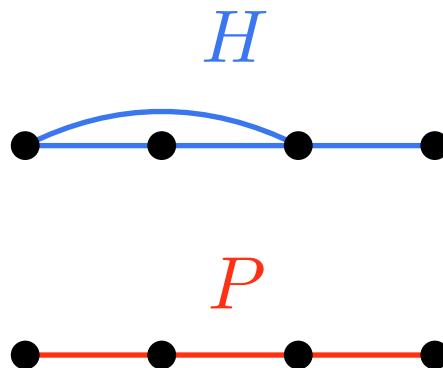
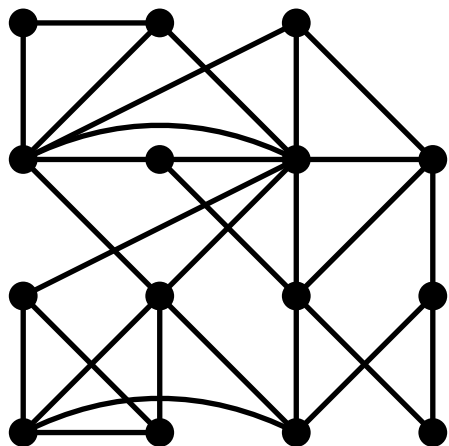
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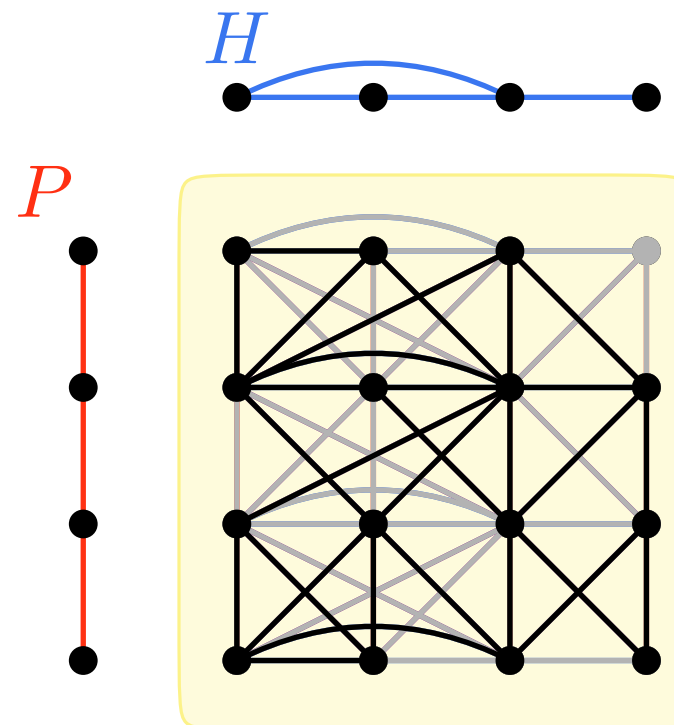
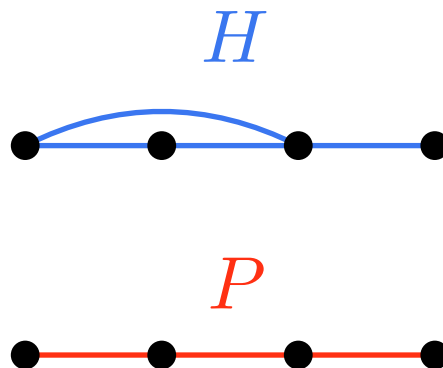
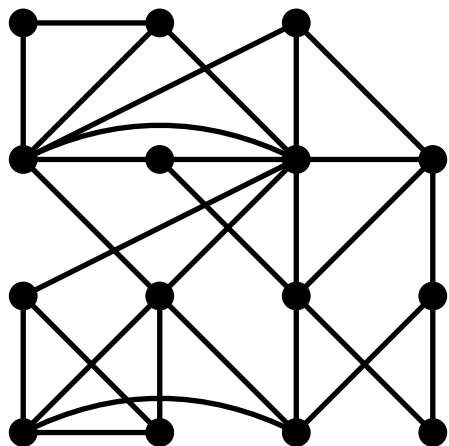
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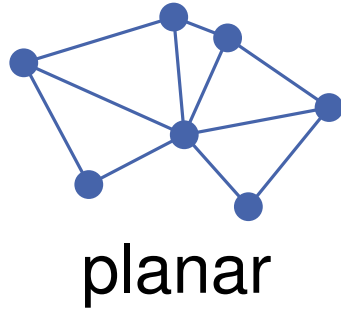
strong product

Existence of Product Structure

- Many beyond-planar graph classes have product structure.

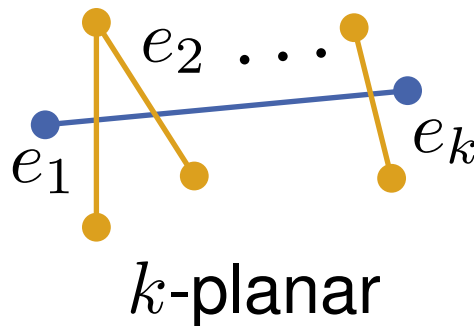
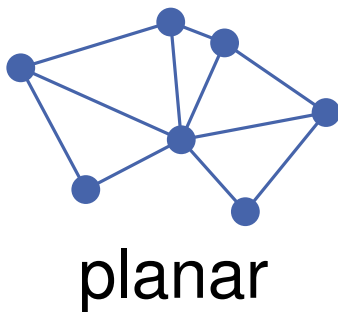
Existence of Product Structure

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Existence of Product Structure

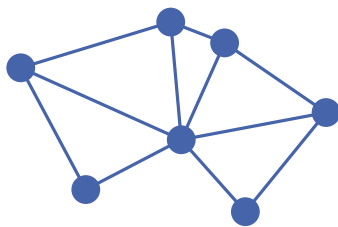
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[Dujmović et al.]

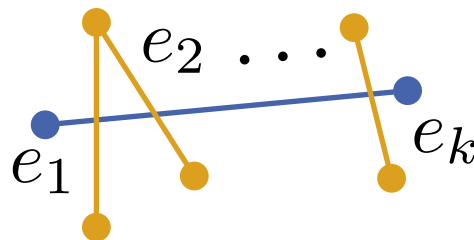
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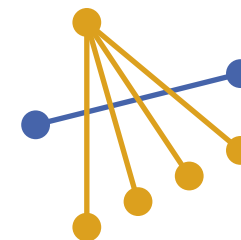


planar

[Dujmović et al.]



k -planar

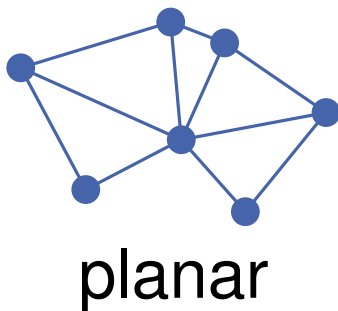


fan-planar

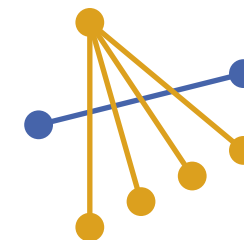
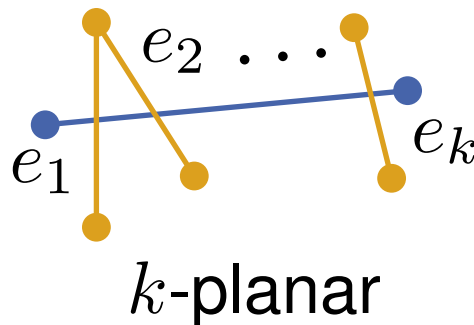
[Hickingbotham and Wood]

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[Dujmović et al.]



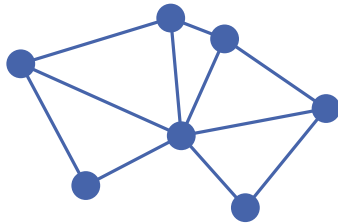
fan-planar

[Hickingbotham and Wood]

- Large cliques $\implies$ **no** product structure.

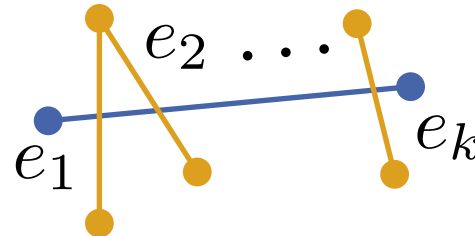
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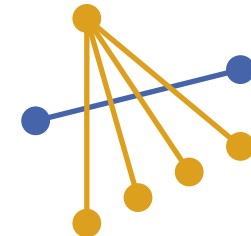


planar

[Dujmović et al.]



k -planar



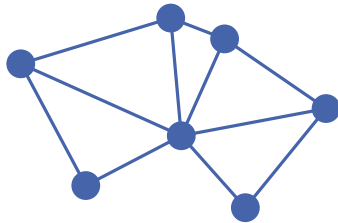
fan-planar

[Hickingbotham and Wood]

-
- Large cliques $\implies$ **no** product structure.
 - Large treewidth in neighborhood $\implies$ **no** product structure.

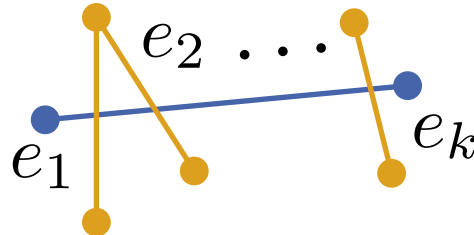
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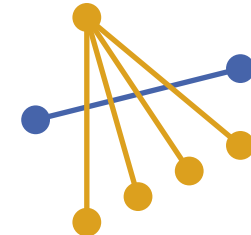


planar

[Dujmović et al.]



k -planar



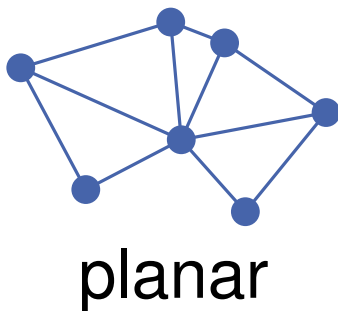
fan-planar

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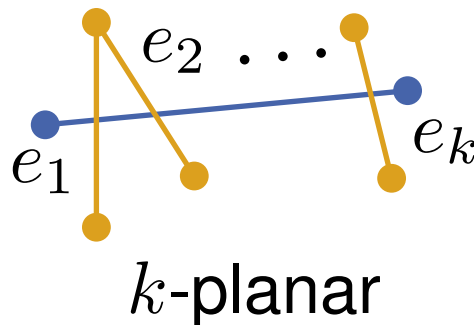
-
- Large cliques $\implies$ **no** product structure.
 - Large treewidth in neighborhood $\implies$ **no** product structure.
 - **No linear local treewidth** $\implies$ **no** product structure.

Existence of Product Structure

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[Dujmović et al.]

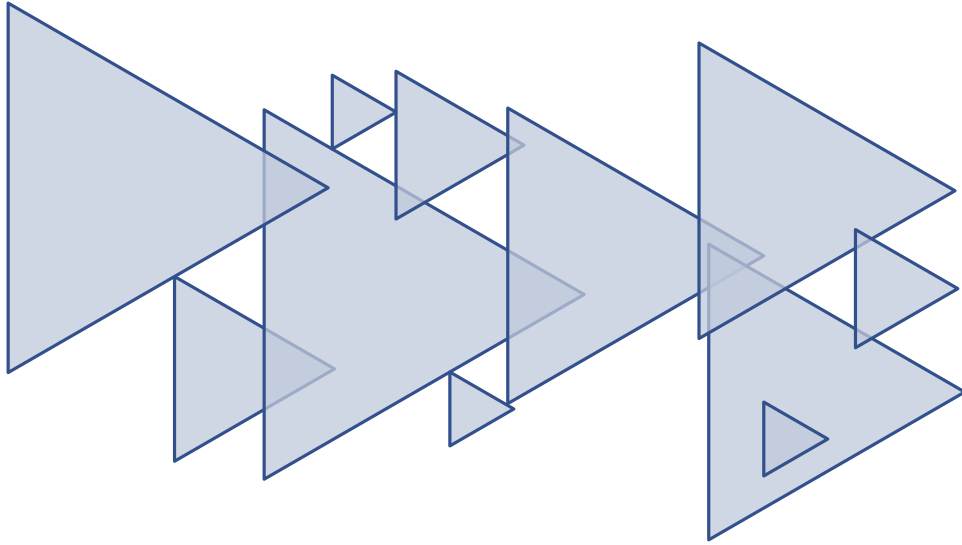


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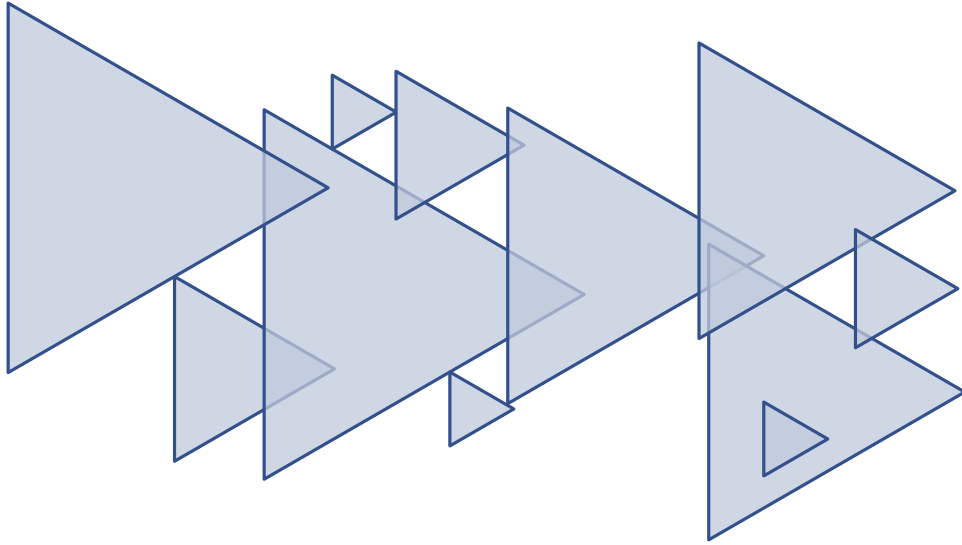
— Where is the border between product structure and no product structure? —

- Large cliques $\implies$ **no** product structure.
- Large treewidth in neighborhood $\implies$ **no** product structure.
- **No linear local treewidth** $\implies$ **no** product structure.

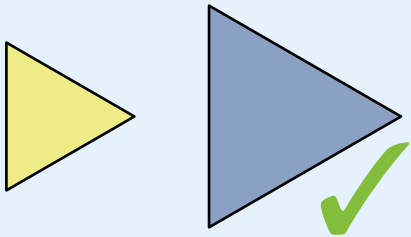
Intersection Graphs of Homothetic n -Gons



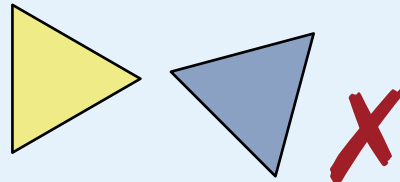
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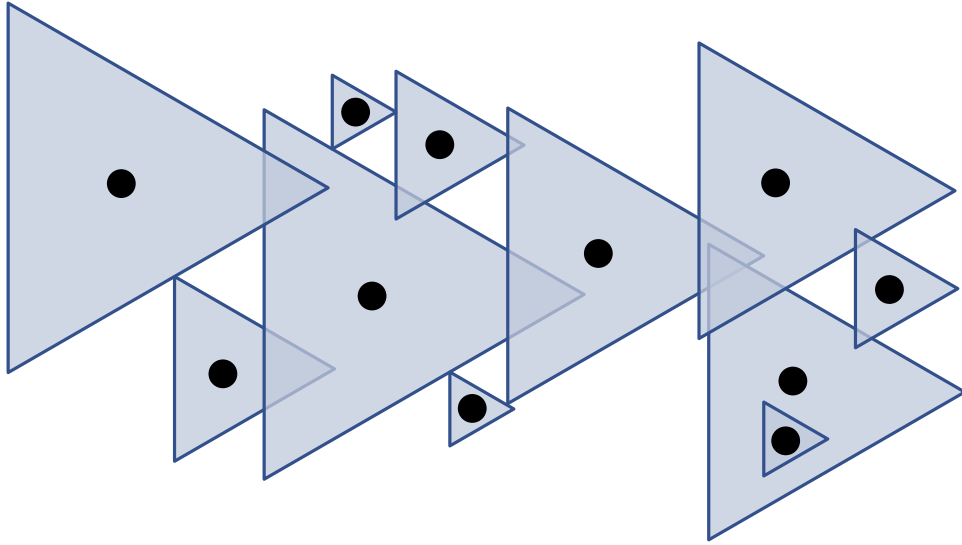
homothetic



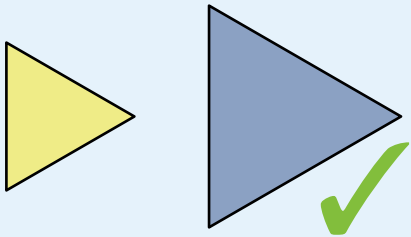
not homothetic



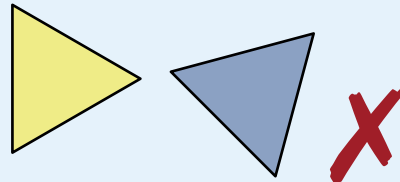
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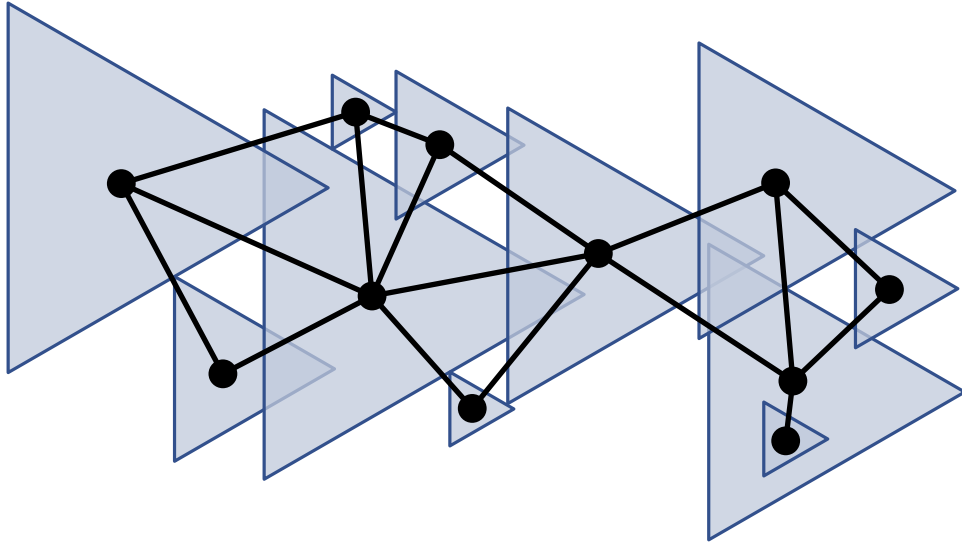
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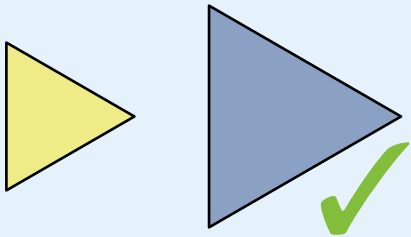
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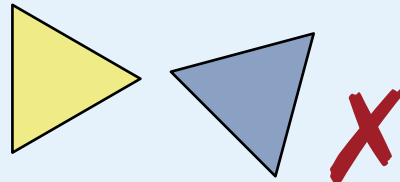
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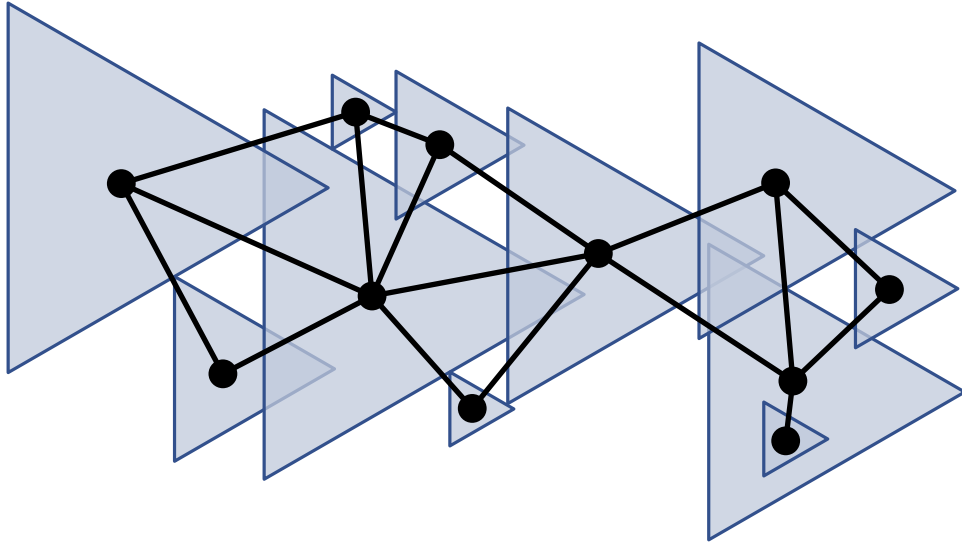
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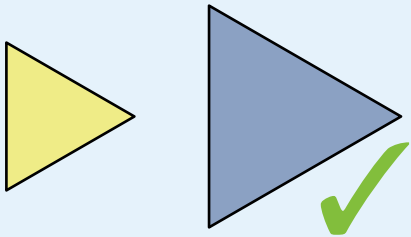


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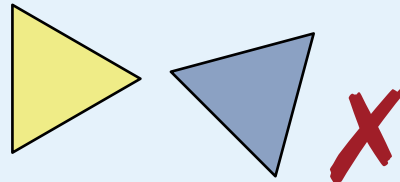


Problems for product structure:

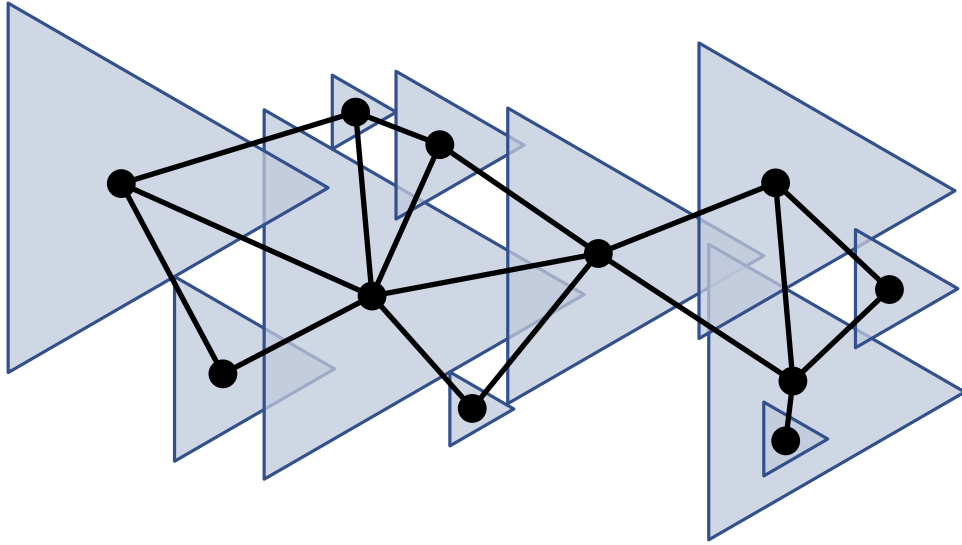
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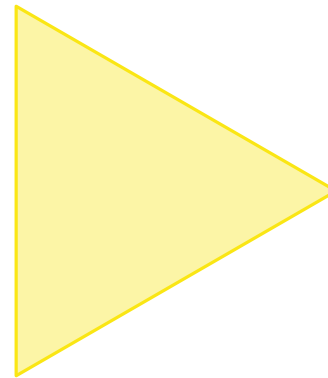
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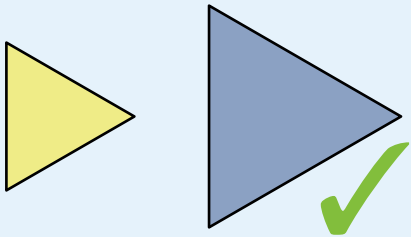
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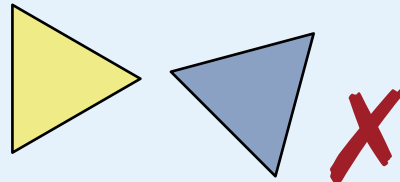
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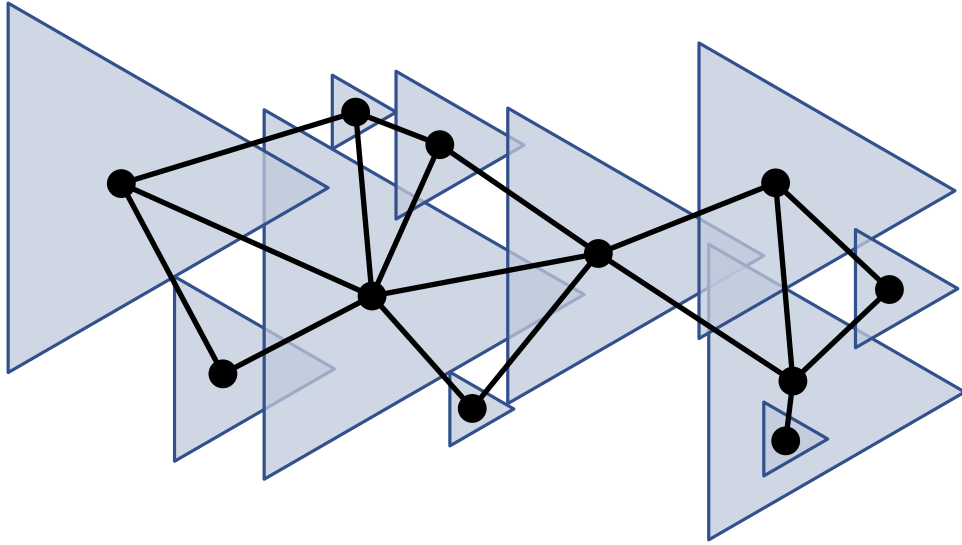
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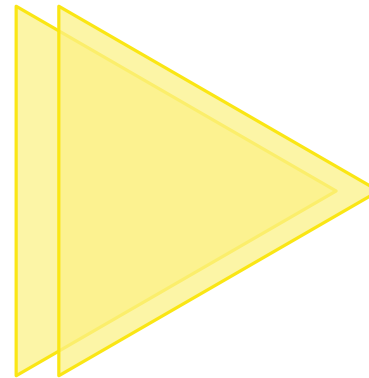
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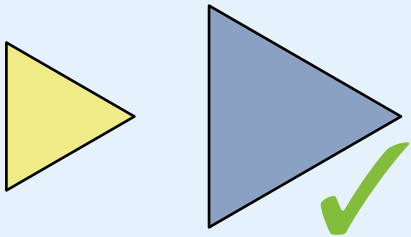
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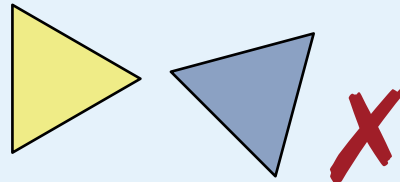
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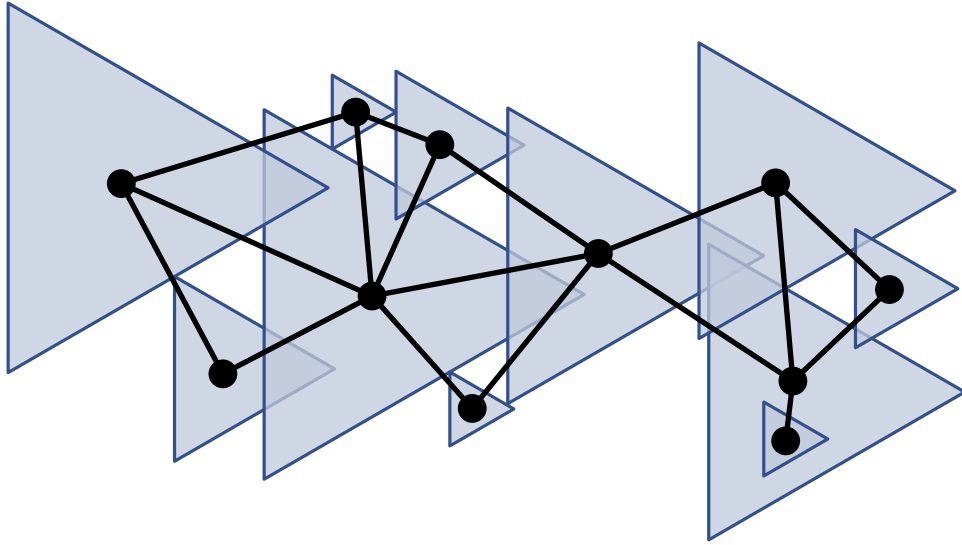
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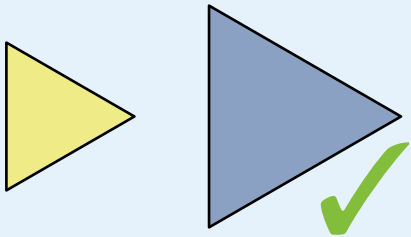
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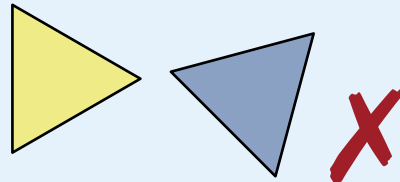
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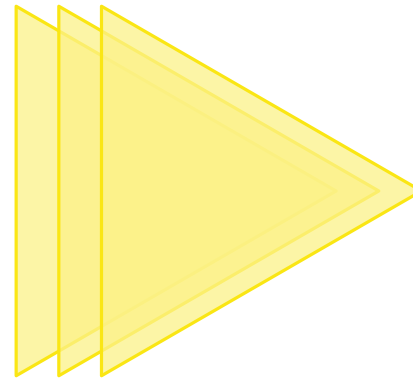
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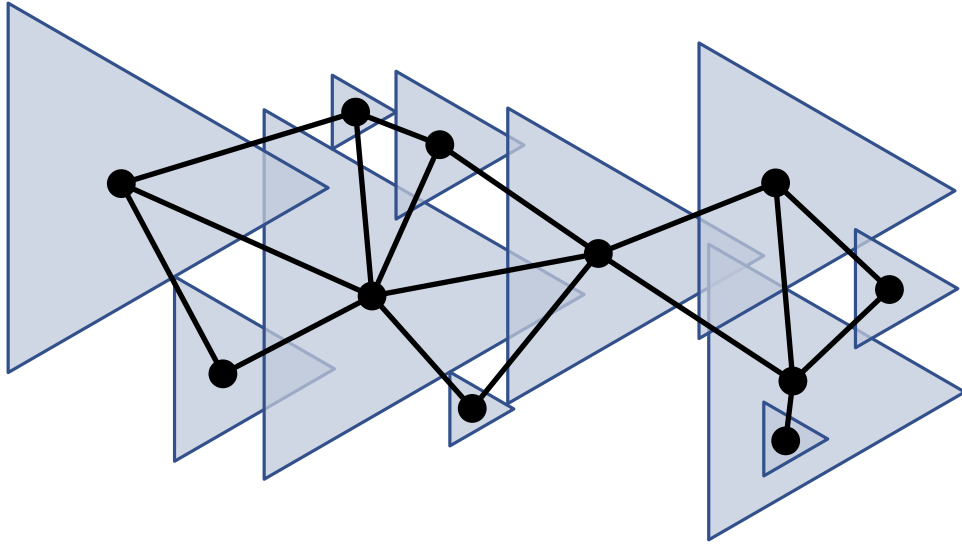
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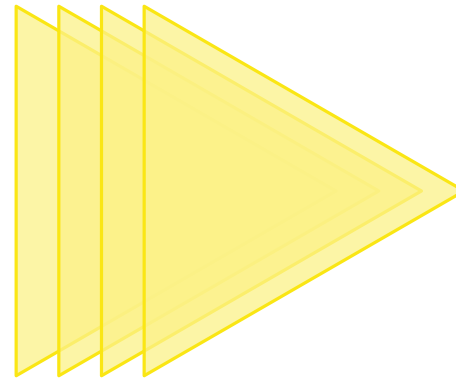
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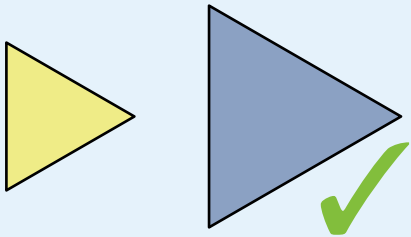
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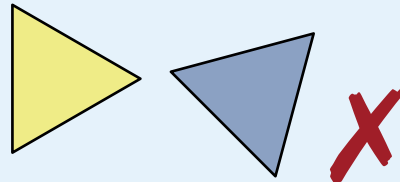
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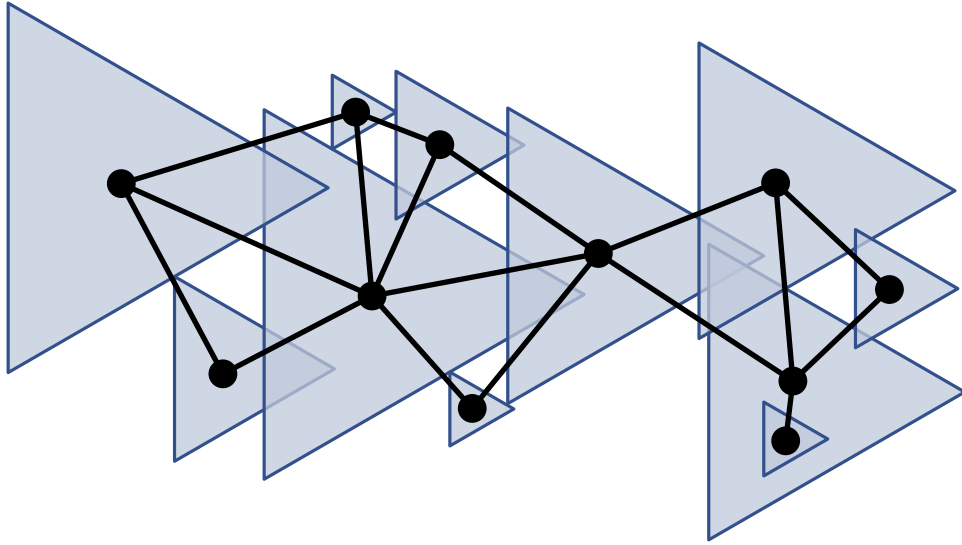
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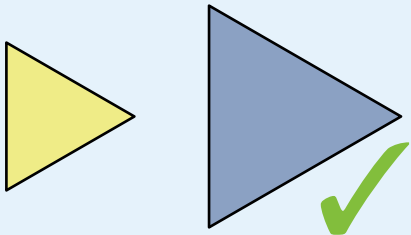
not homothetic



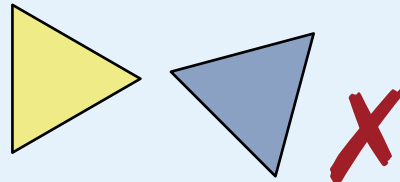
Intersection Graphs of Homothetic n -Gons



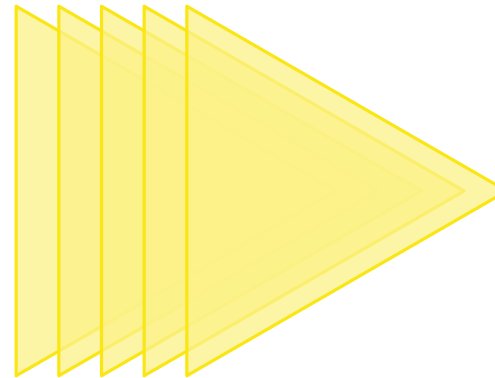
homothetic



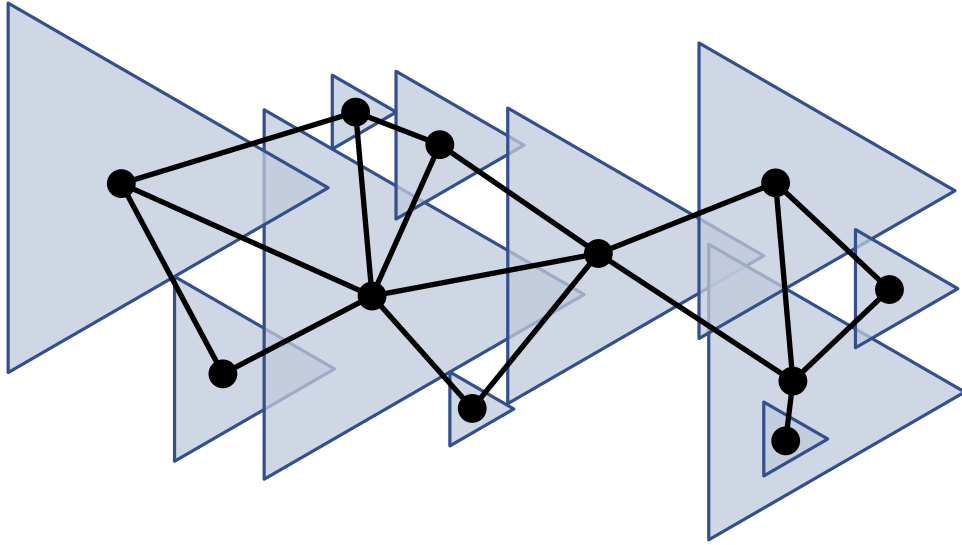
not homothetic



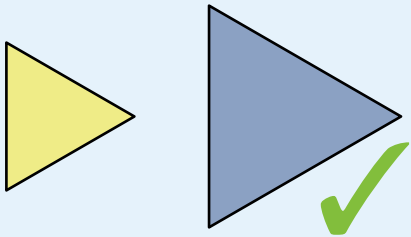
Problems for product structure:



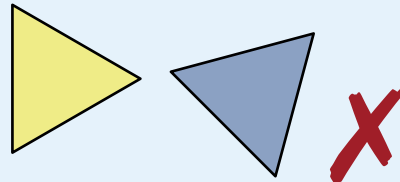
Intersection Graphs of Homothetic n -Gons



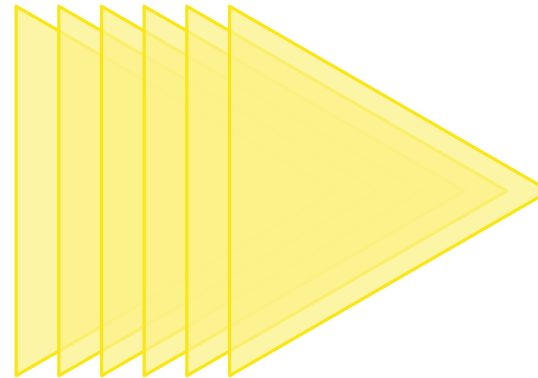
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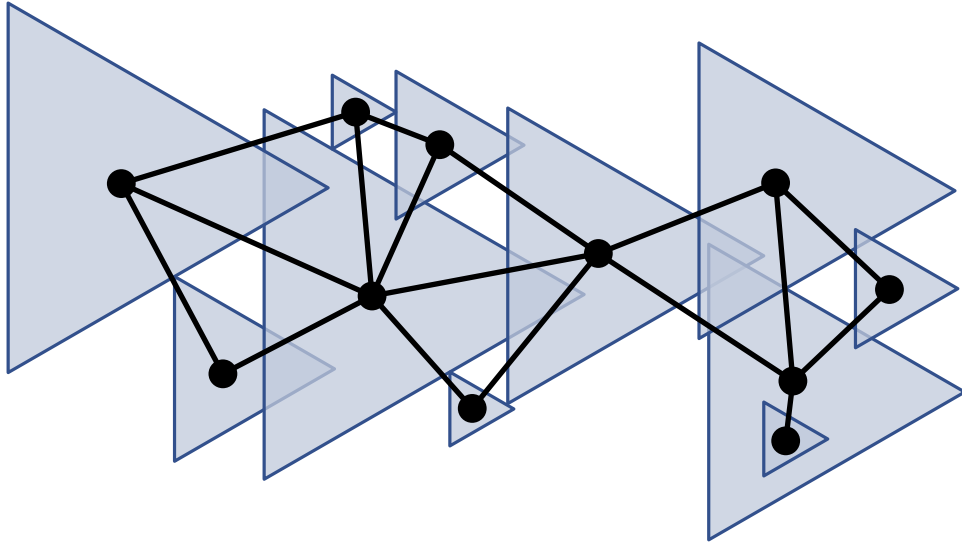
not homothetic



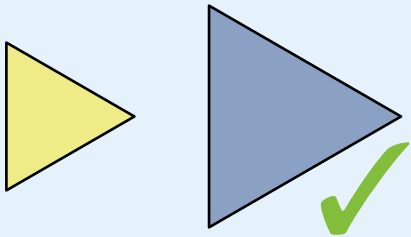
Problems for product structure:



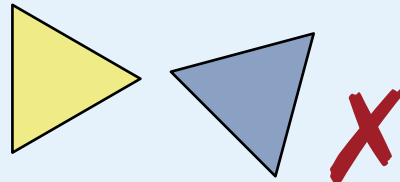
Intersection Graphs of Homothetic n -Gons



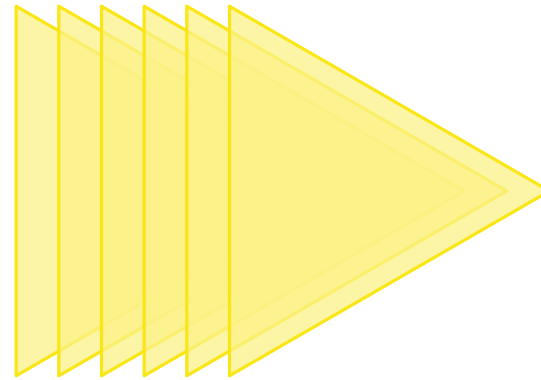
homothetic



not homothetic

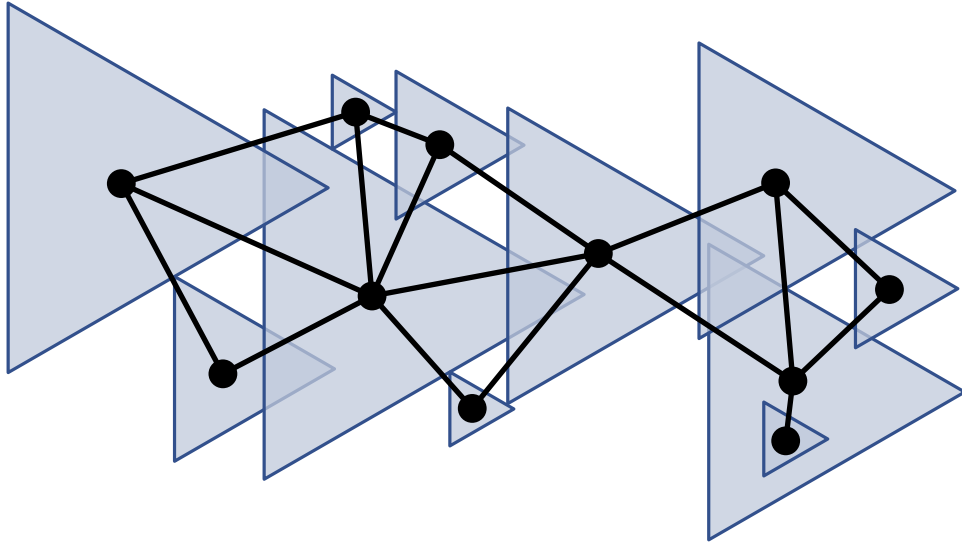


Problems for product structure:

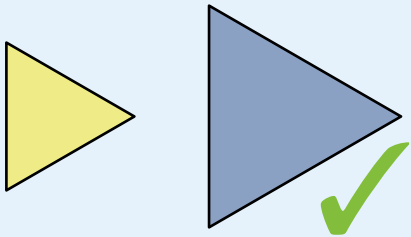


large cliques

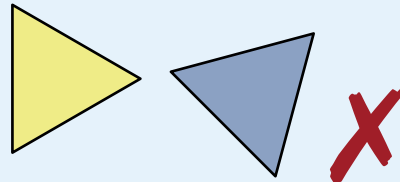
Intersection Graphs of Homothetic n -Gons



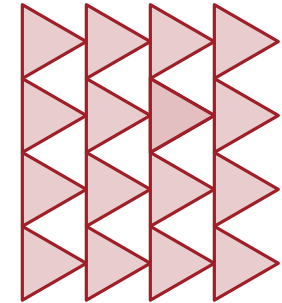
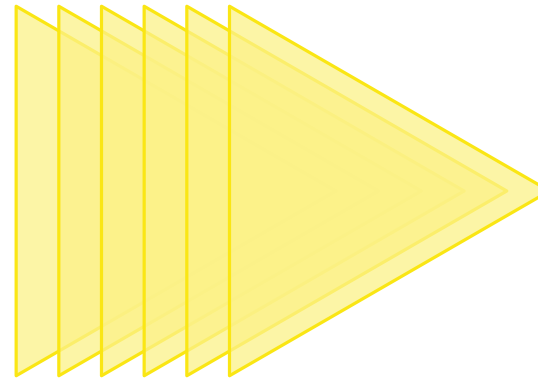
homothetic



not homothetic

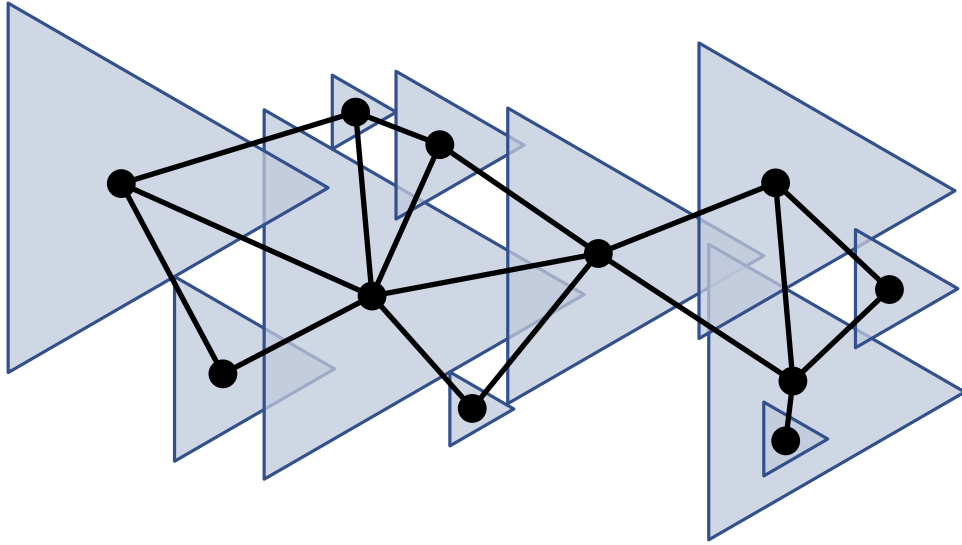


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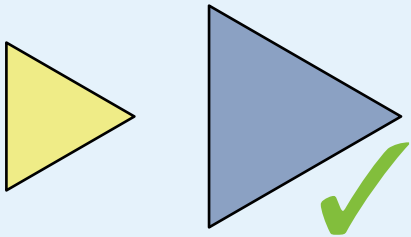


large cliques

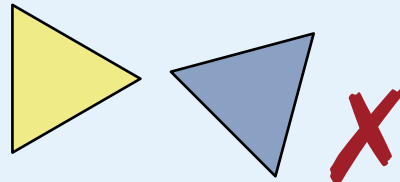
Intersection Graphs of Homothetic n -Gons



homothetic

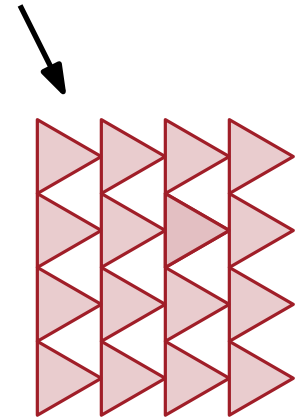
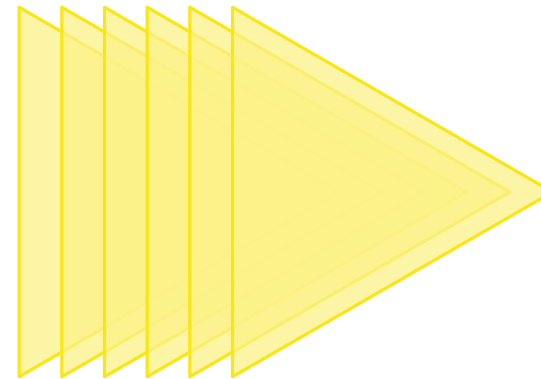


not homothetic



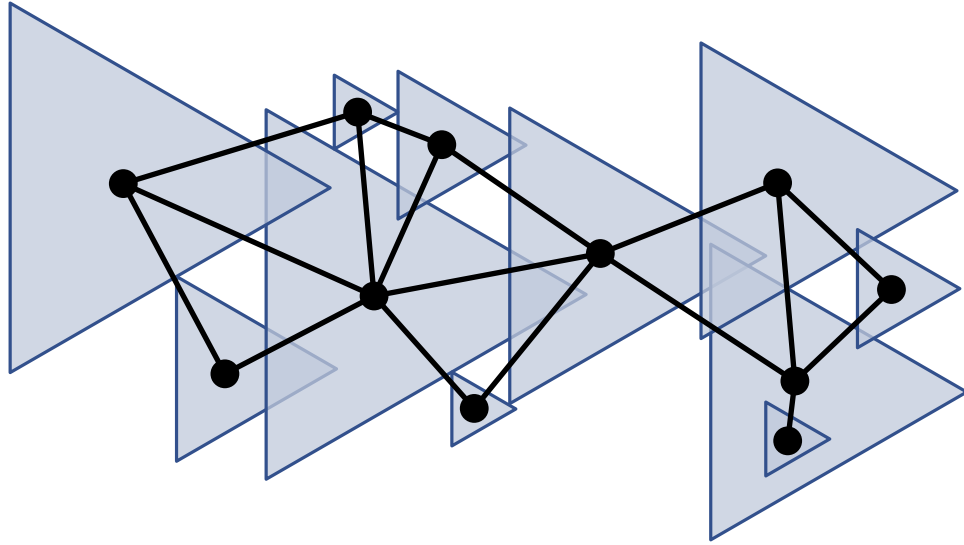
Problems for product structure:

large treewidth

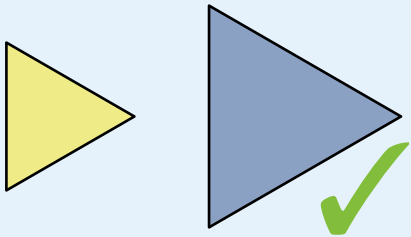


large cliques

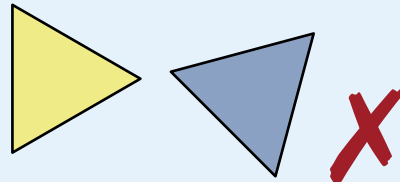
Intersection Graphs of Homothetic n -Gons



homothetic

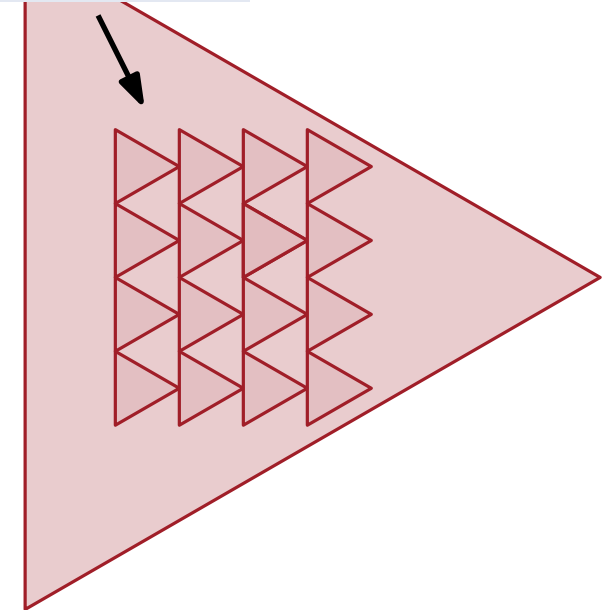
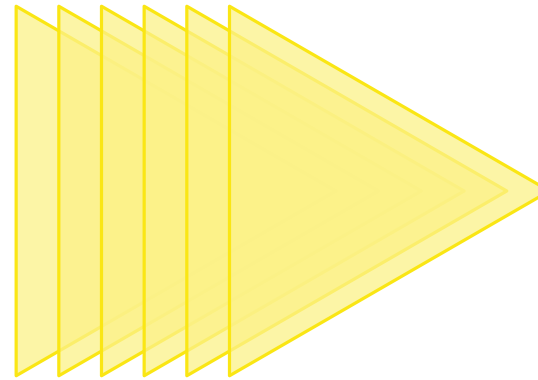


not homothetic



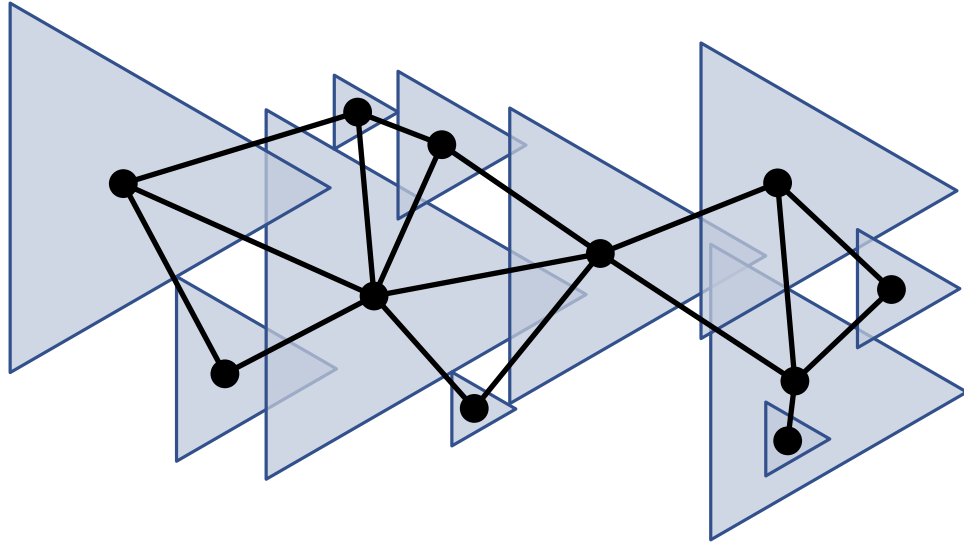
Problems for product structure:

large treewidth

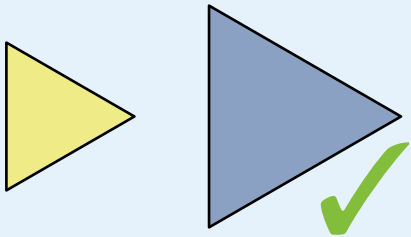


large cliques

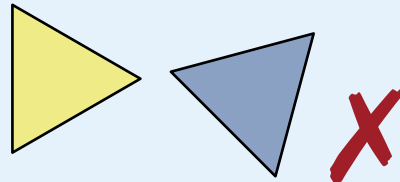
Intersection Graphs of Homothetic n -Gons



homothetic

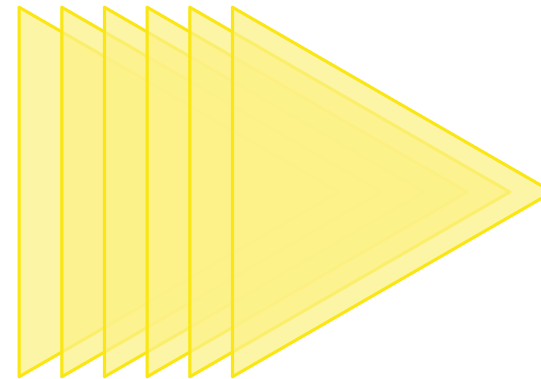


not homothetic

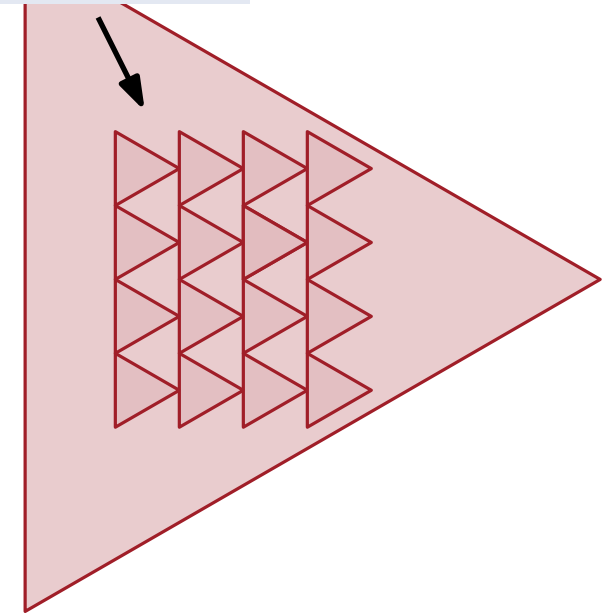


Problems for product structure:

large treewidth



large cliques



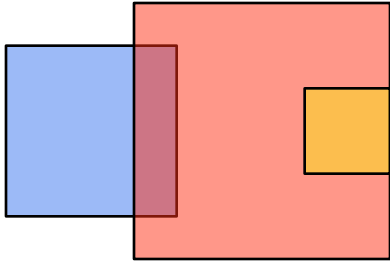
grids in neighborhood

α -free Intersection Graphs

A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.

α -free Intersection Graphs

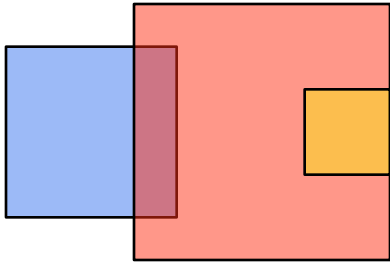
A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.



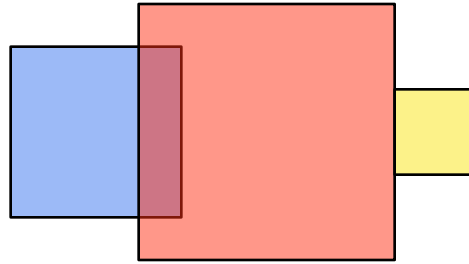
0-free

α -free Intersection Graphs

A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.



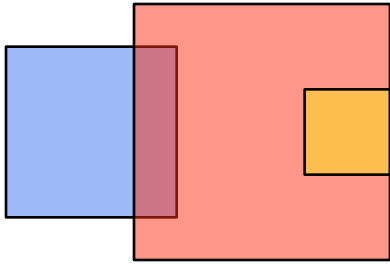
0-free



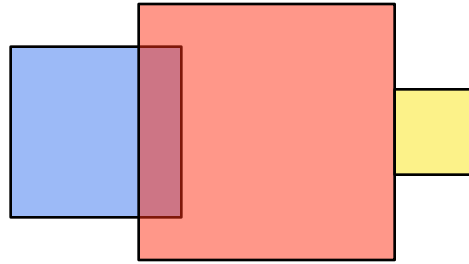
$\frac{3}{4}$ -free

α -free Intersection Graphs

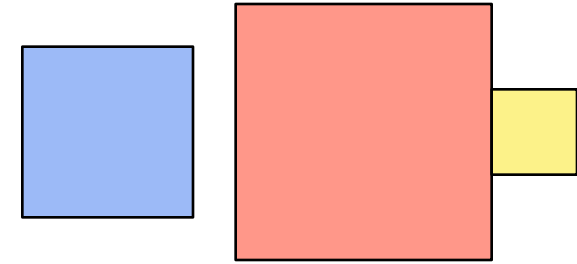
A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.



0-free



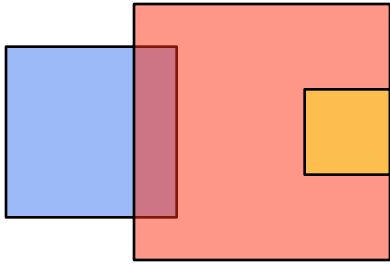
$\frac{3}{4}$ -free



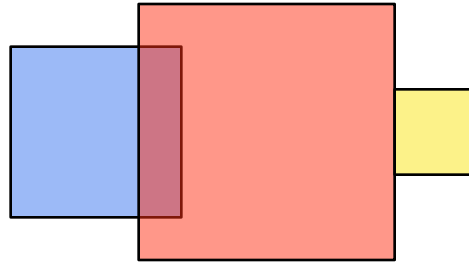
1-free

α -free Intersection Graphs

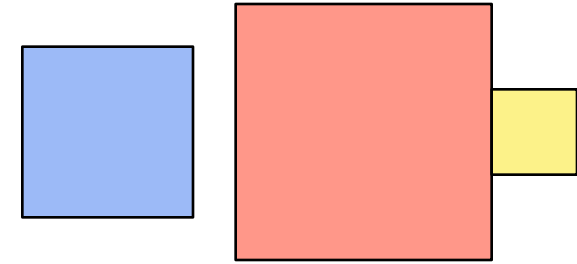
A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.



0-free



$\frac{3}{4}$ -free

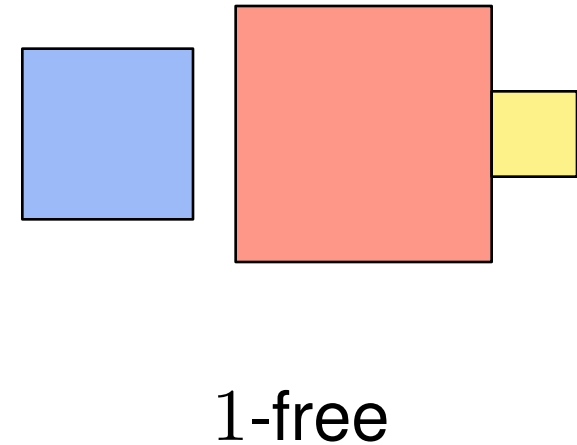
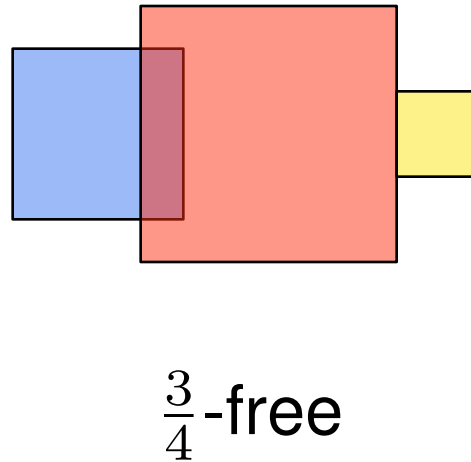
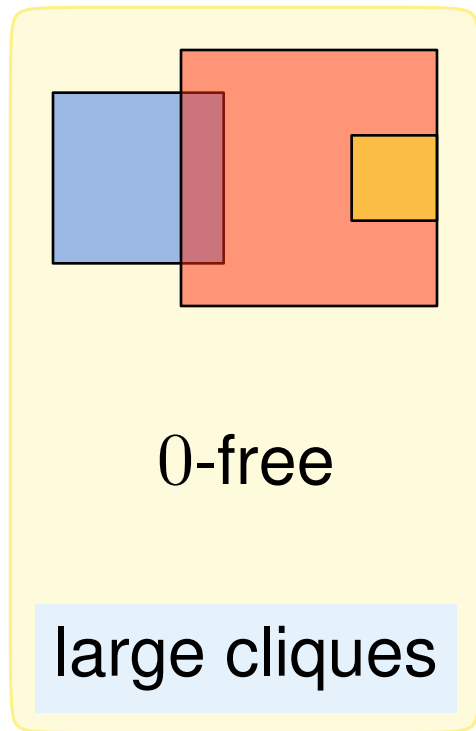


1-free

large cliques

α -free Intersection Graphs

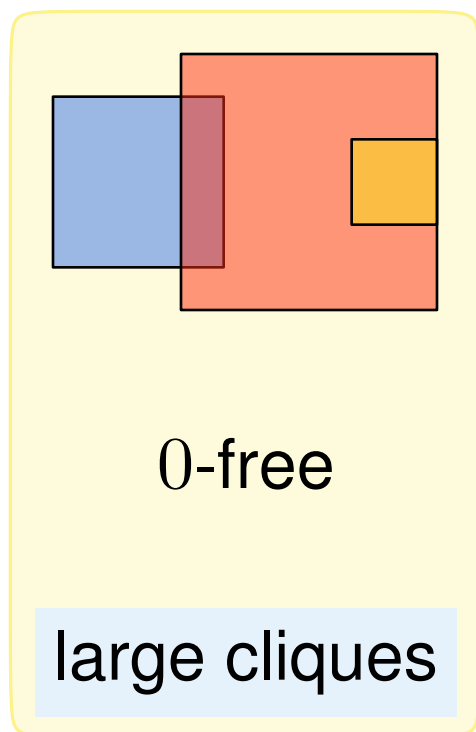
A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.



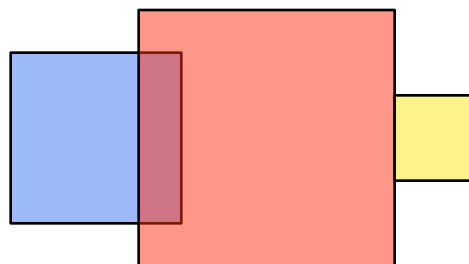
no product structure

α -free Intersection Graphs

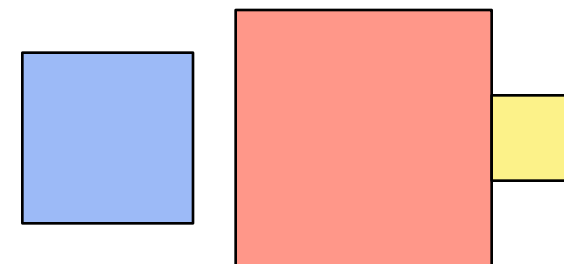
A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.



no product structure



$\frac{3}{4}$ -free

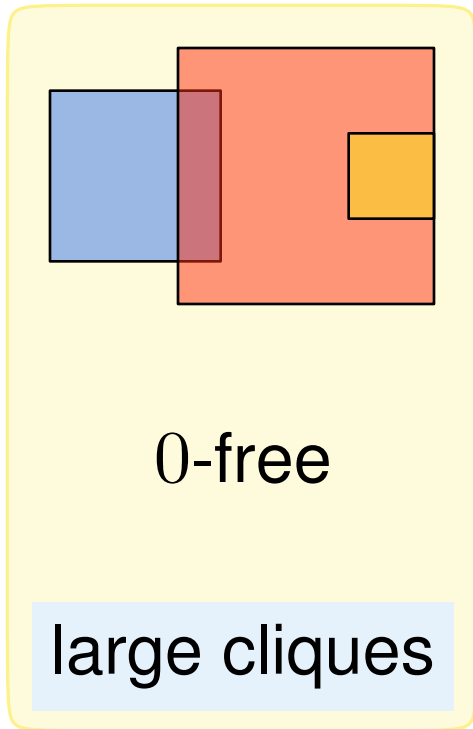


1-free

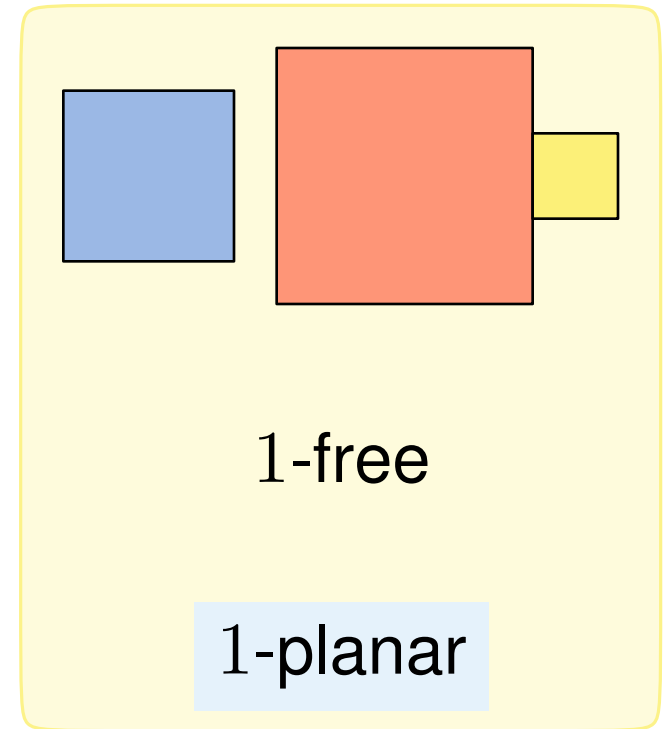
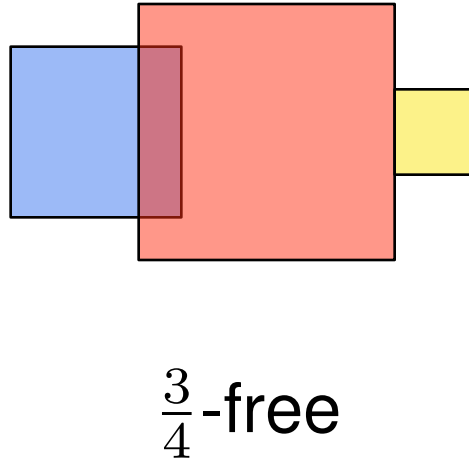
1-planar

α -free Intersection Graphs

A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.



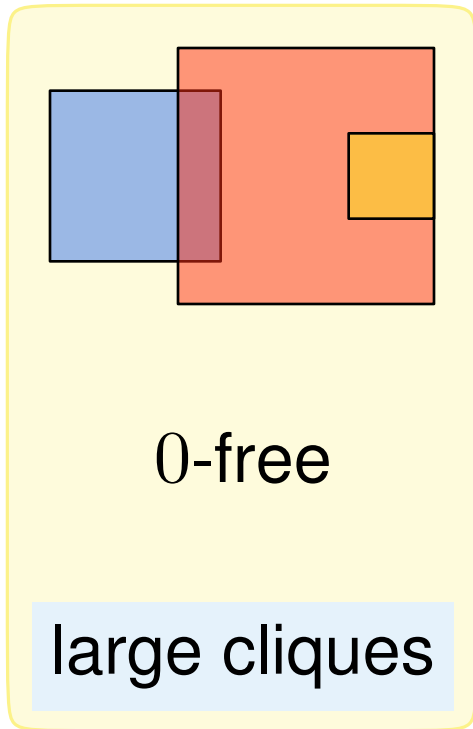
no product structure



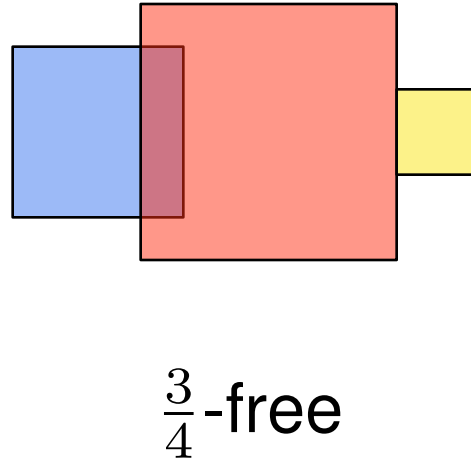
product structure

α -free Intersection Graphs

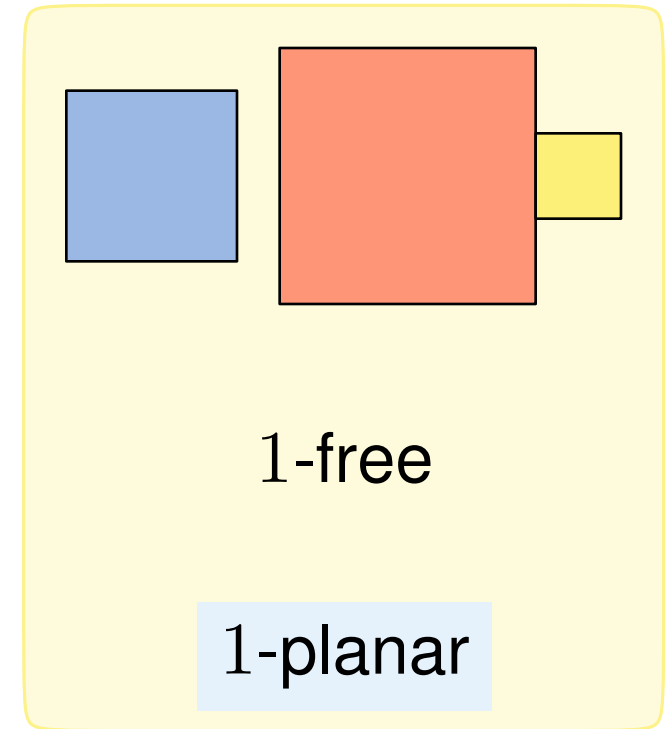
A set $\mathcal{S}$ of shapes in the plane is α -free with $\alpha \in [0, 1]$ if every shape $S \in \mathcal{S}$ has at least α of its area disjoint from all other shapes.



no product structure

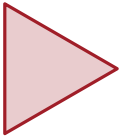


What about $\alpha \in (0, 1)$?

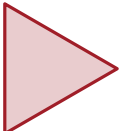


product structure

Our Results for Regular n -gons

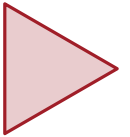
■ For  and  : **no** product structure for $\alpha < 1$.

Our Results for Regular n -gons

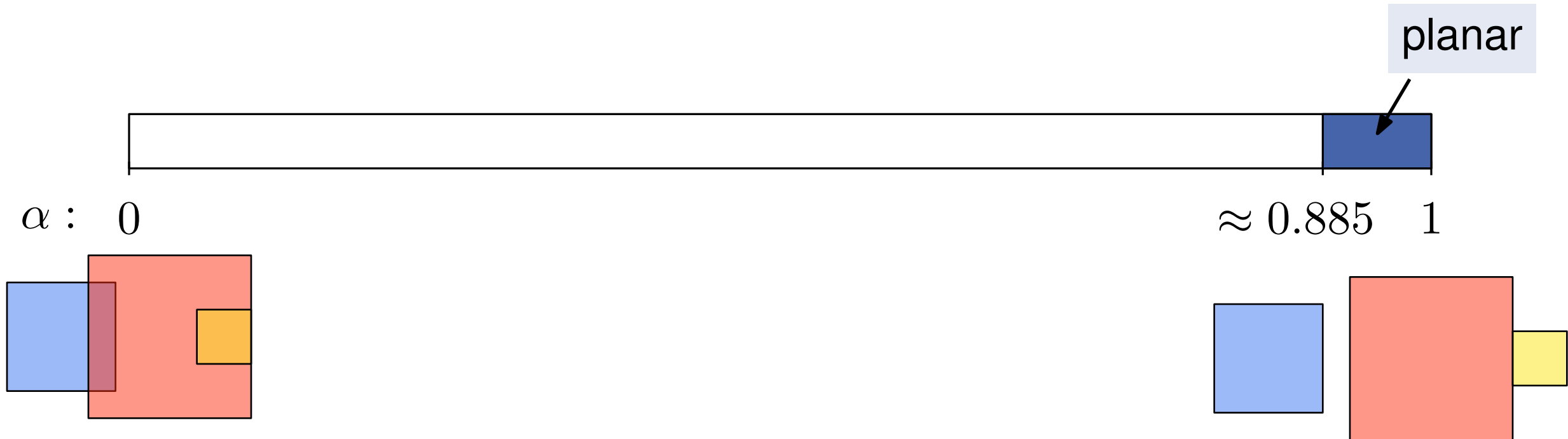
- For  and  : **no** product structure for $\alpha < 1$.
- For even $n \geq 6$:



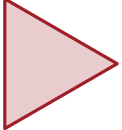
Our Results for Regular n -gons

■ For  and  : **no** product structure for $\alpha < 1$.

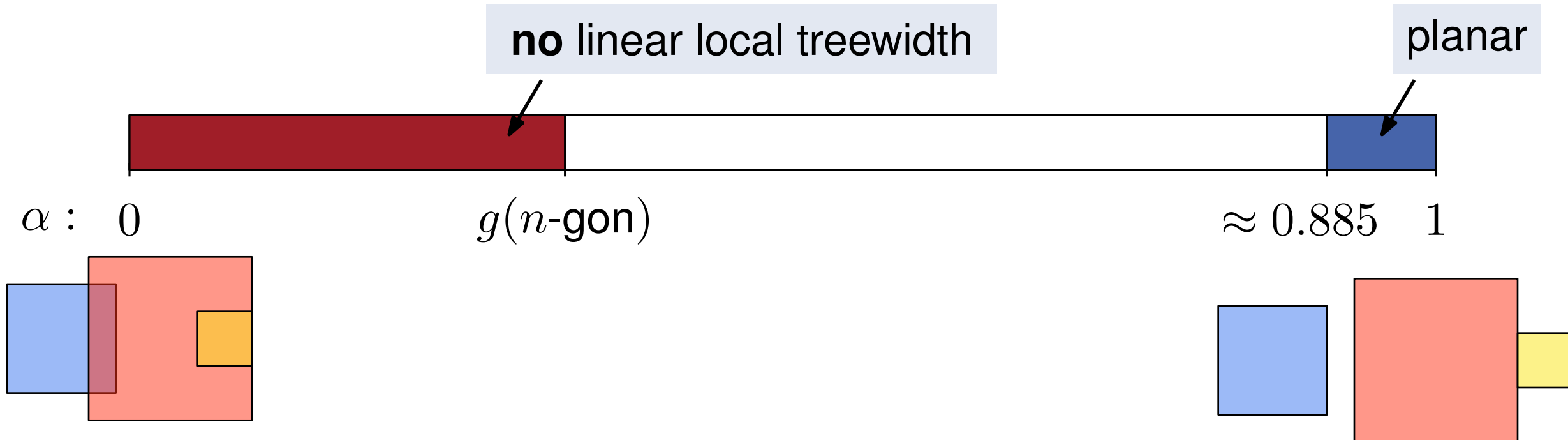
■ For even $n \geq 6$:



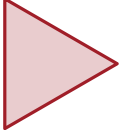
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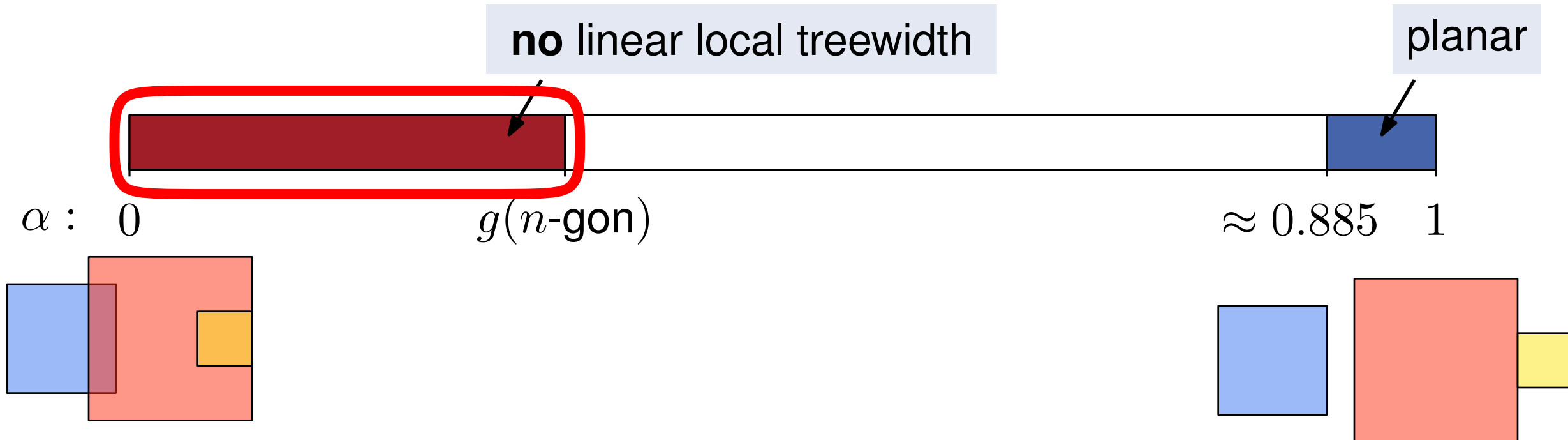
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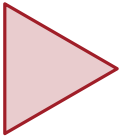
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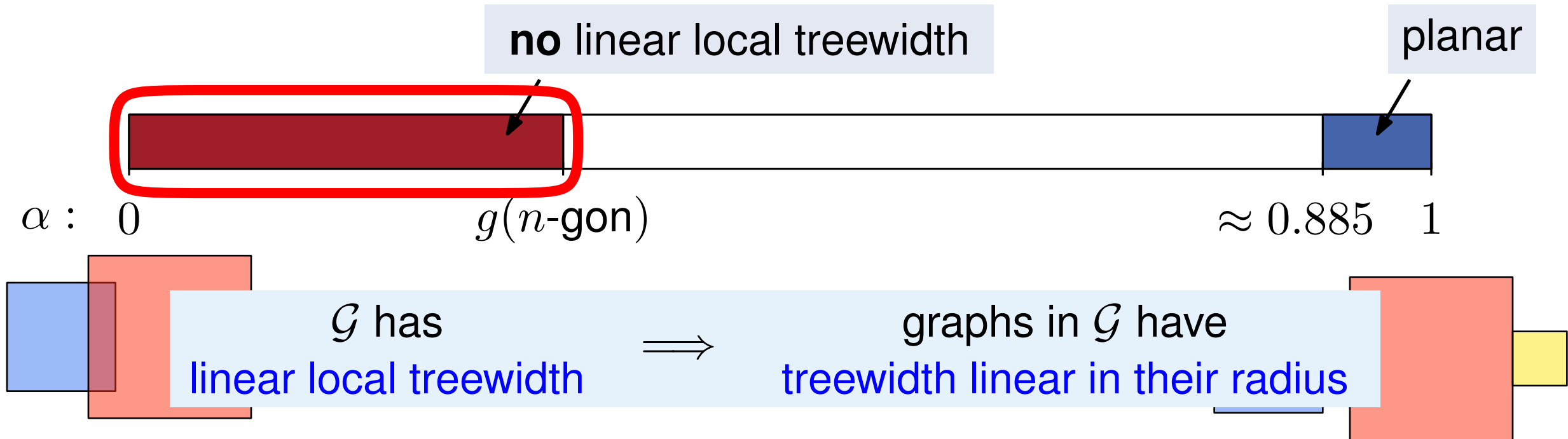
■ For even $n \geq 6$:



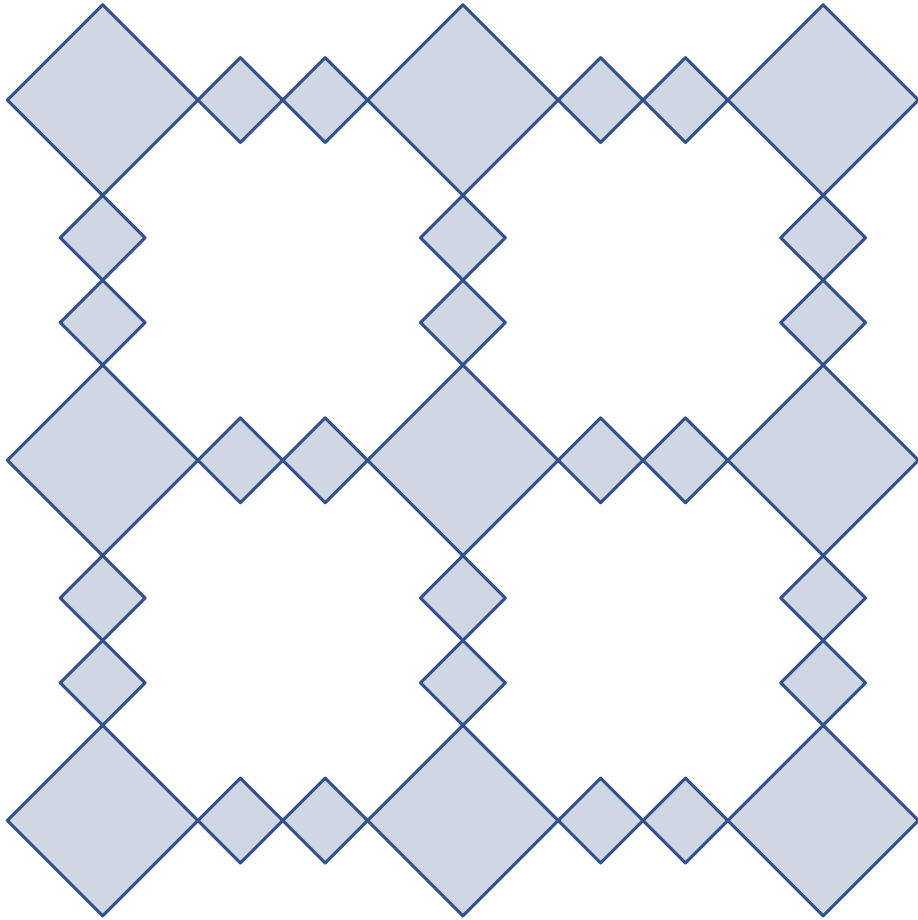
Our Results for Regular n -gons

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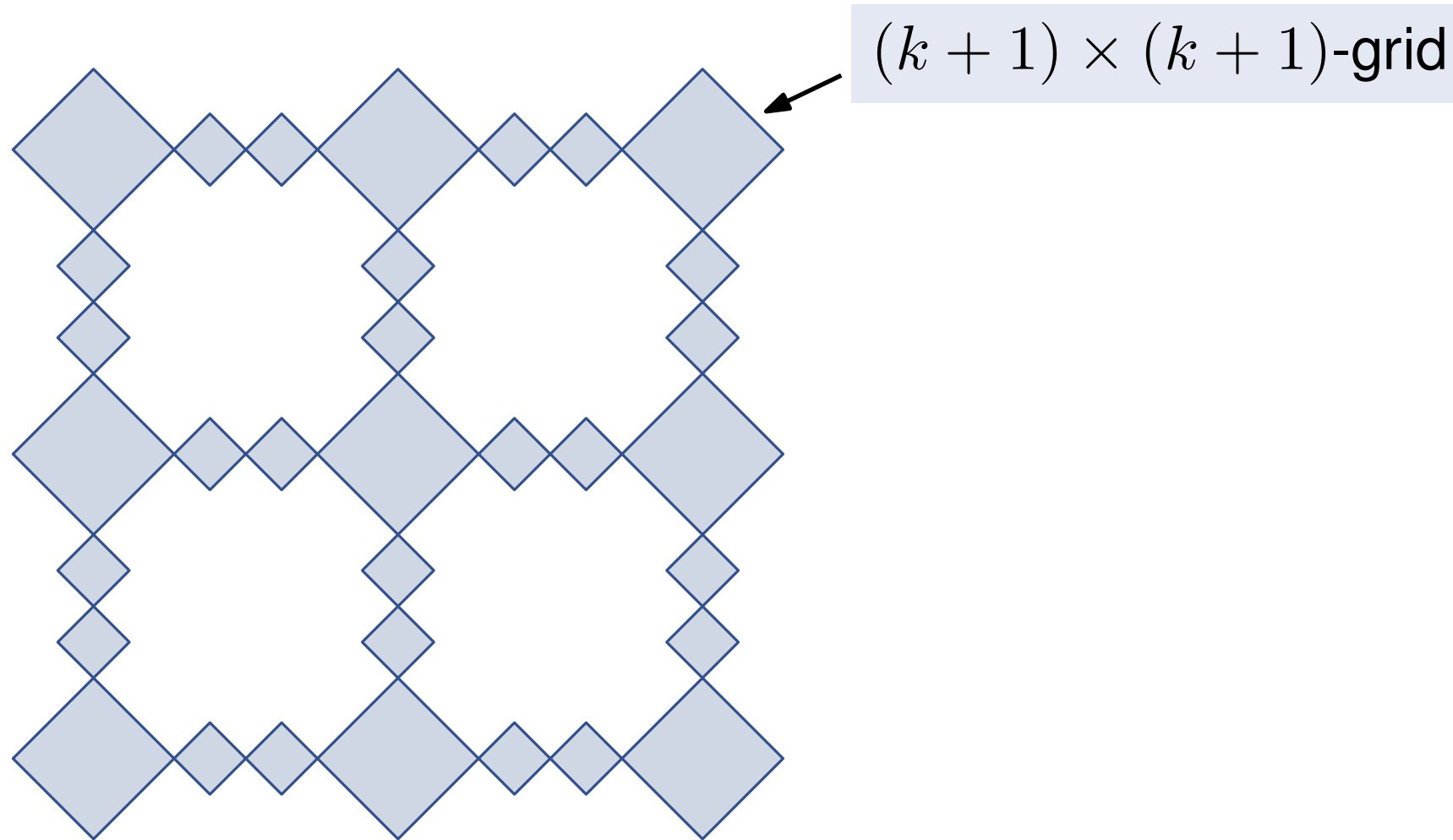
■ For even $n \geq 6$:



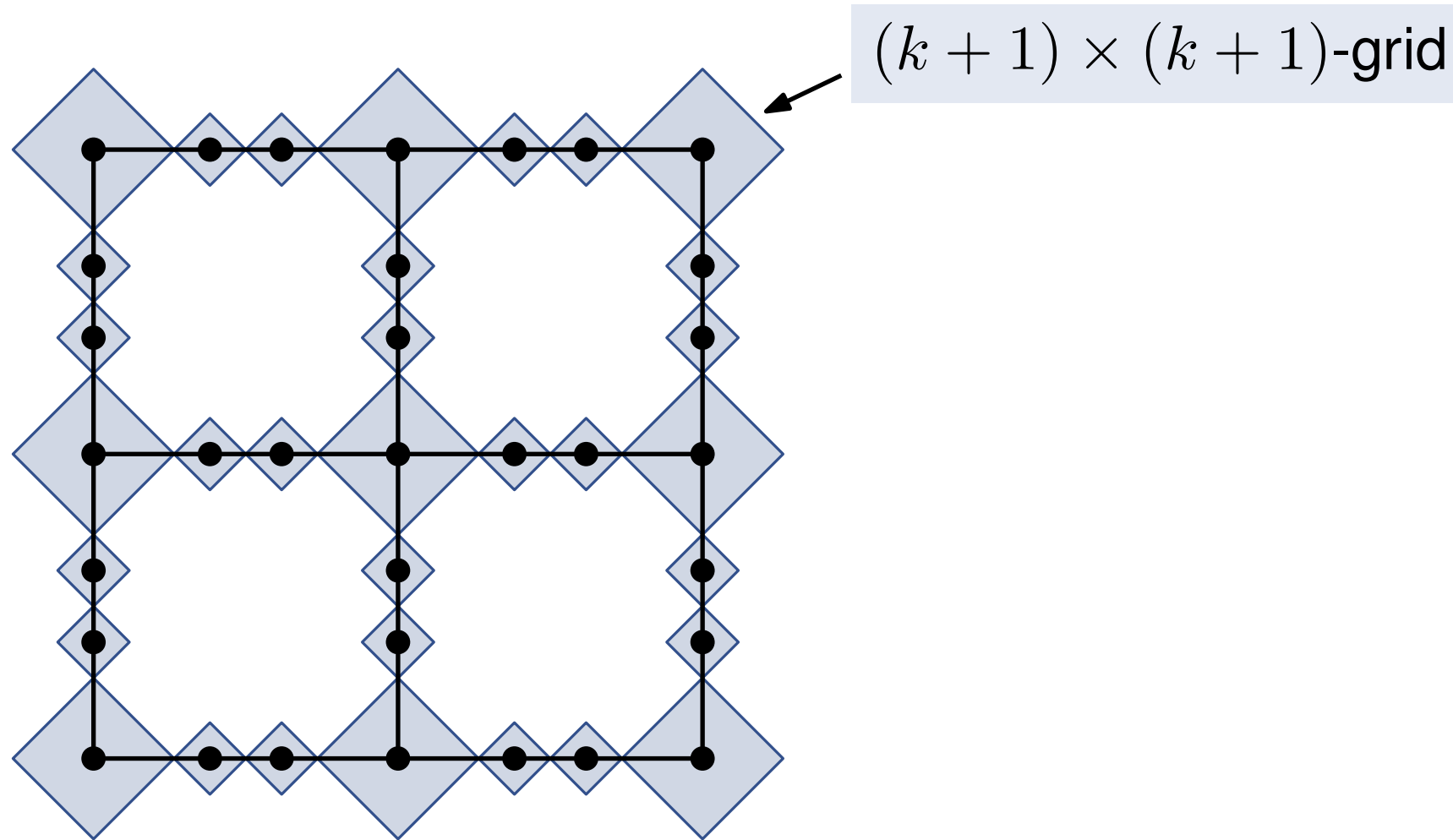
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



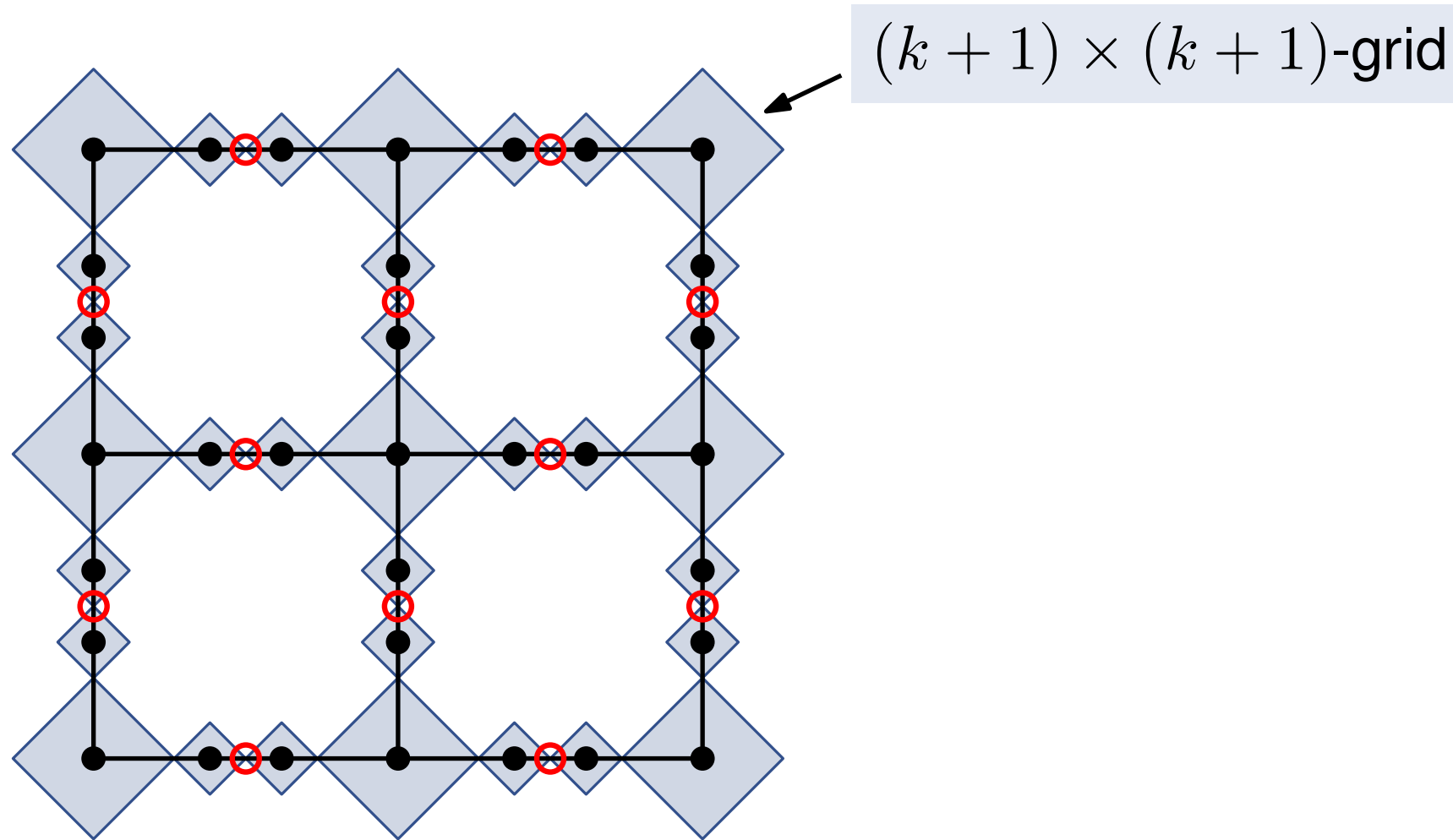
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



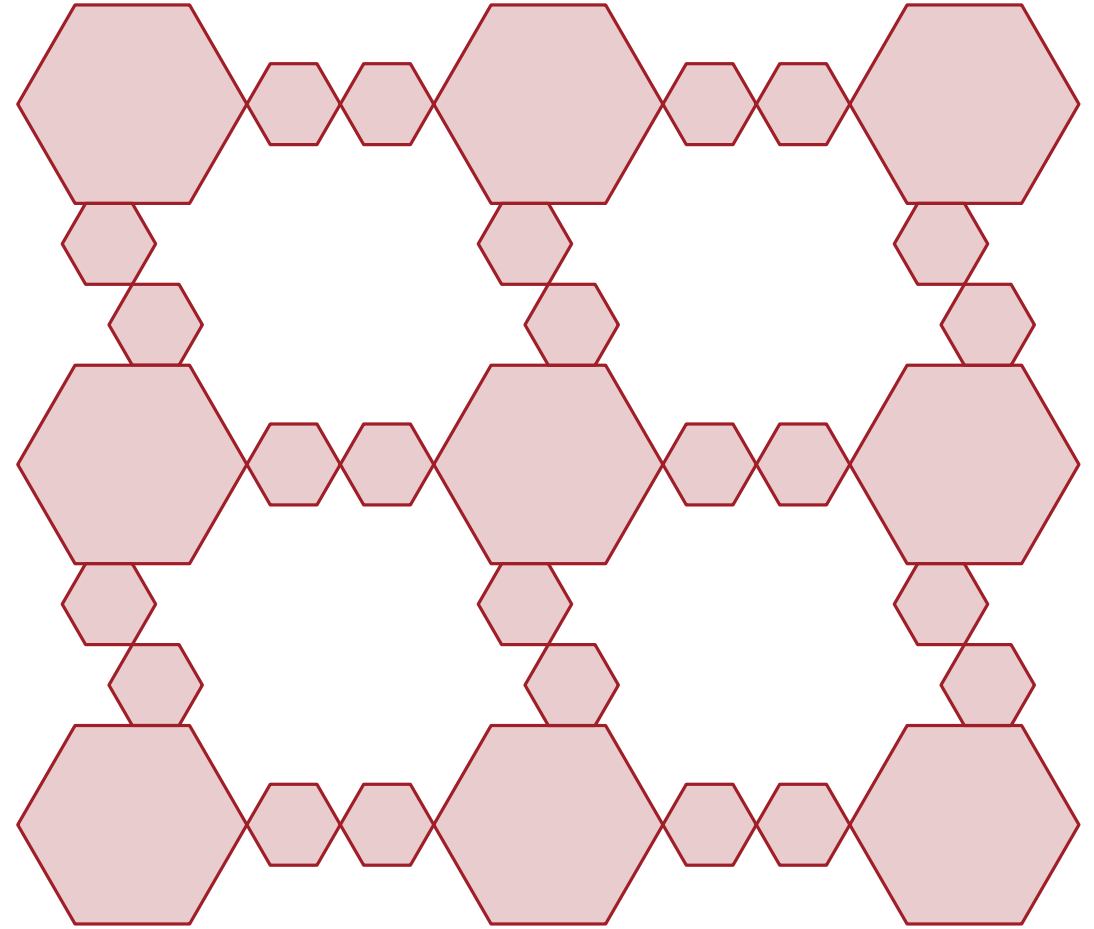
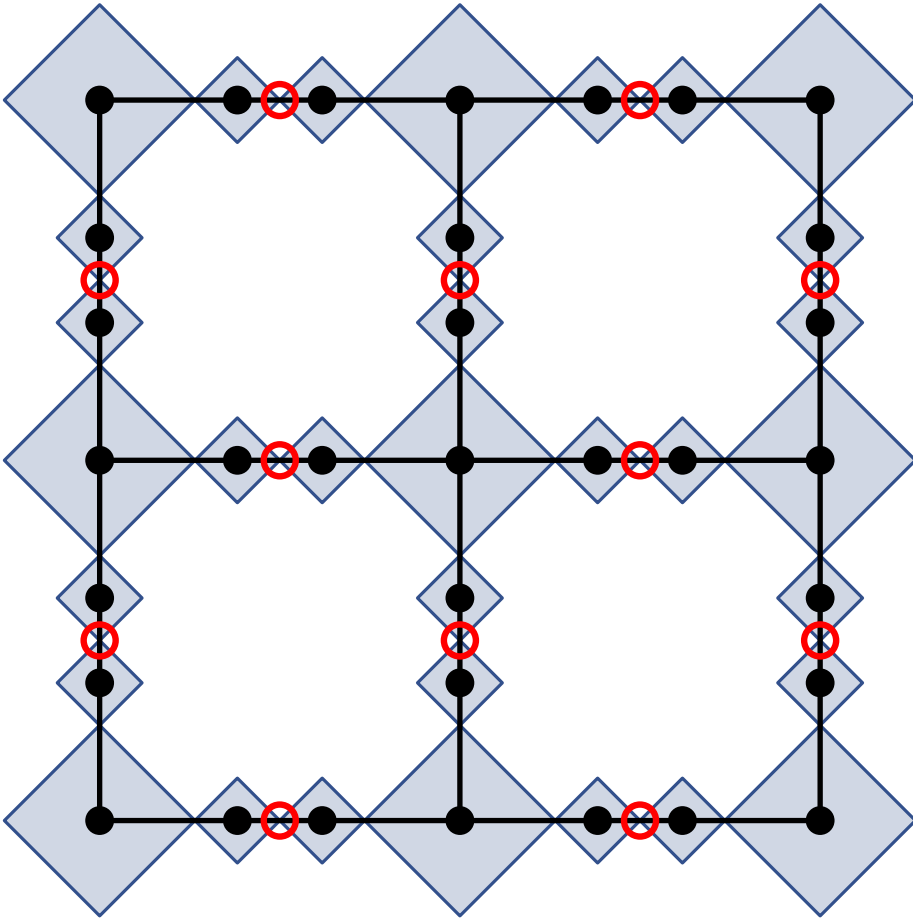
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



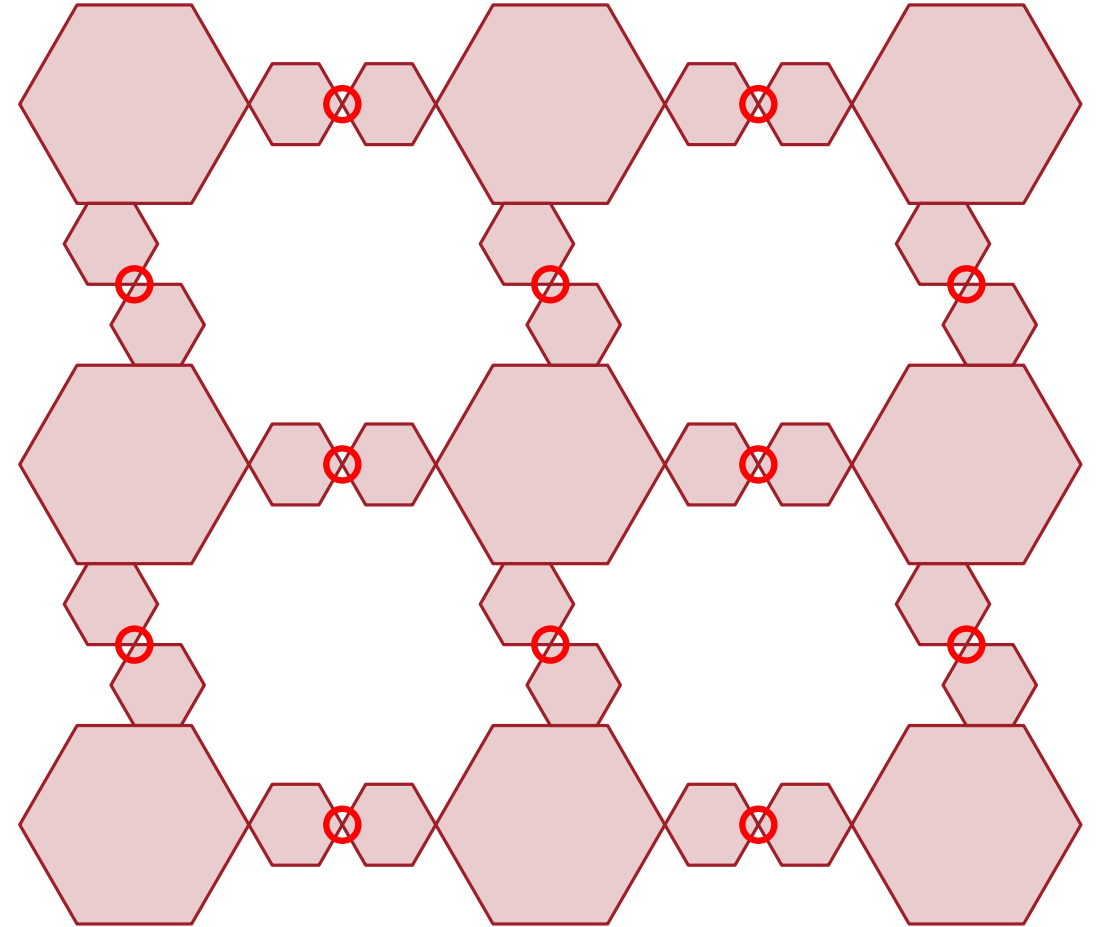
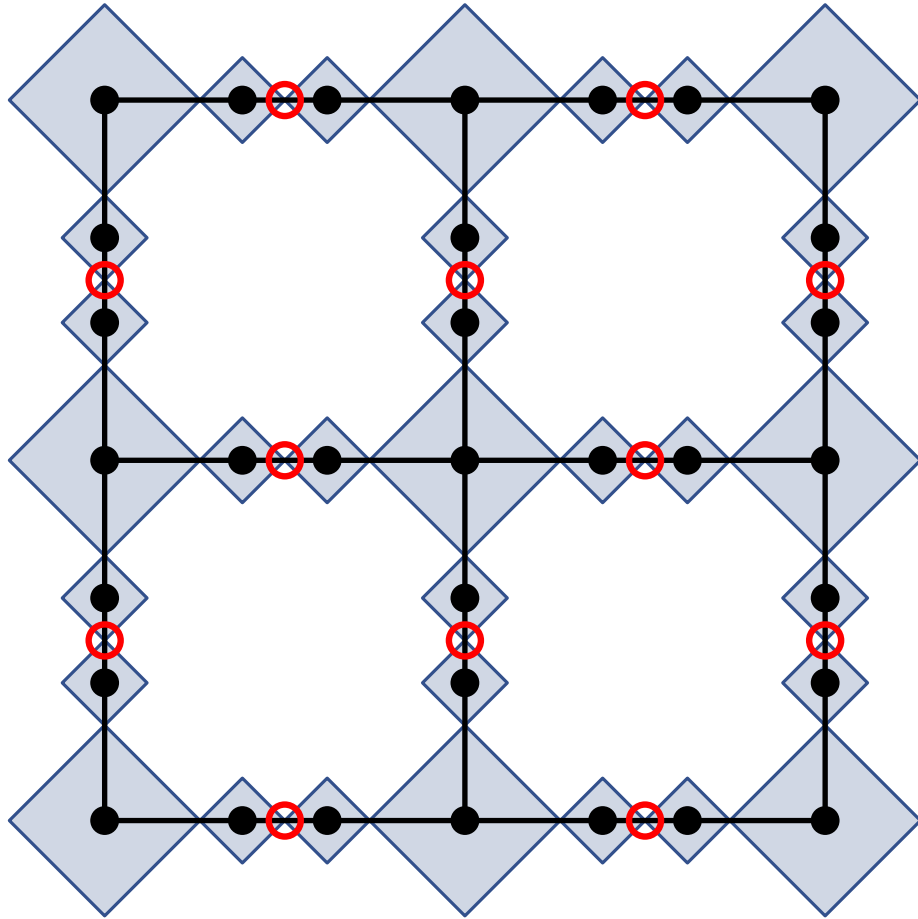
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



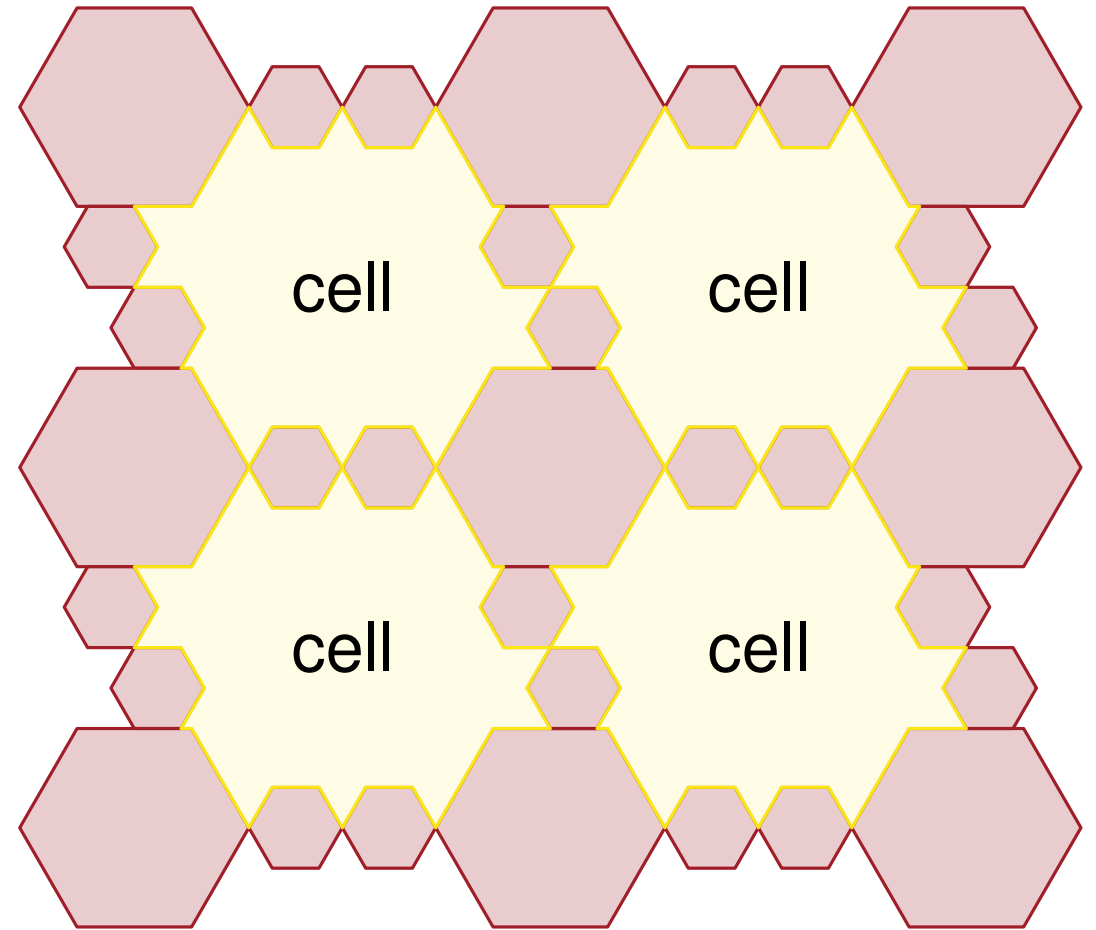
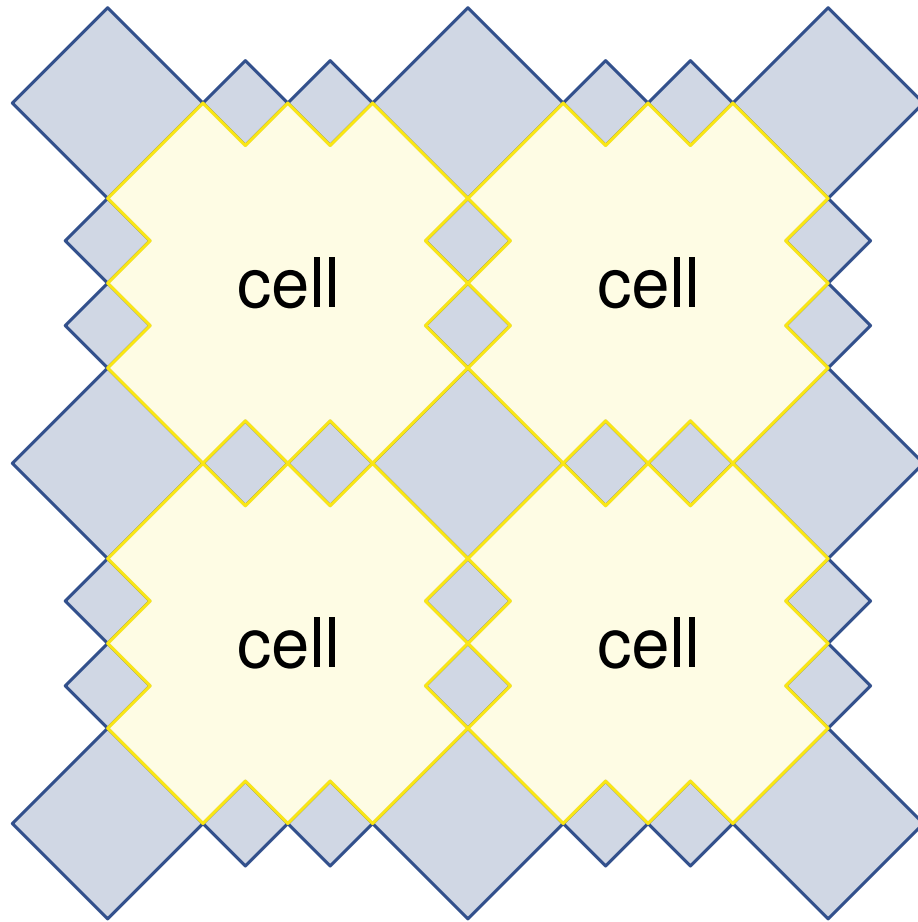
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



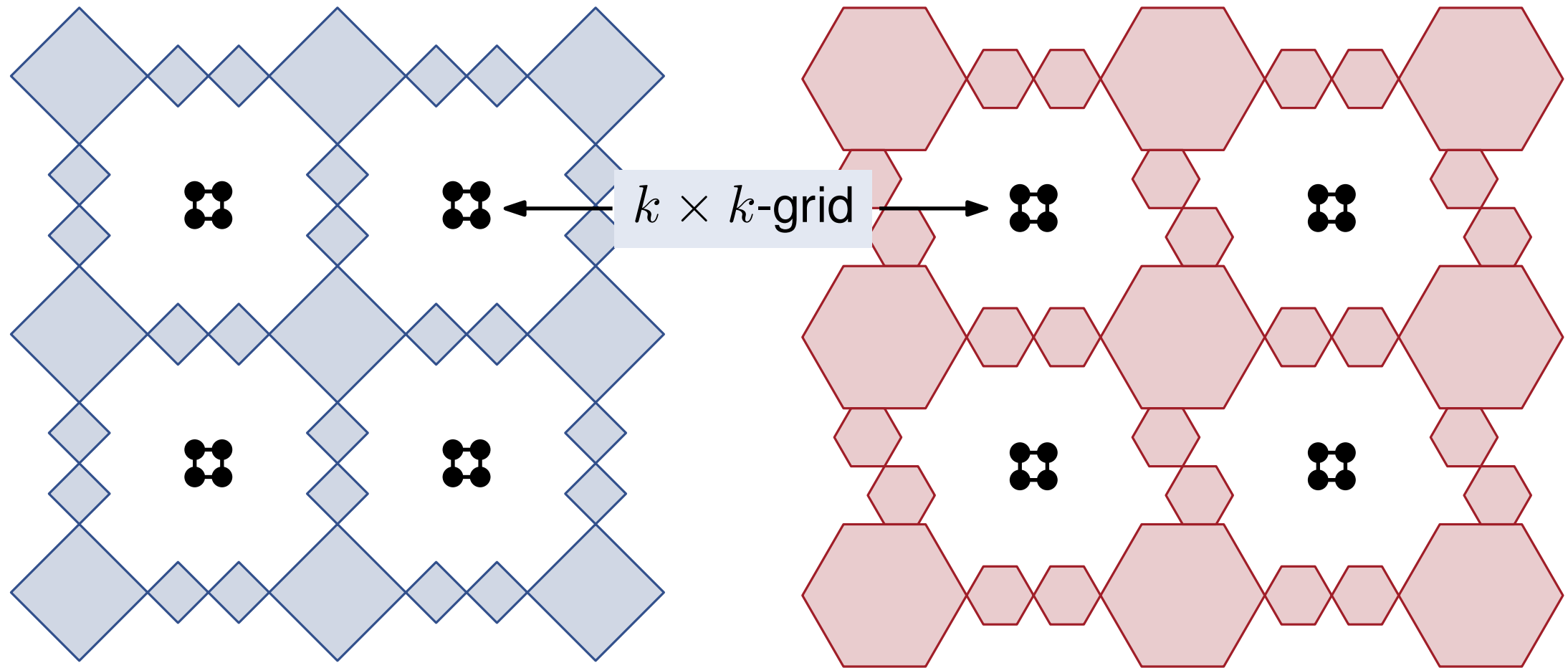
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



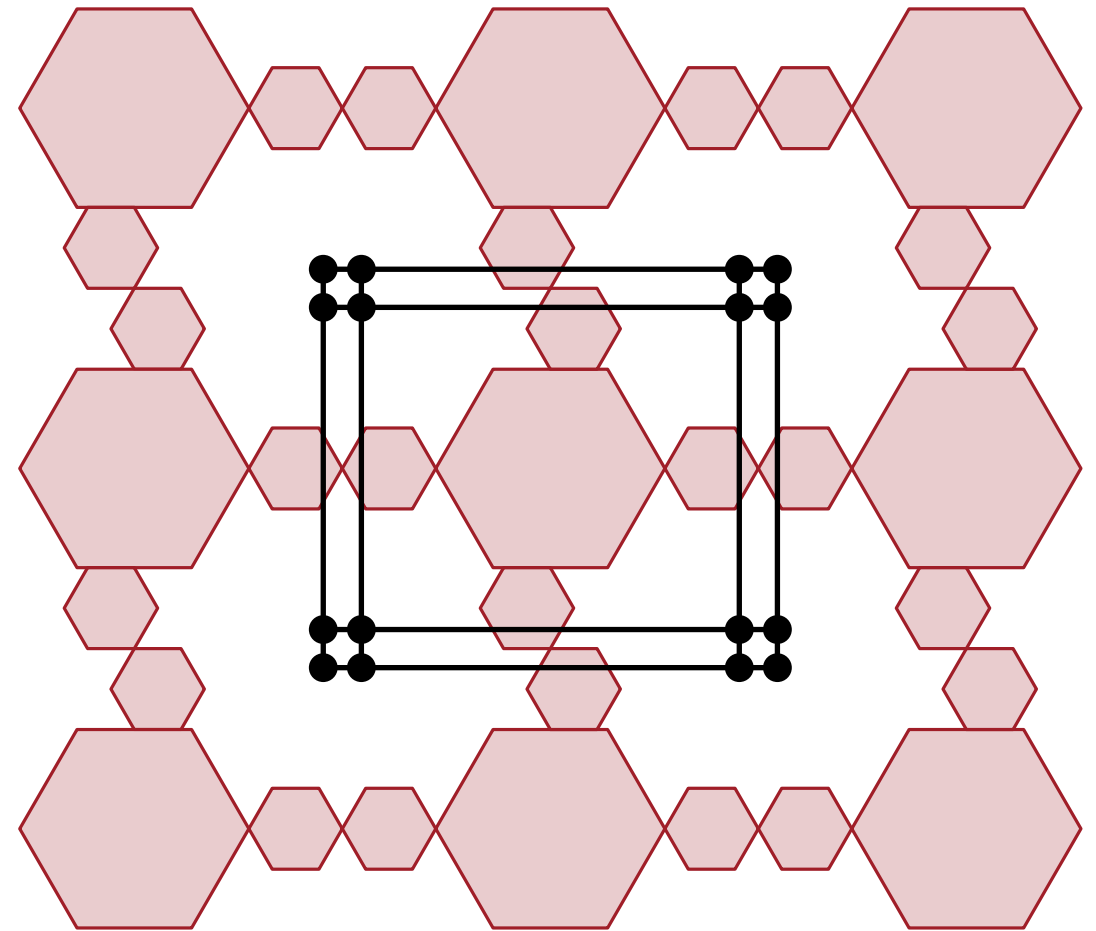
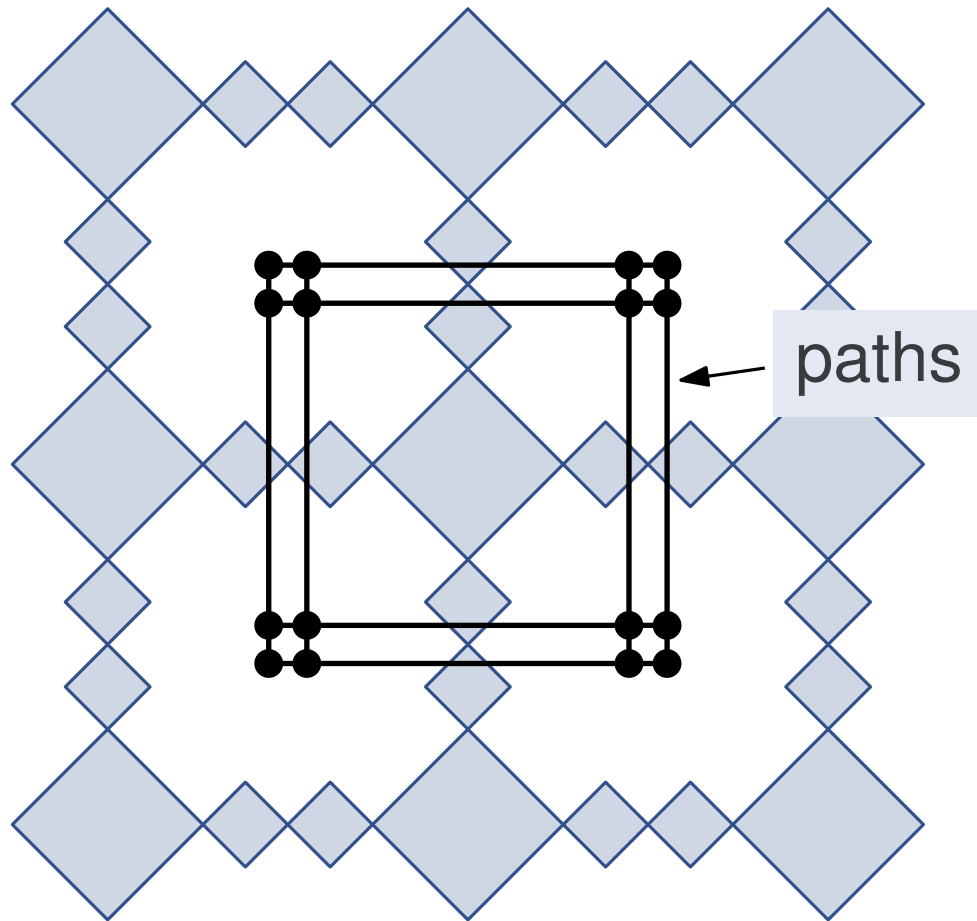
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



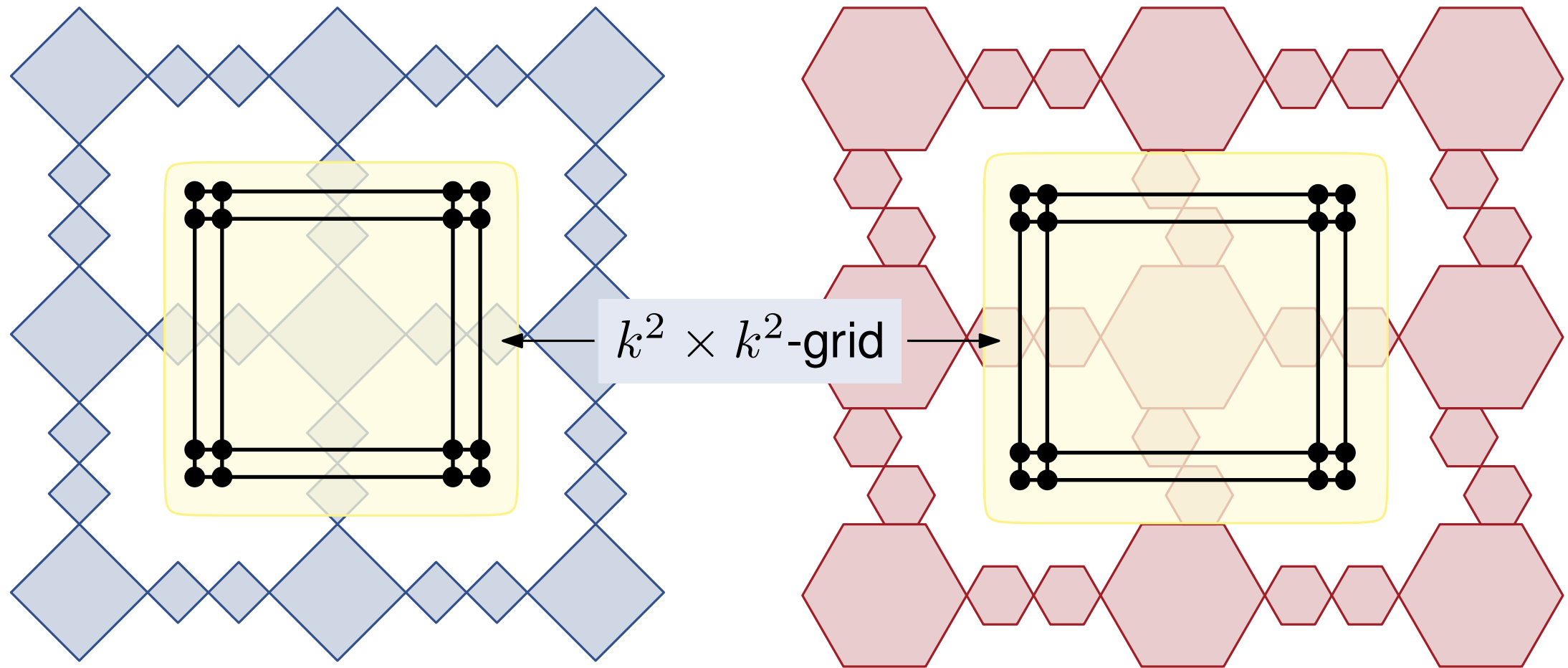
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



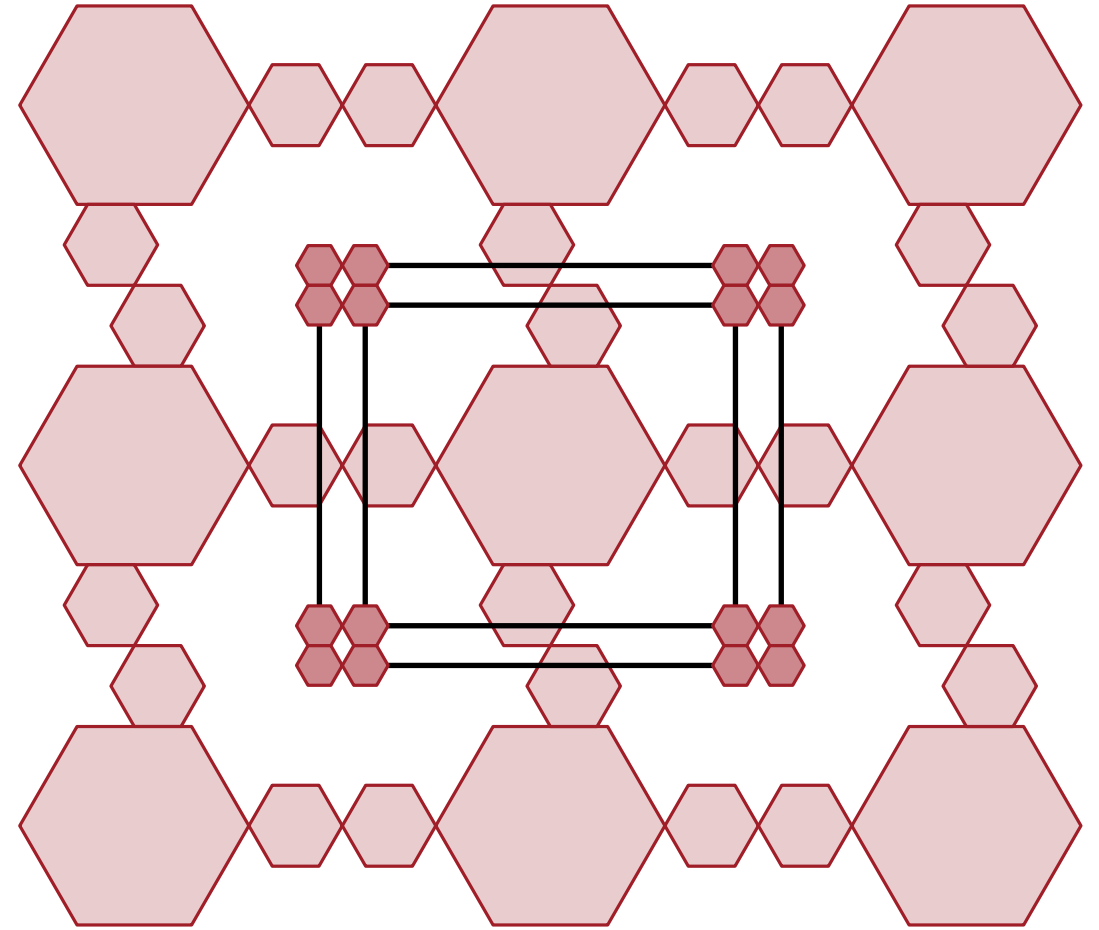
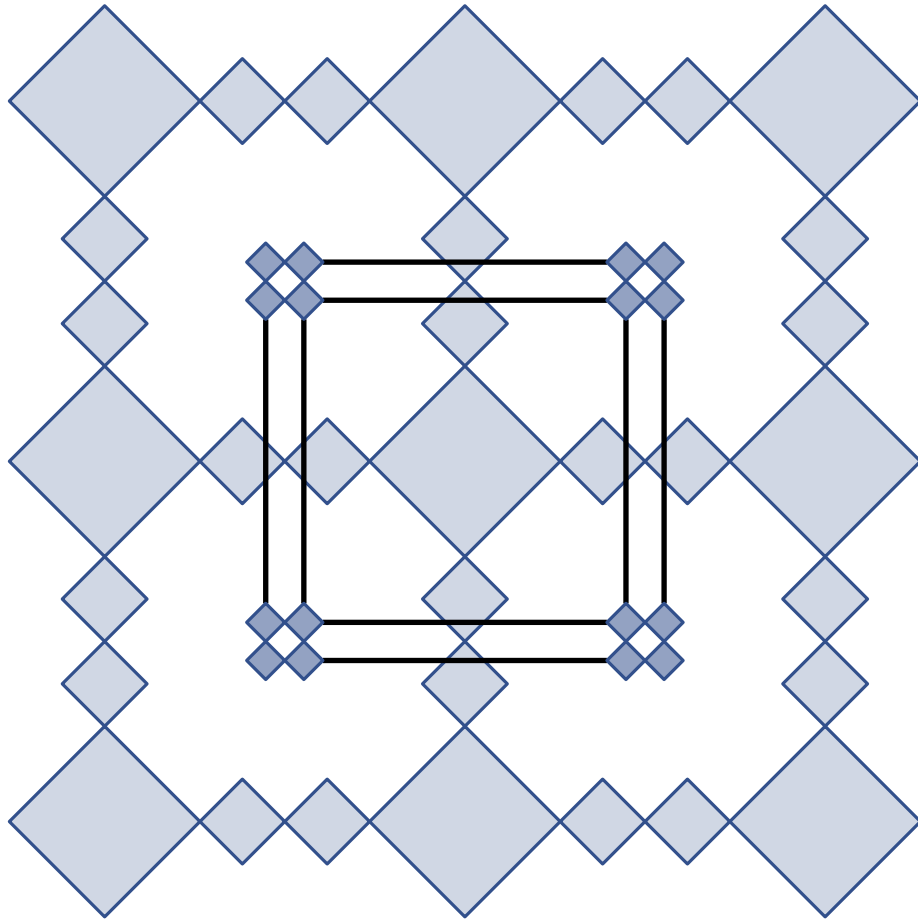
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



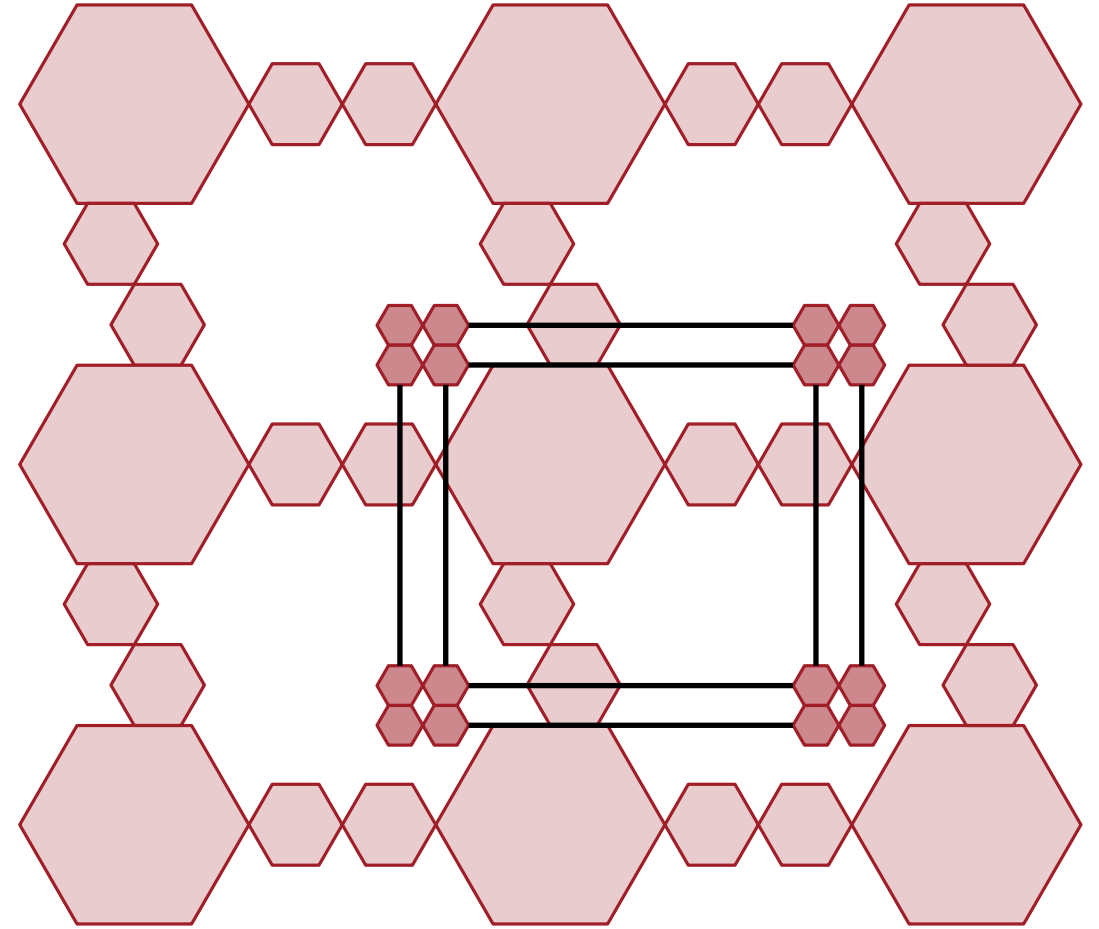
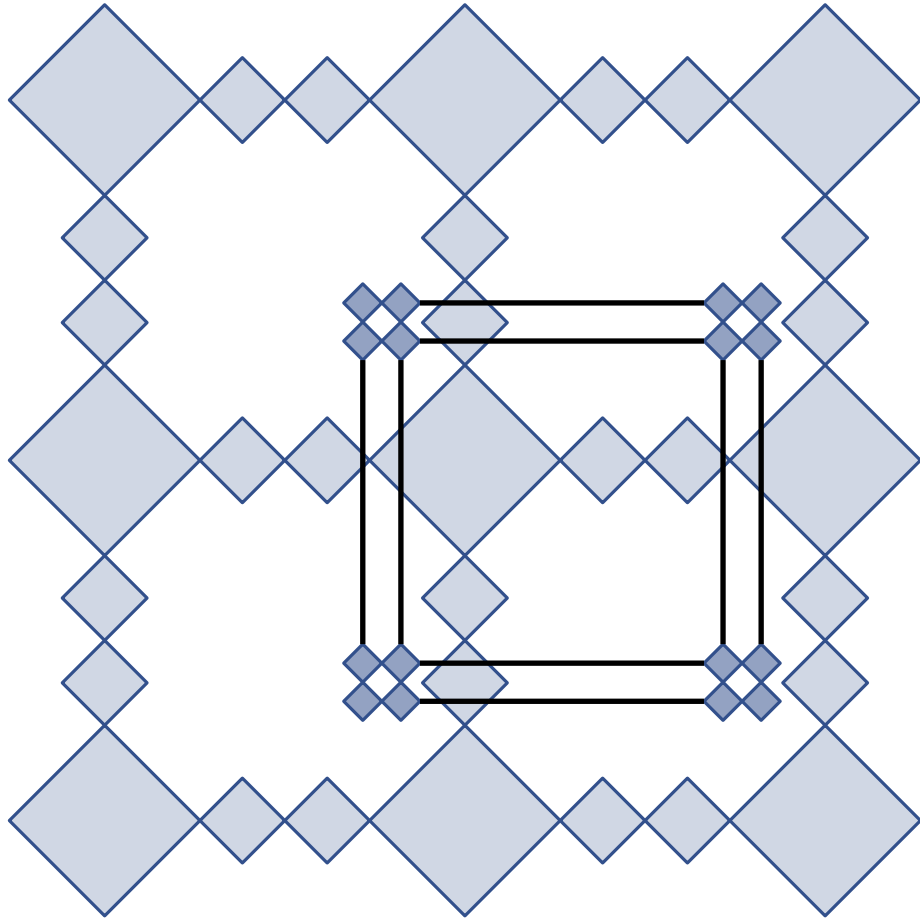
Constructing Graphs with Radius $\mathcal{O}(k)$ and Treewidth $\Omega(k^2)$



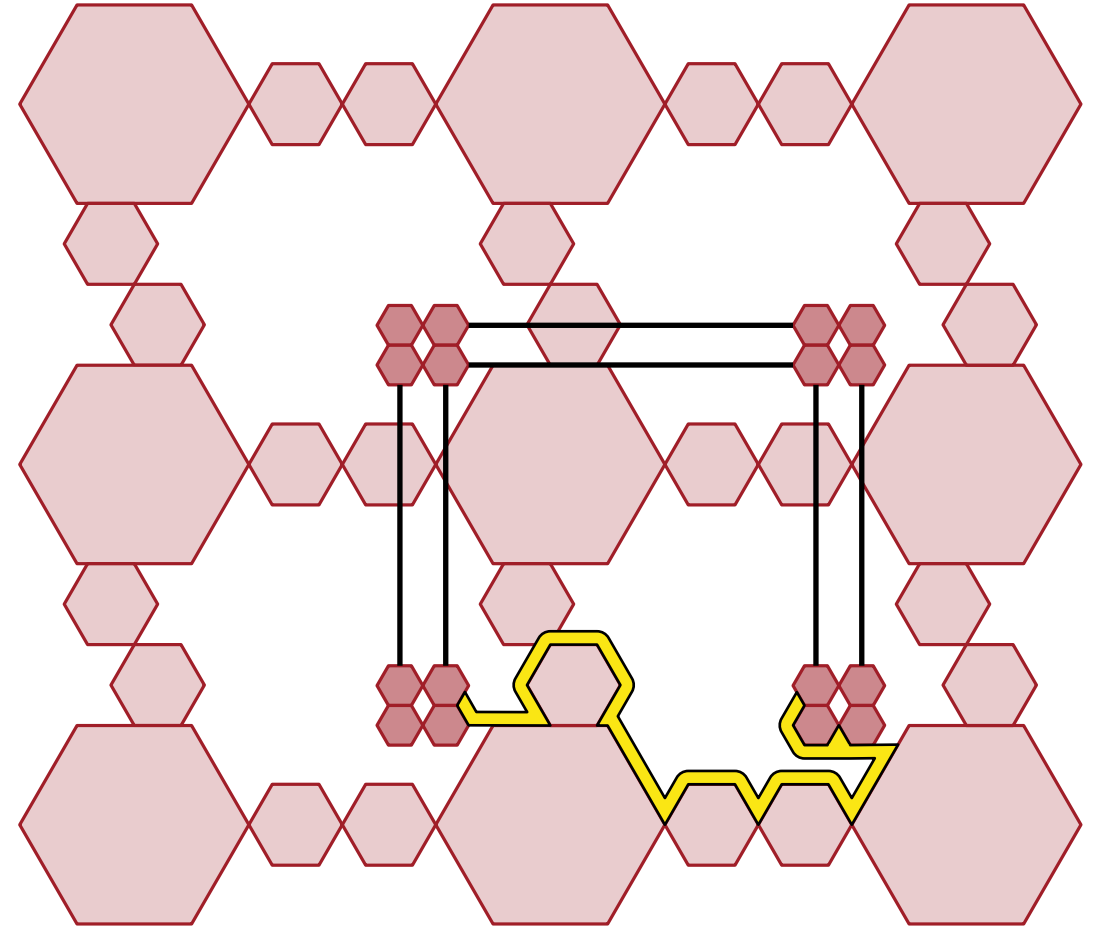
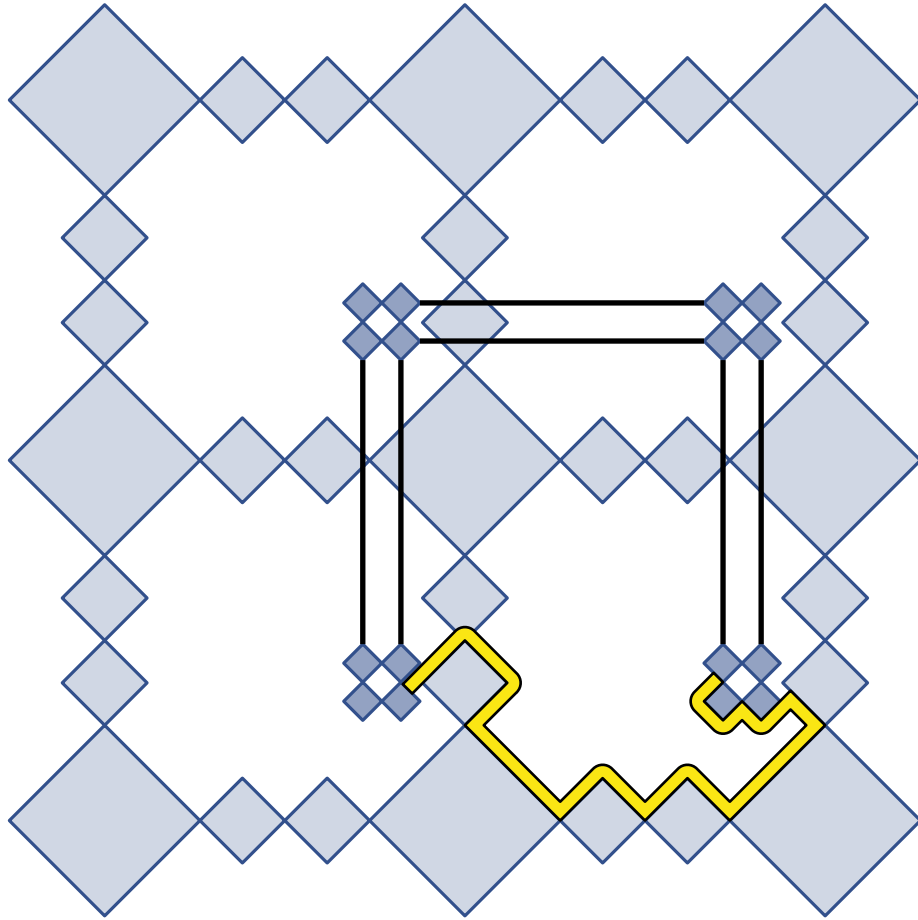
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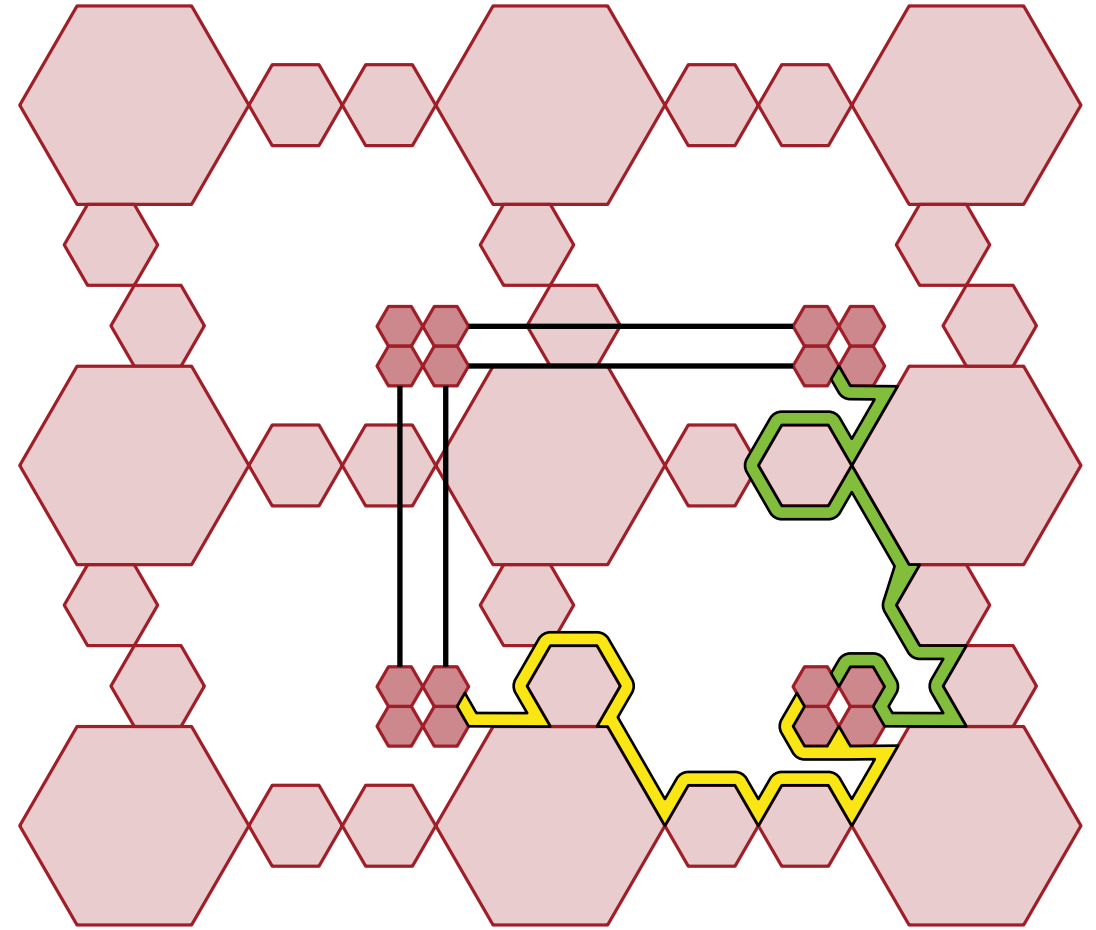
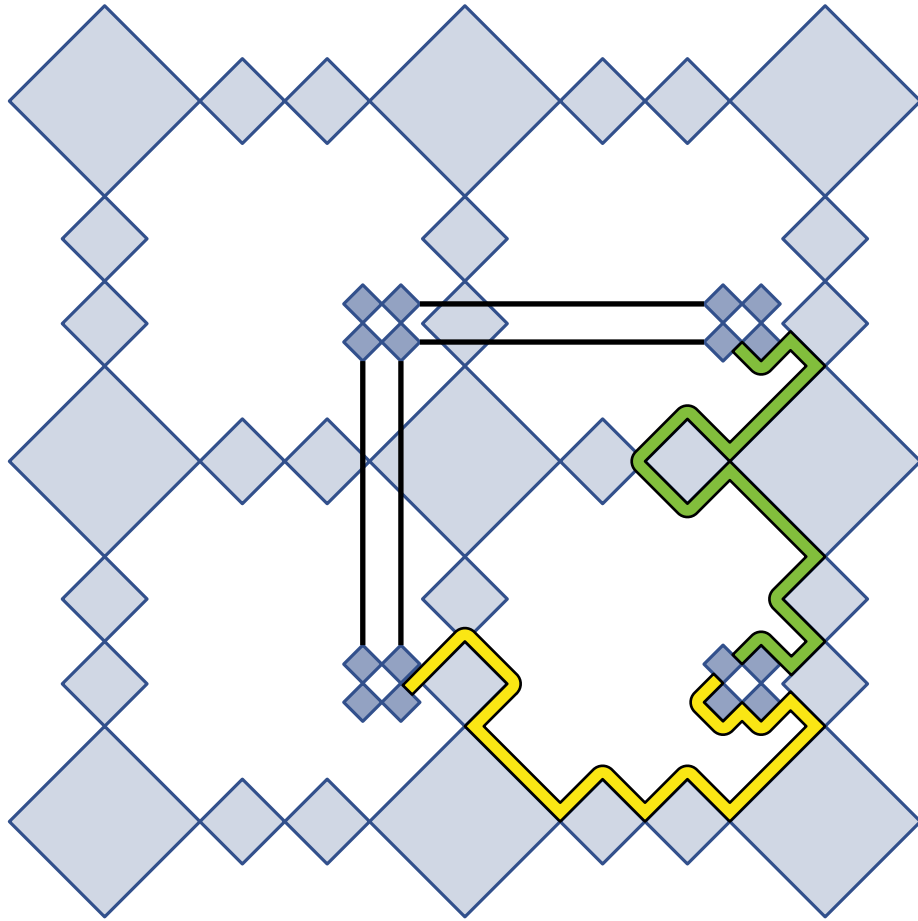
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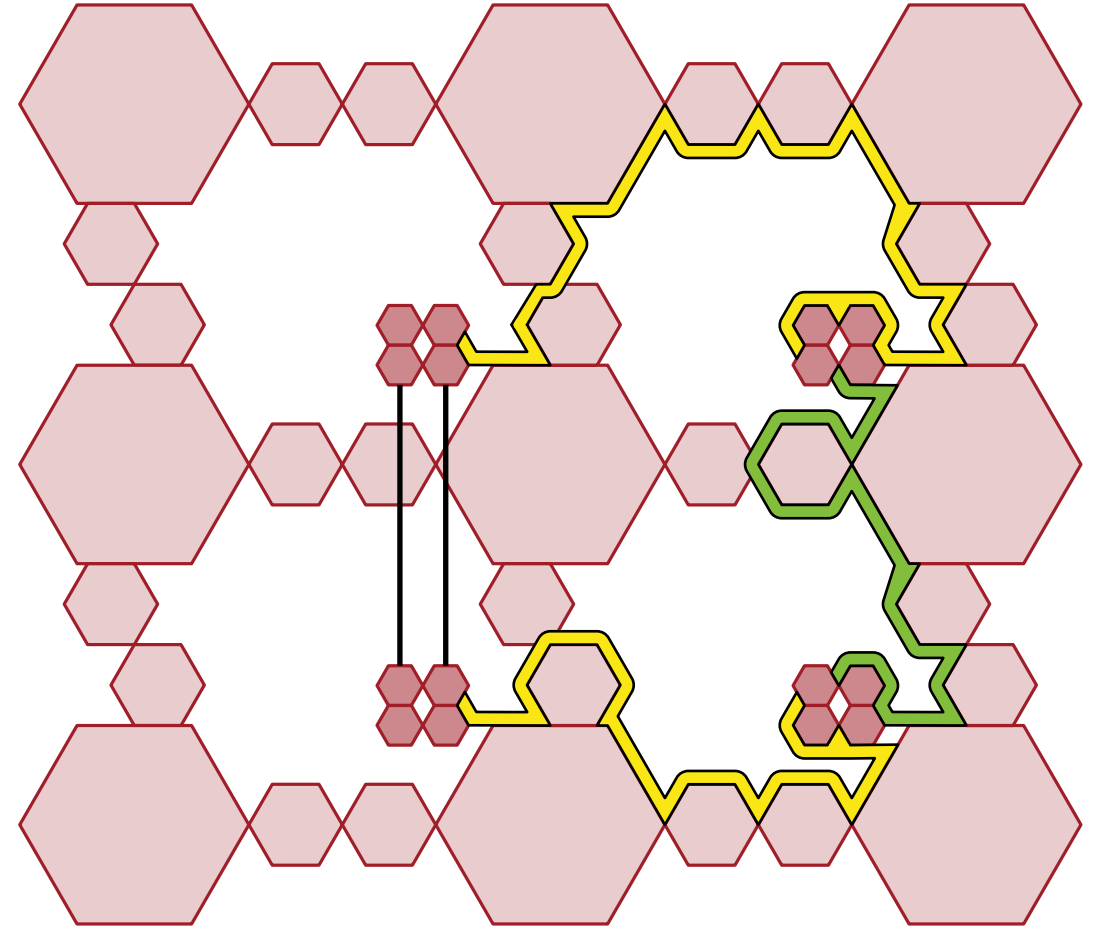
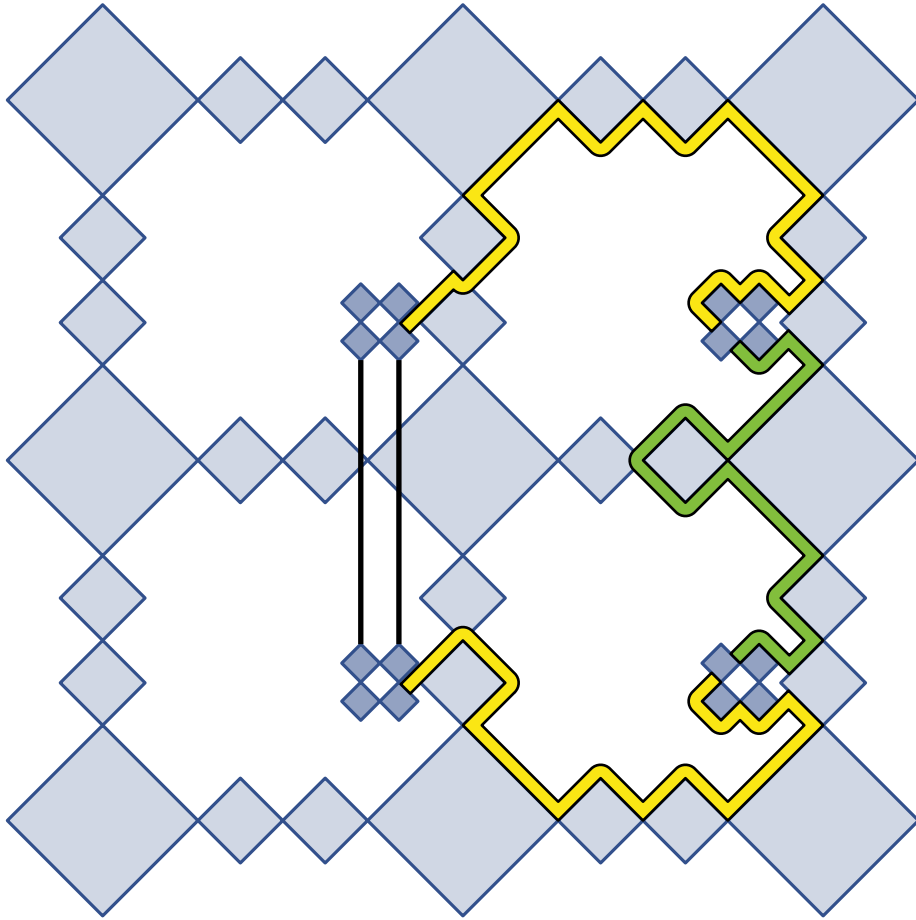
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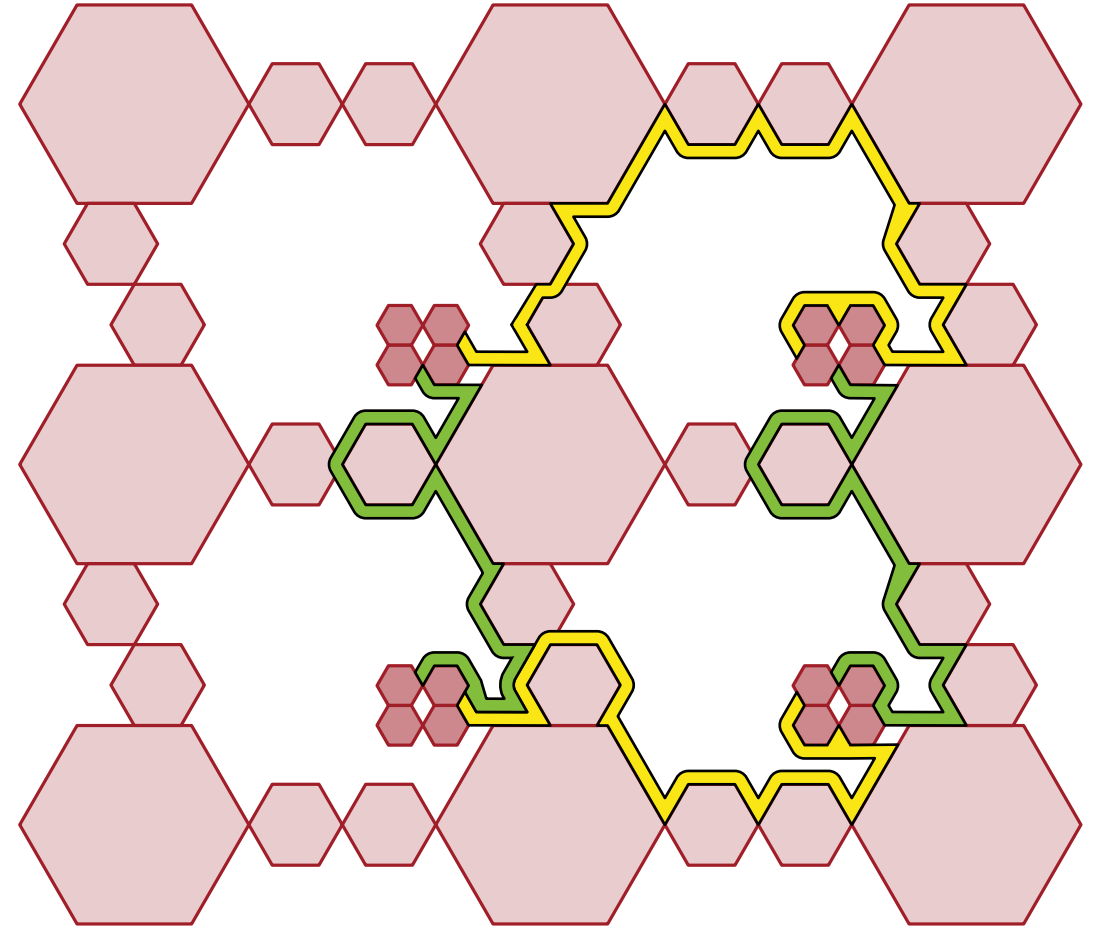
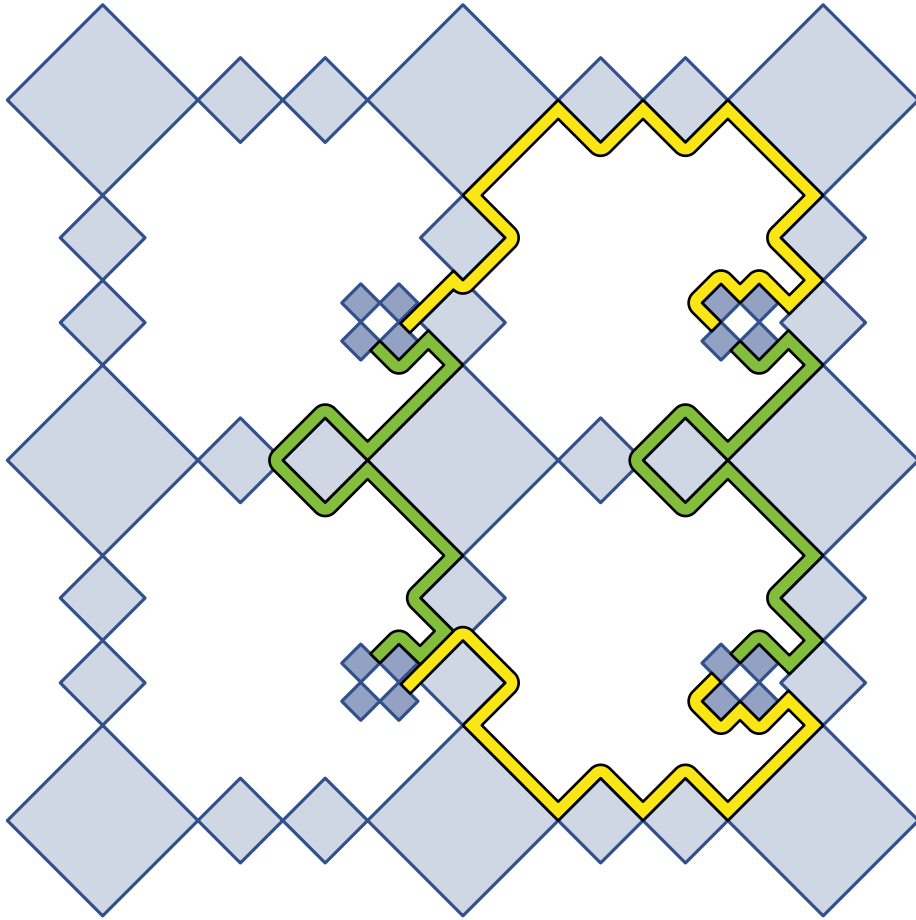
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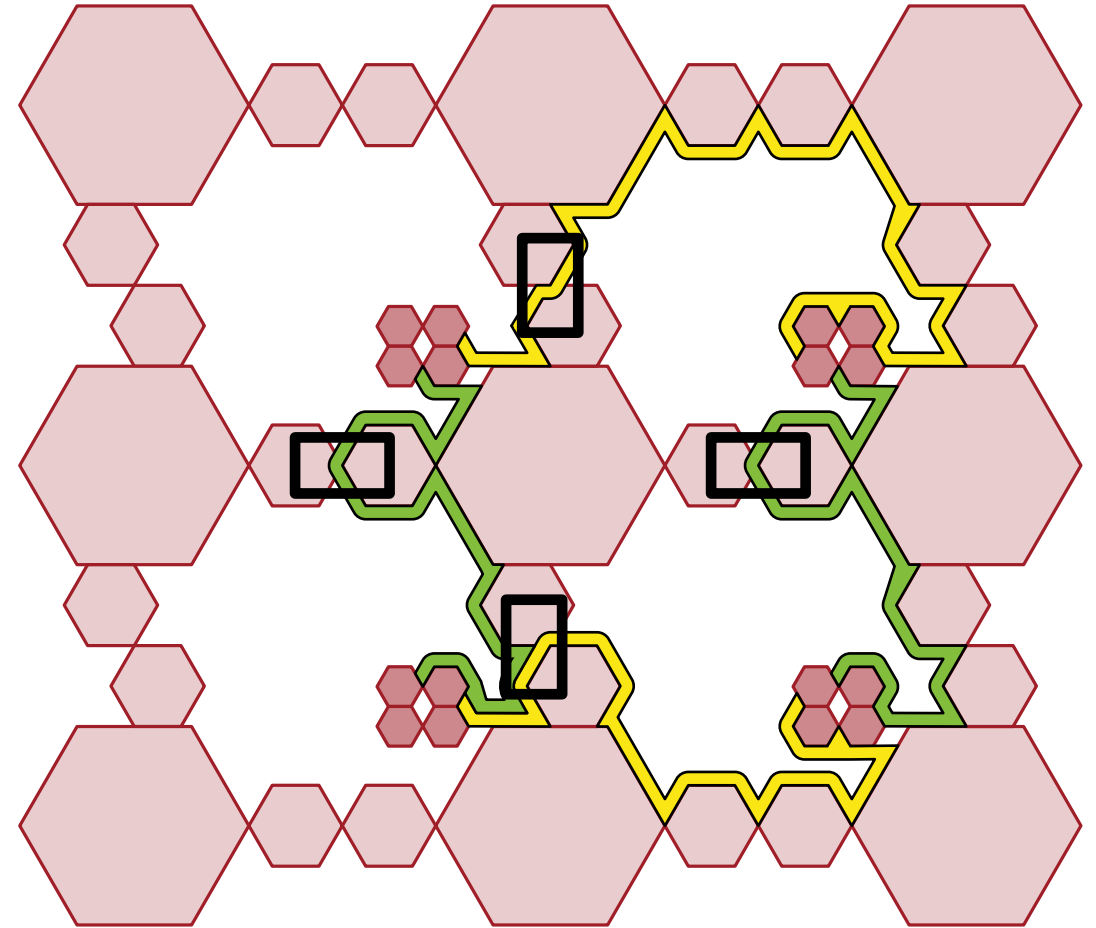
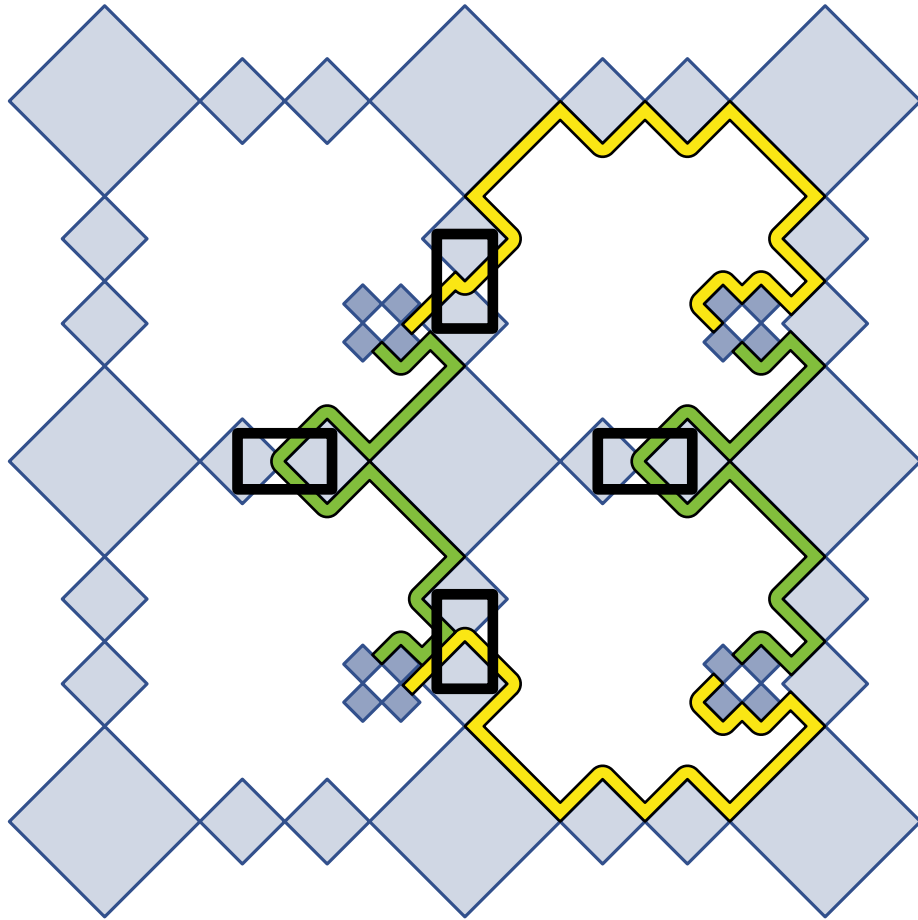
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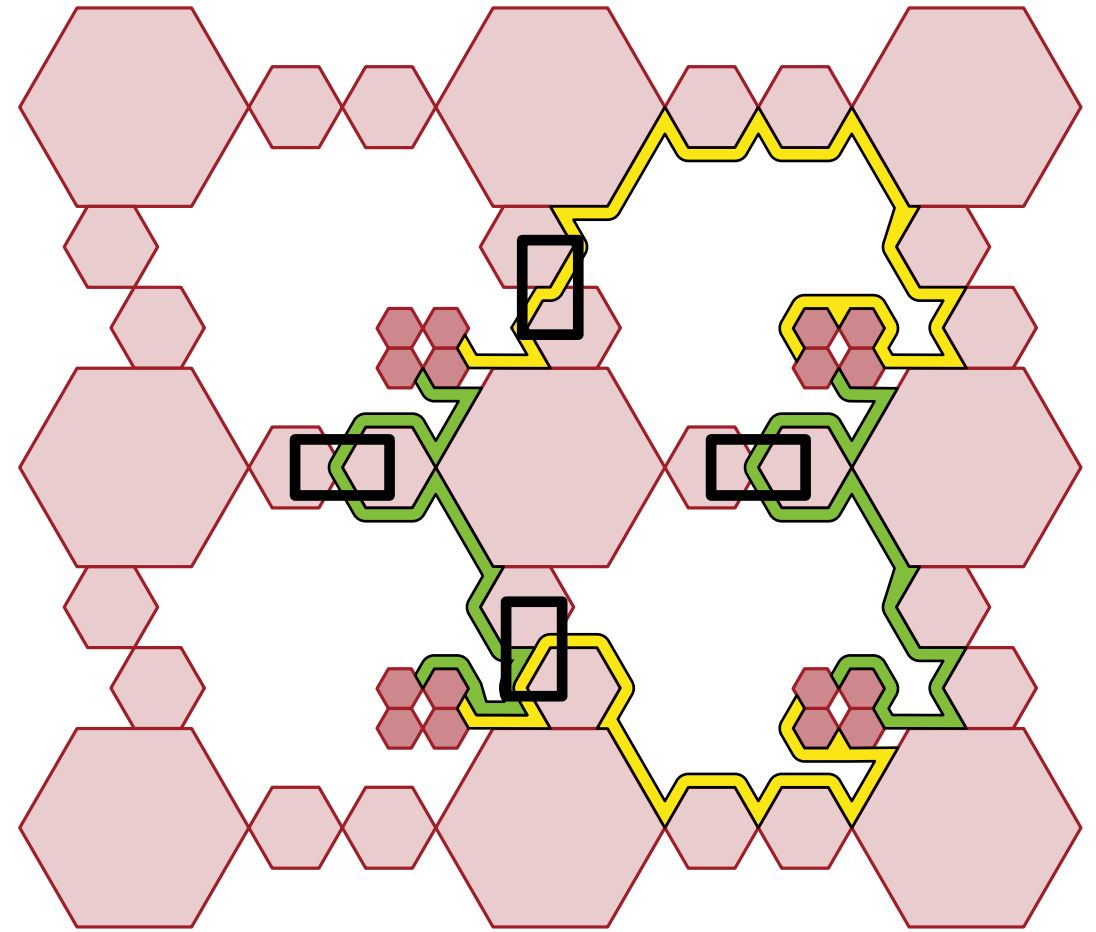
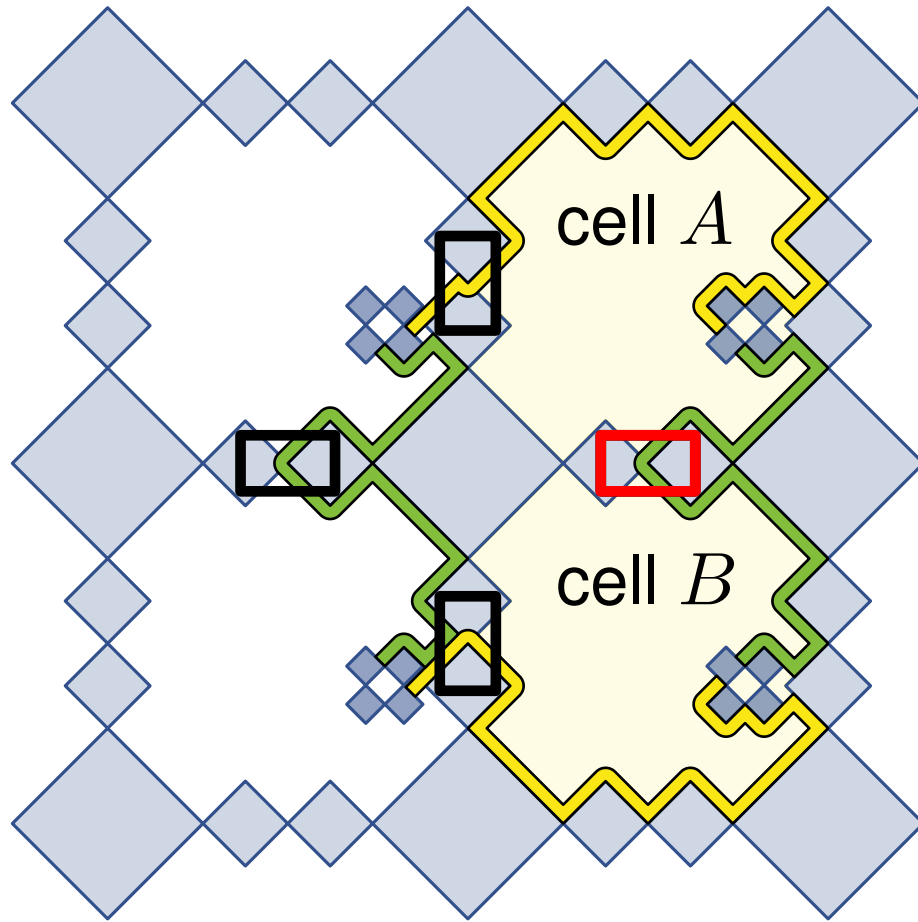
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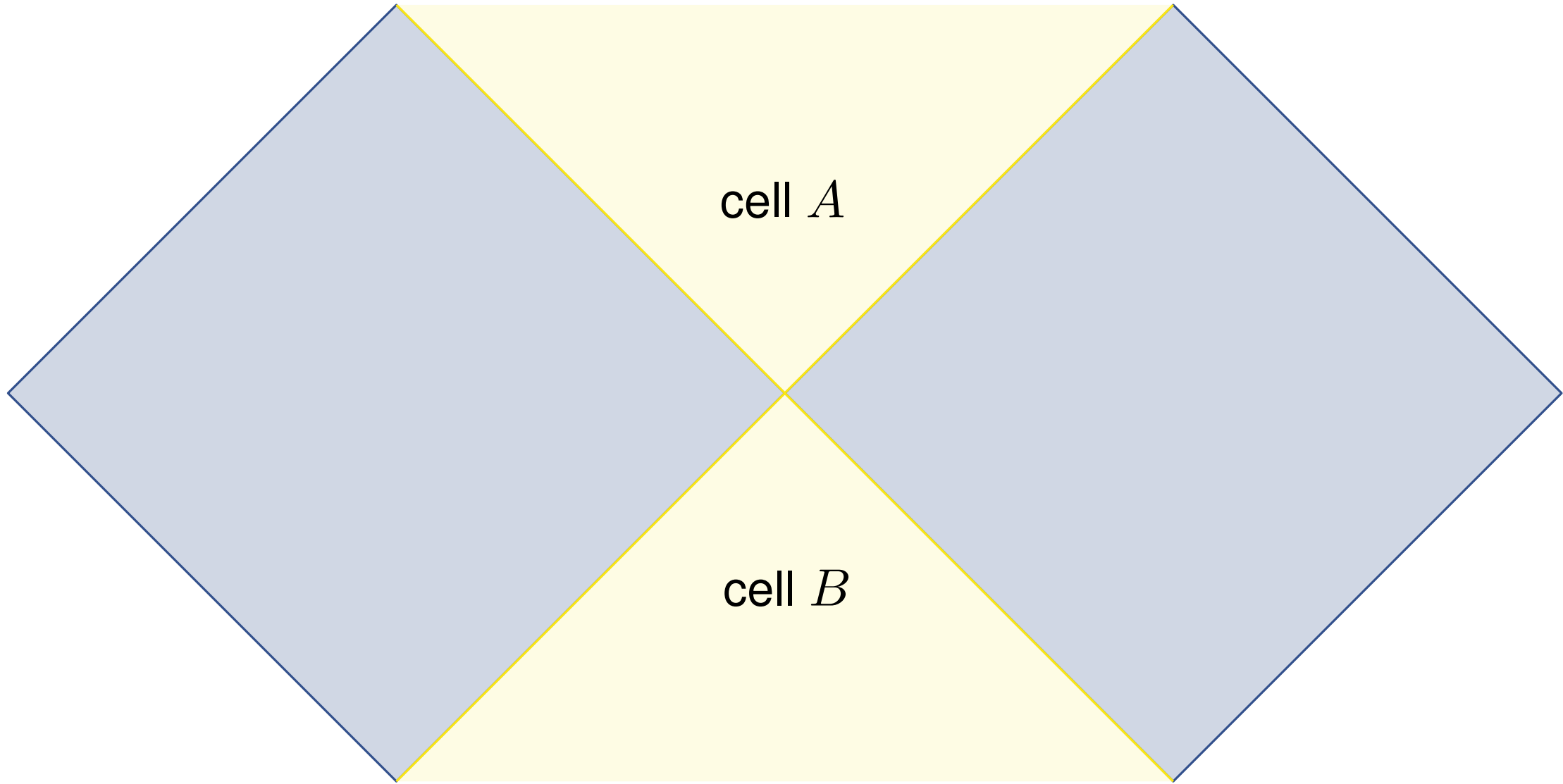
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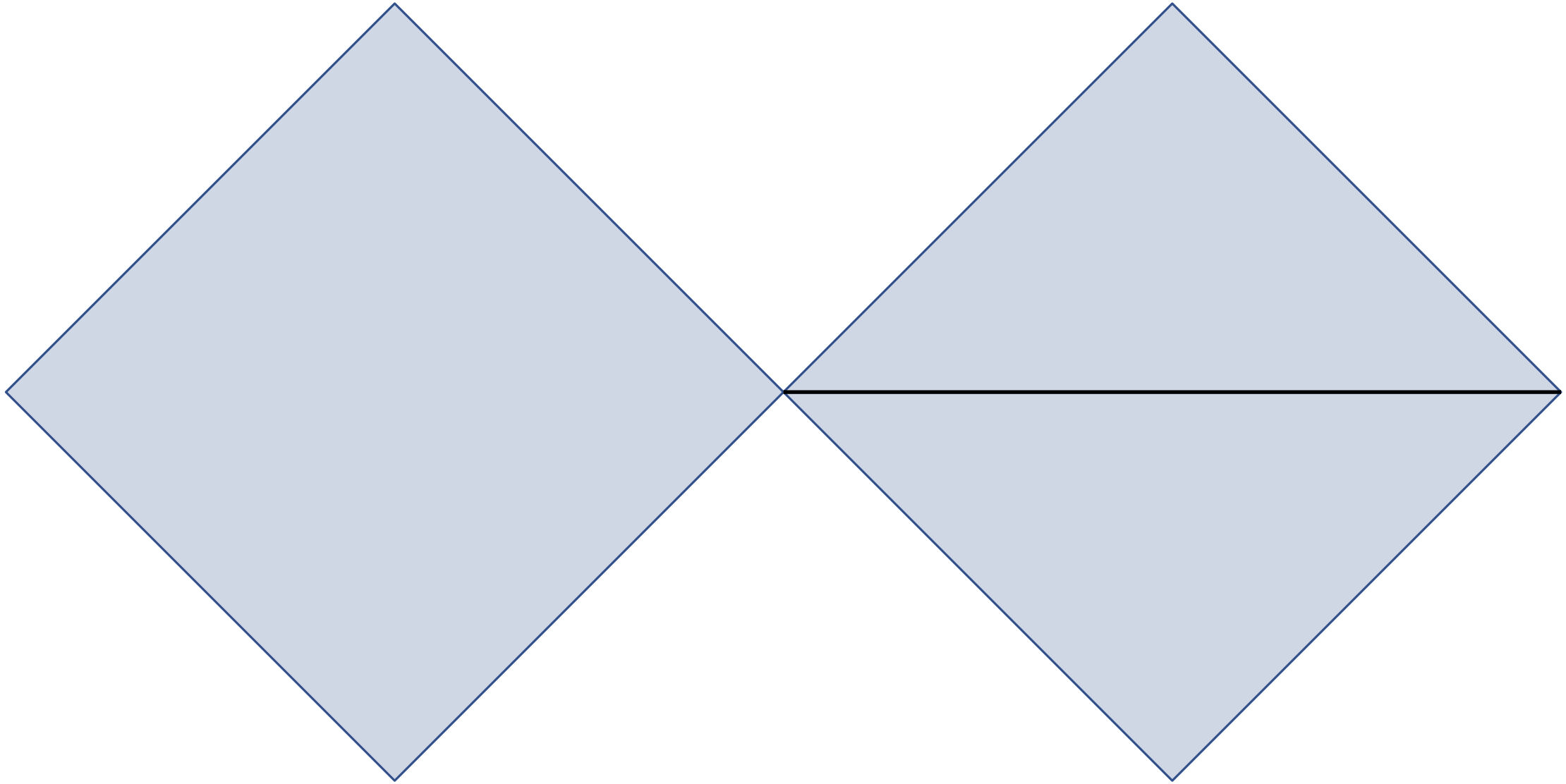
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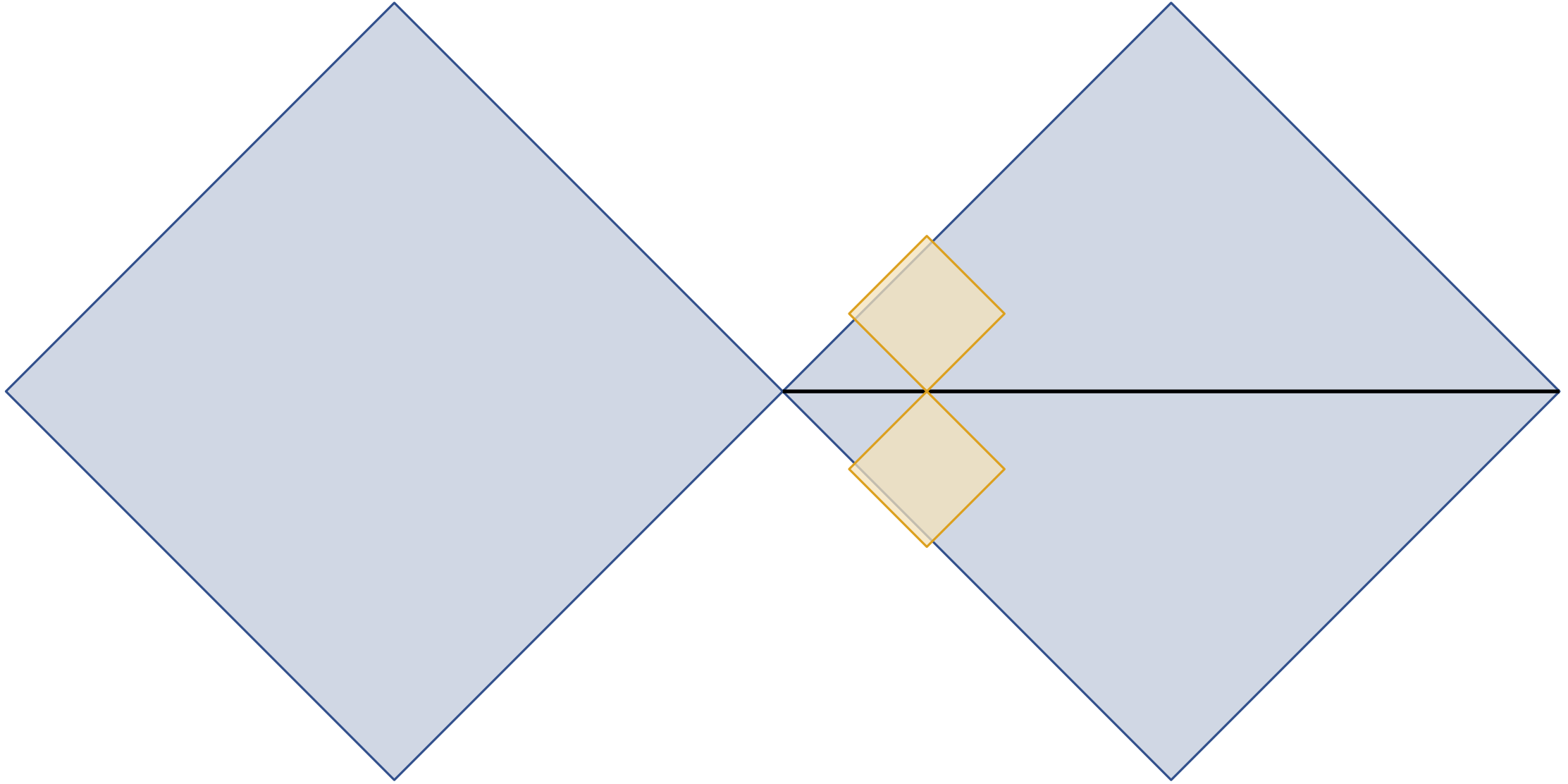
Independent Edges Between Cells: Rectangles



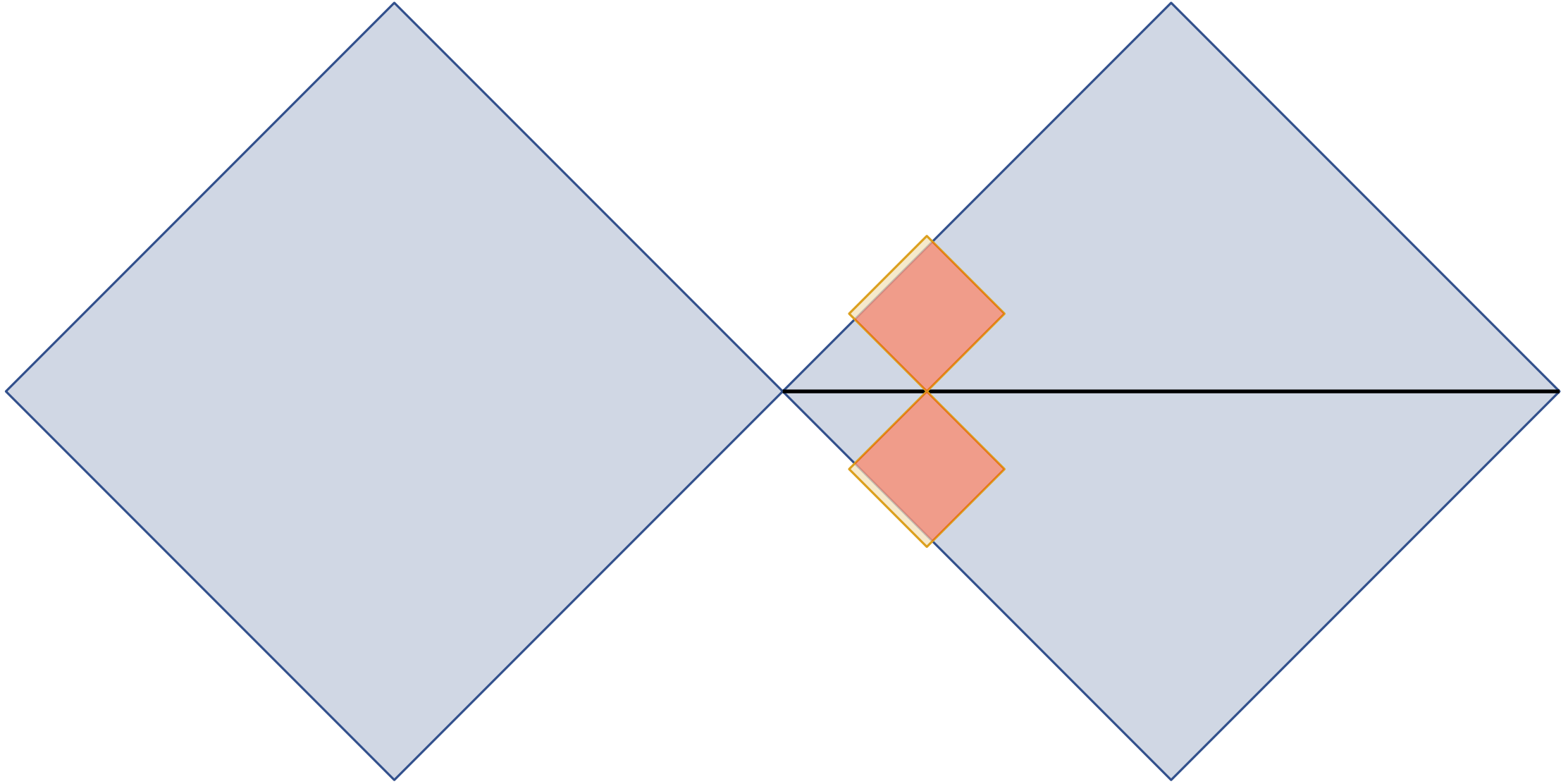
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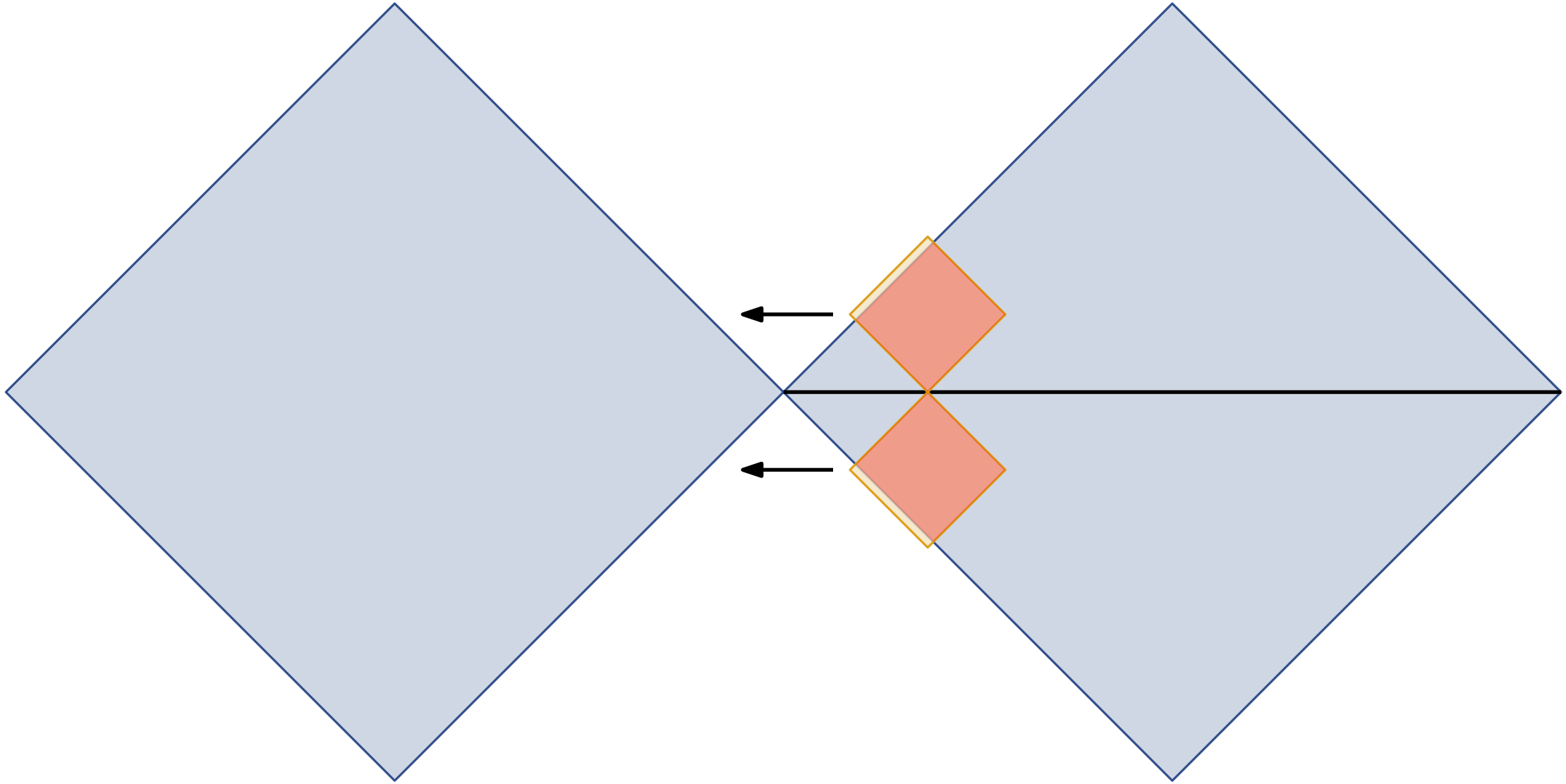
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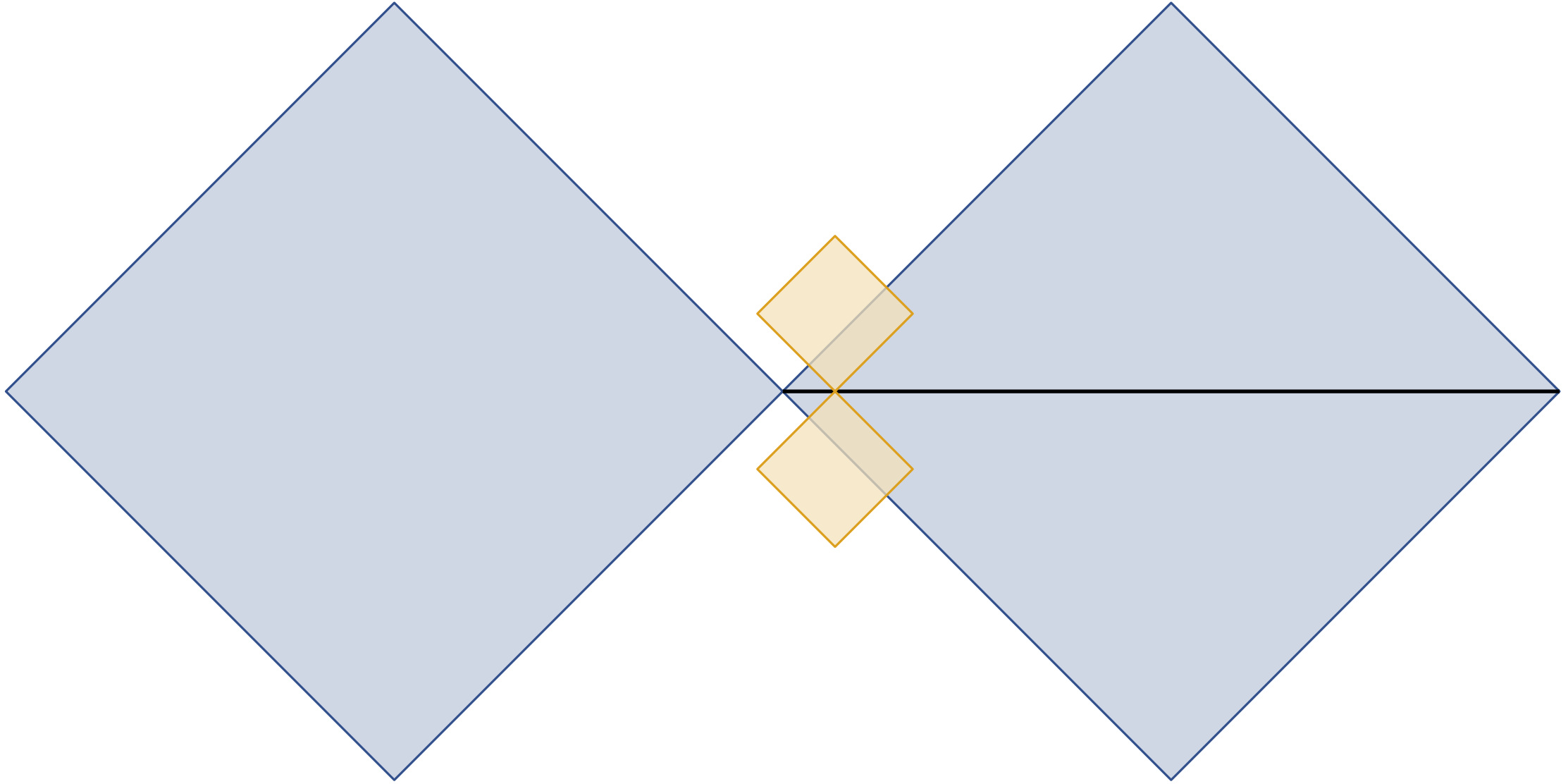
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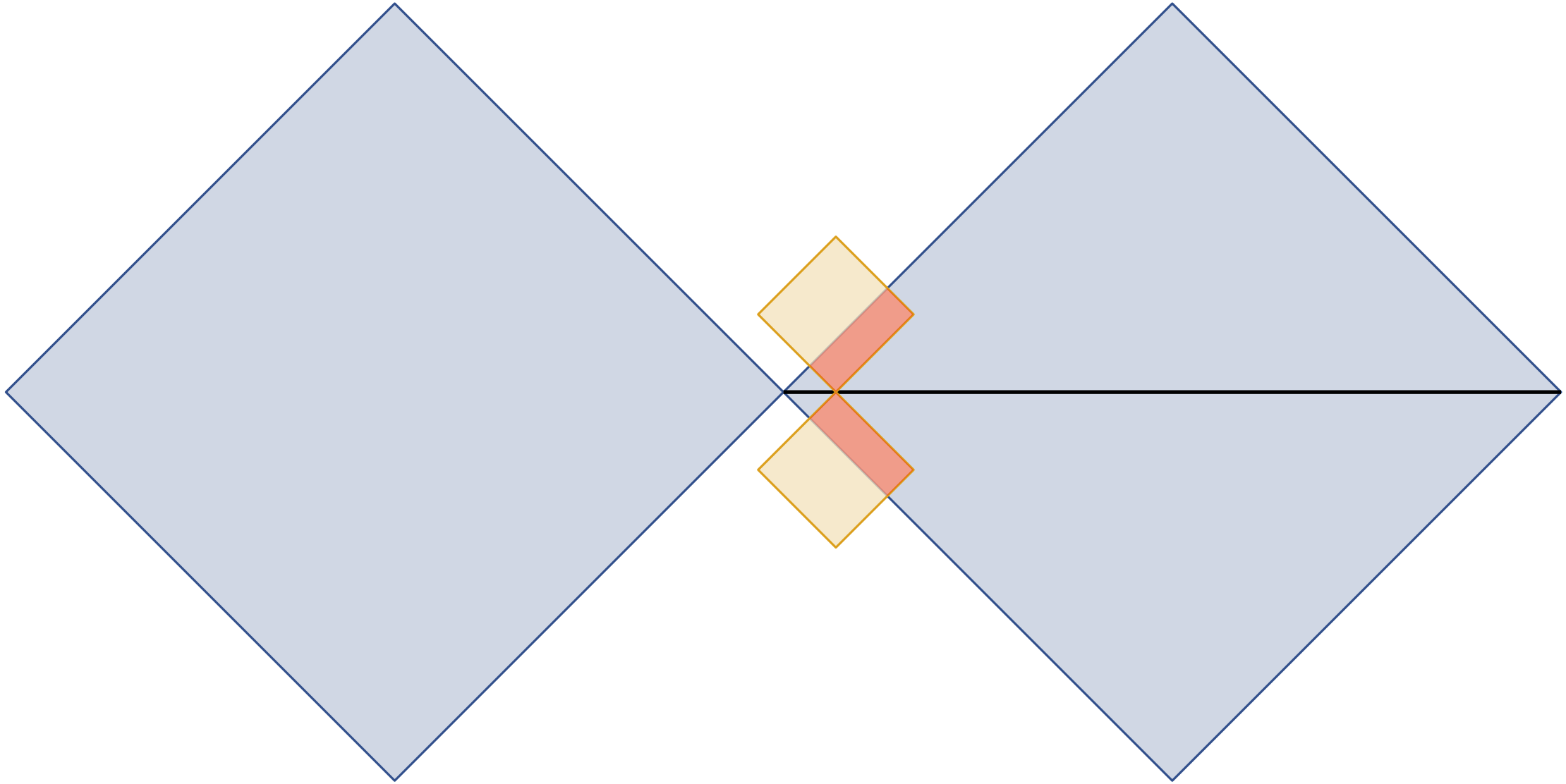
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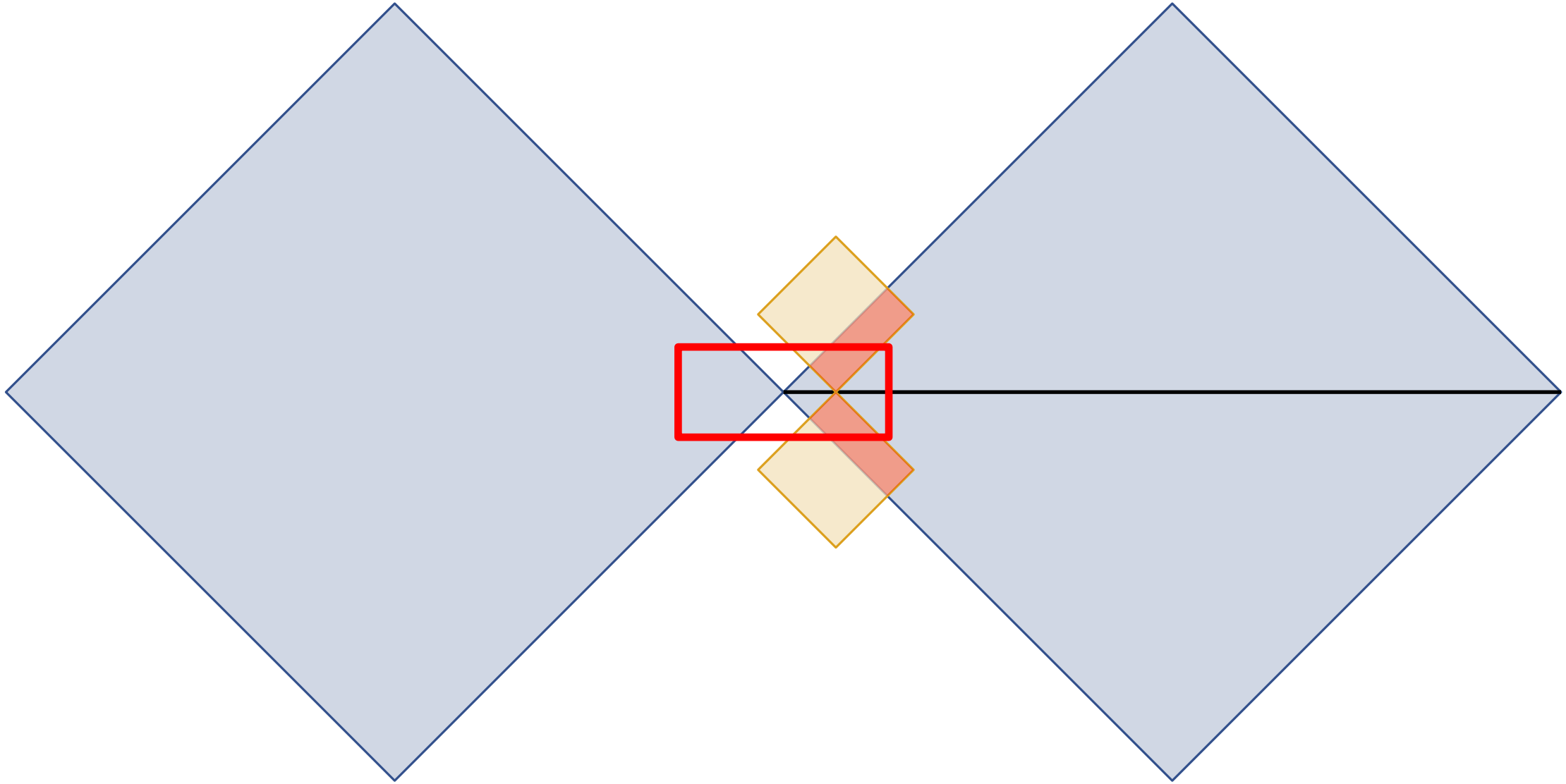
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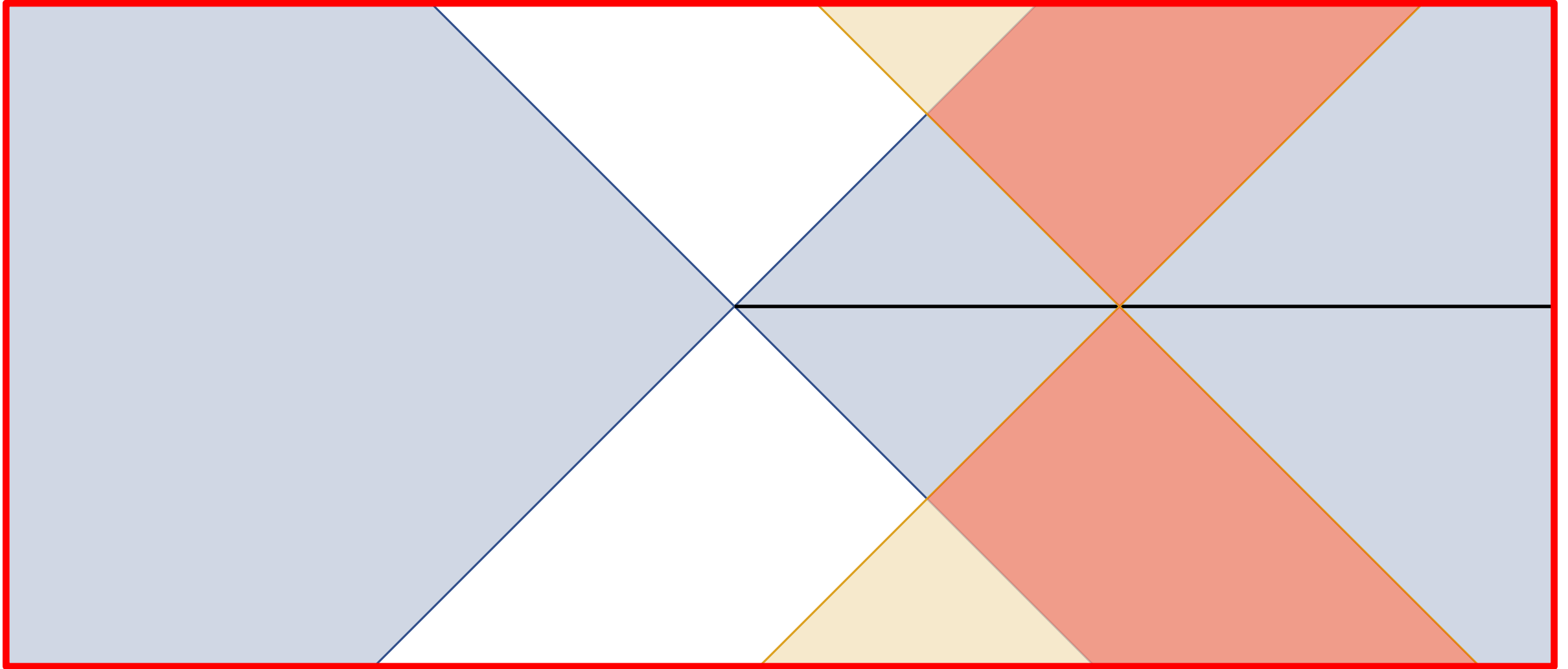
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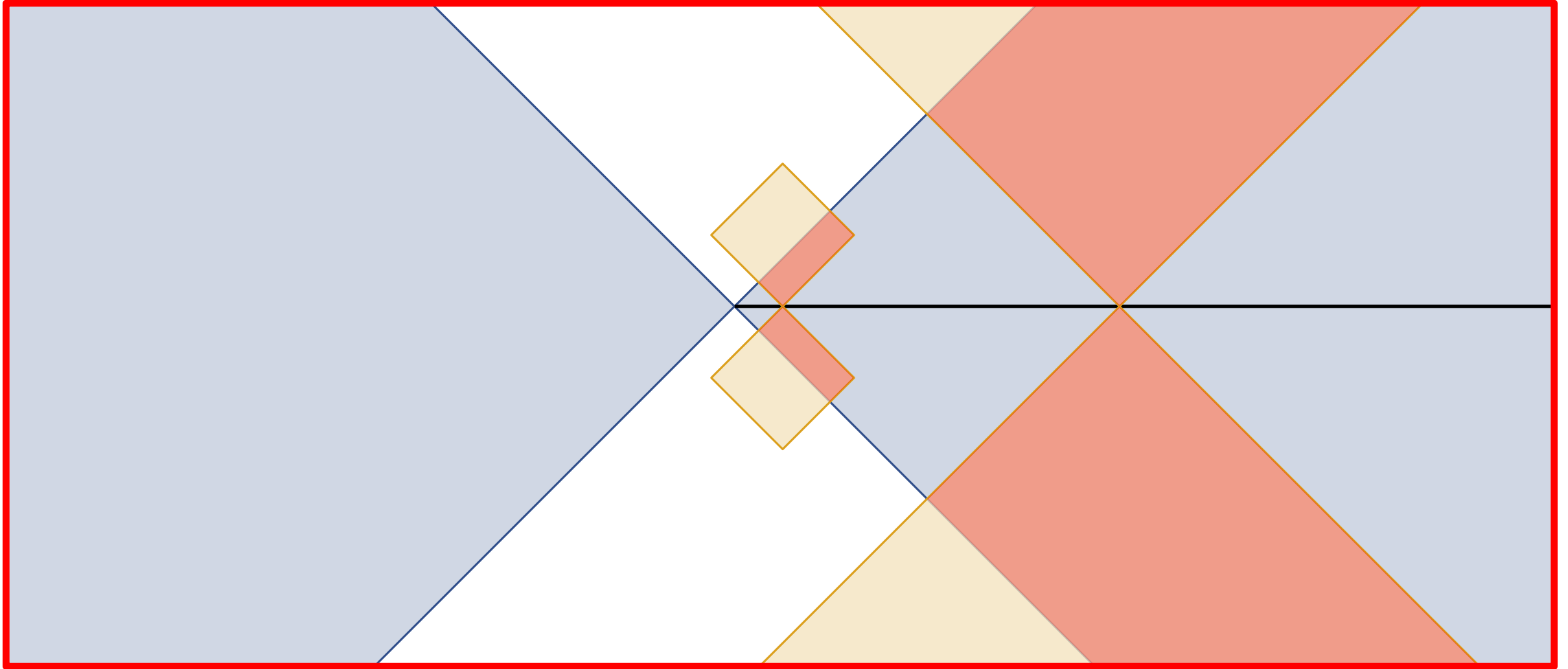
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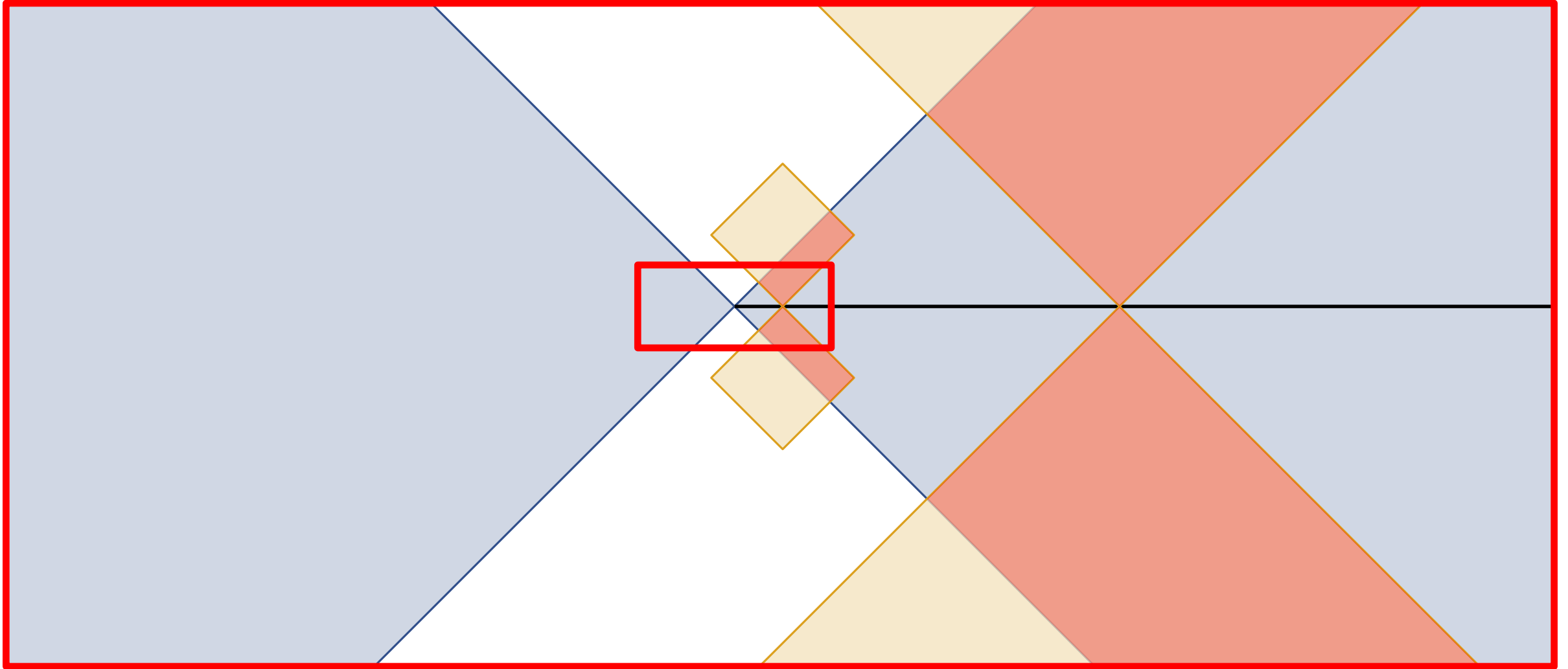
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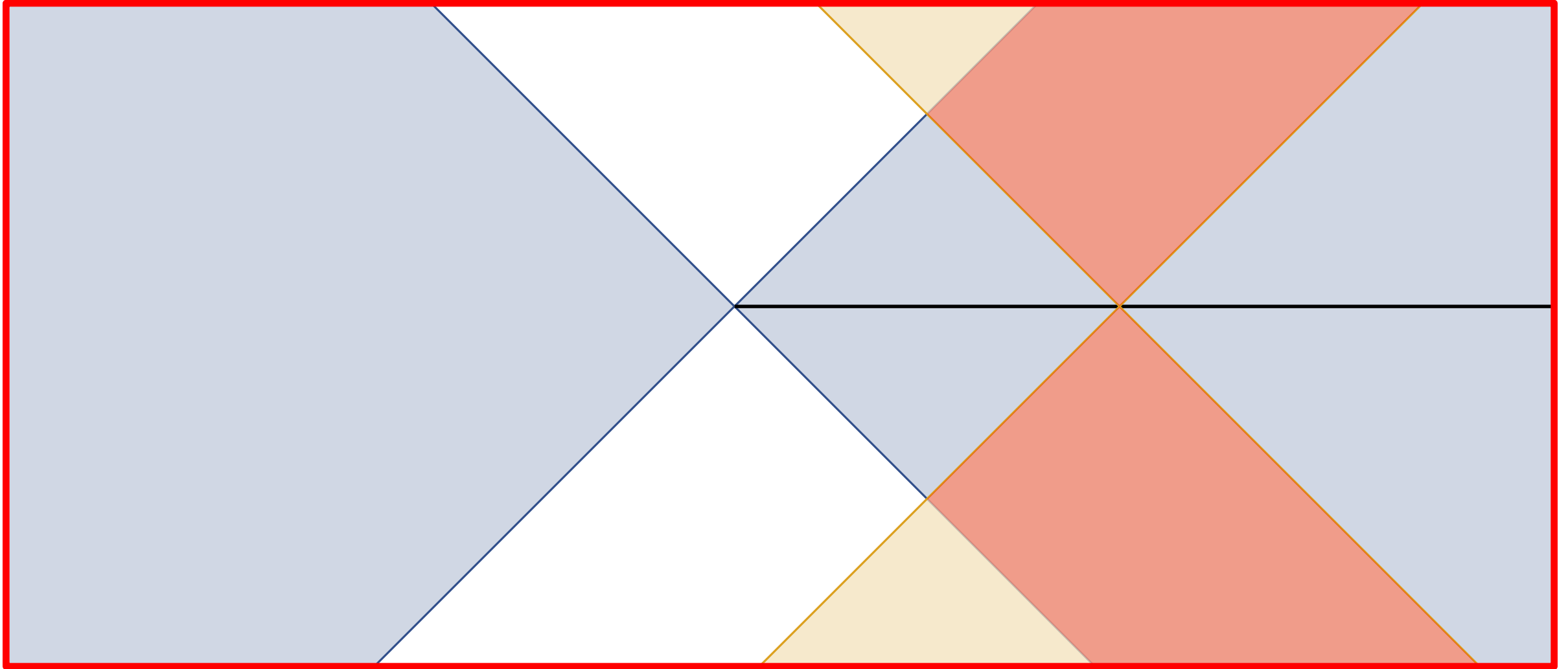
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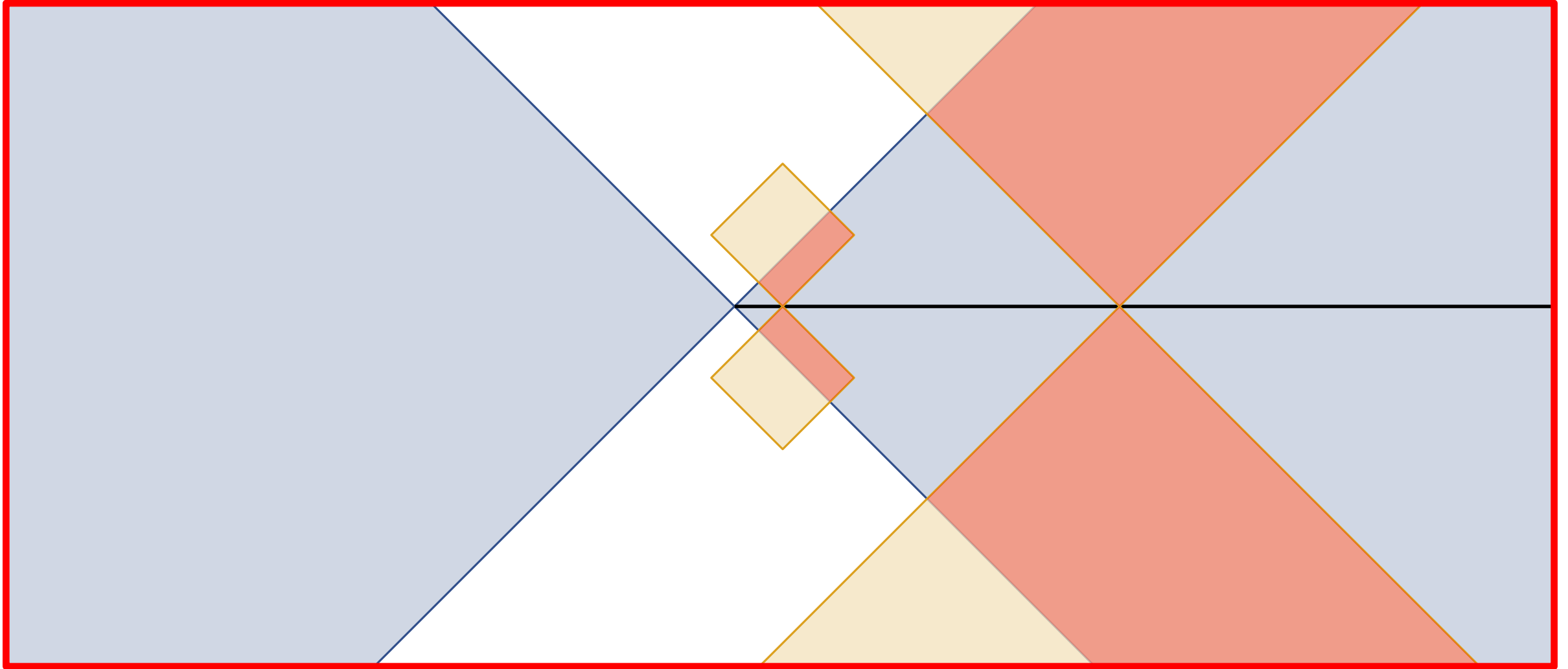
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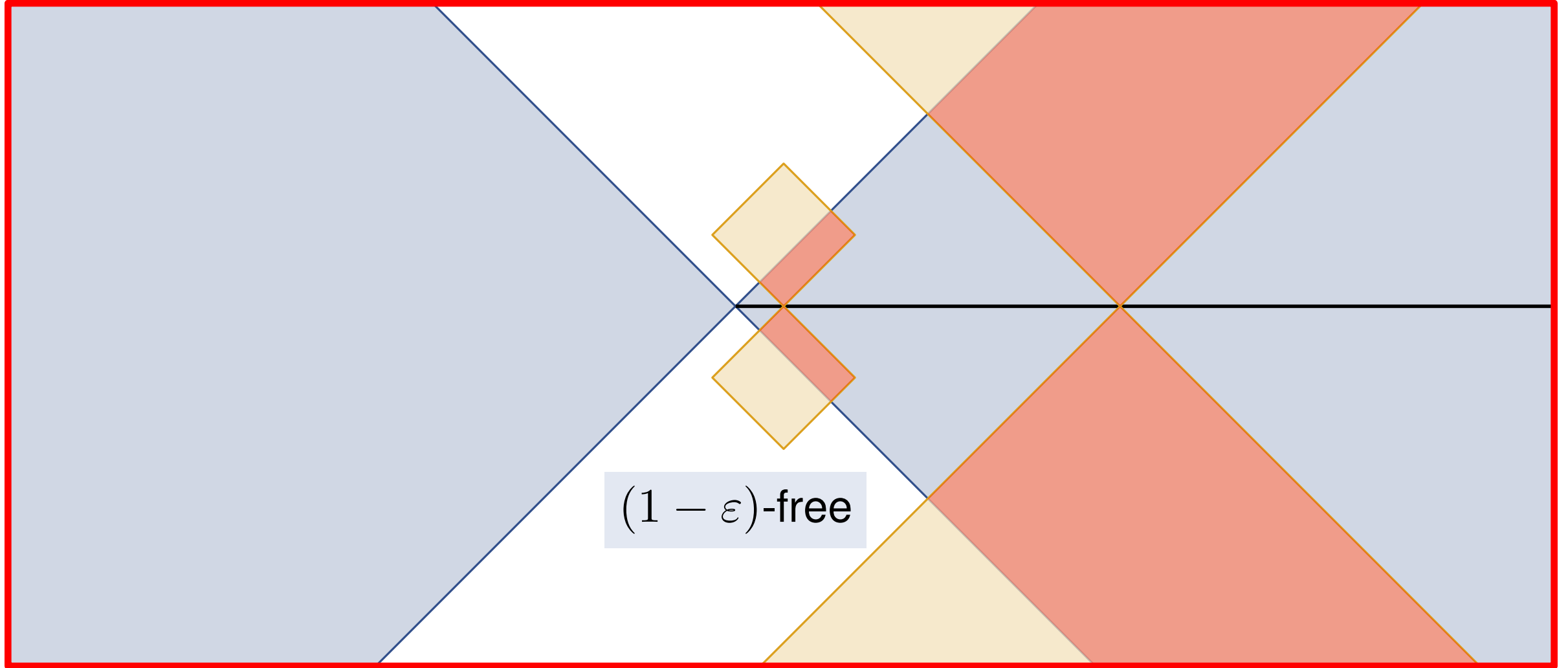
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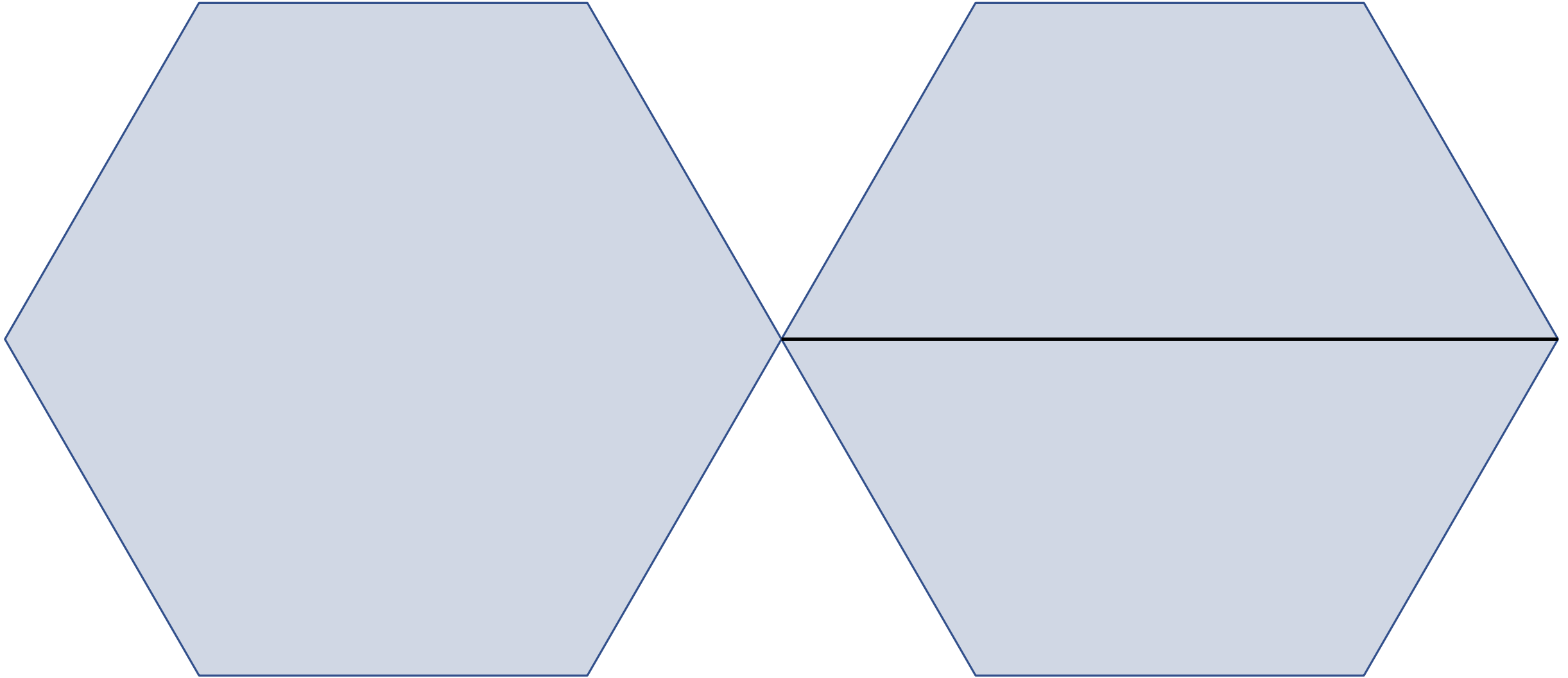
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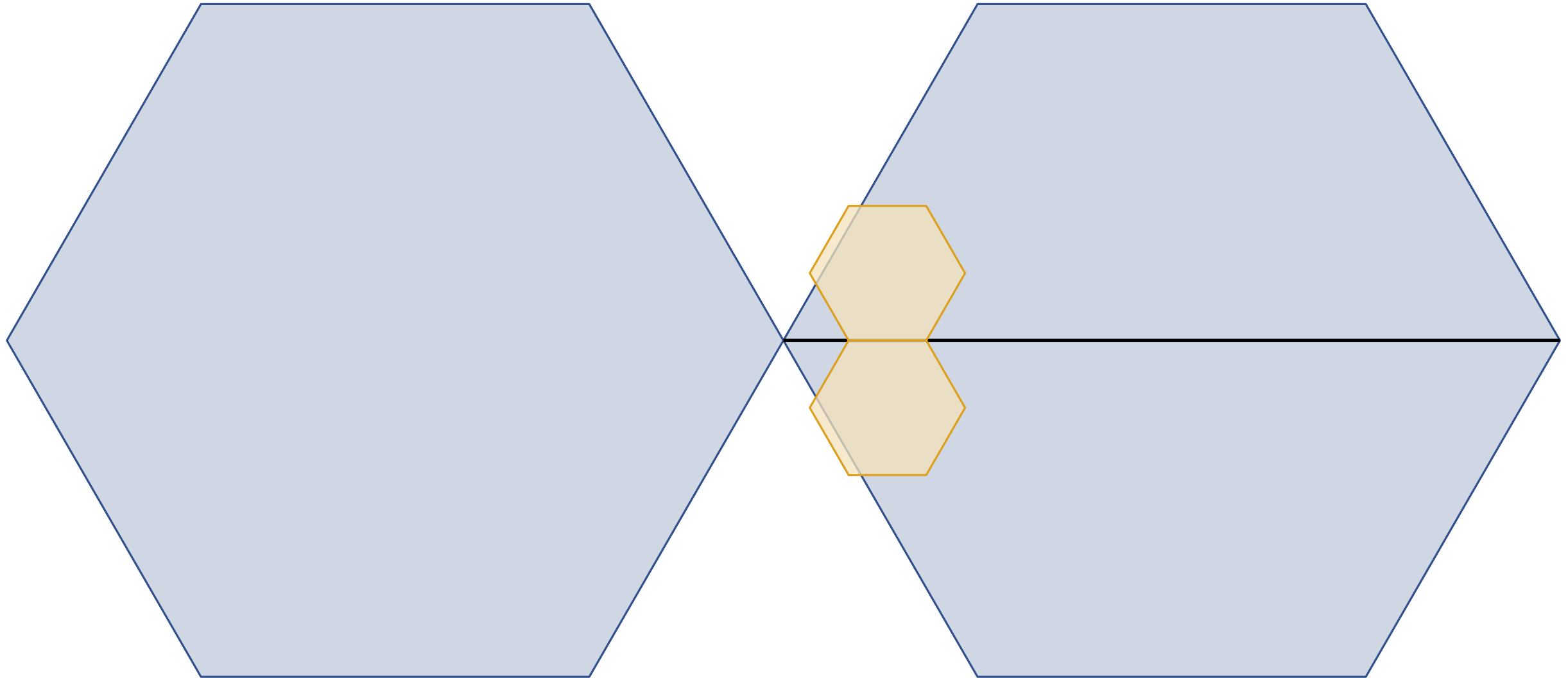
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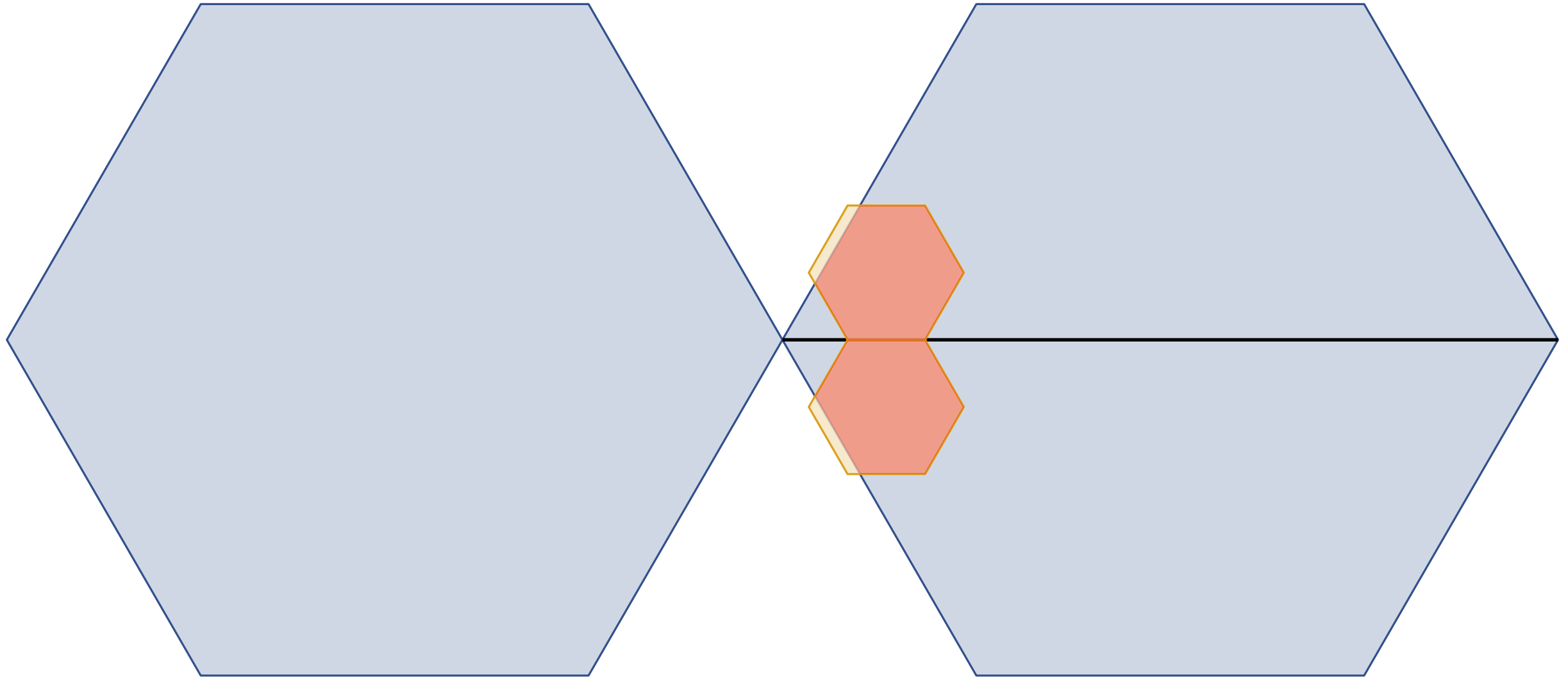
Independent Edges Between Cells: Hexagons



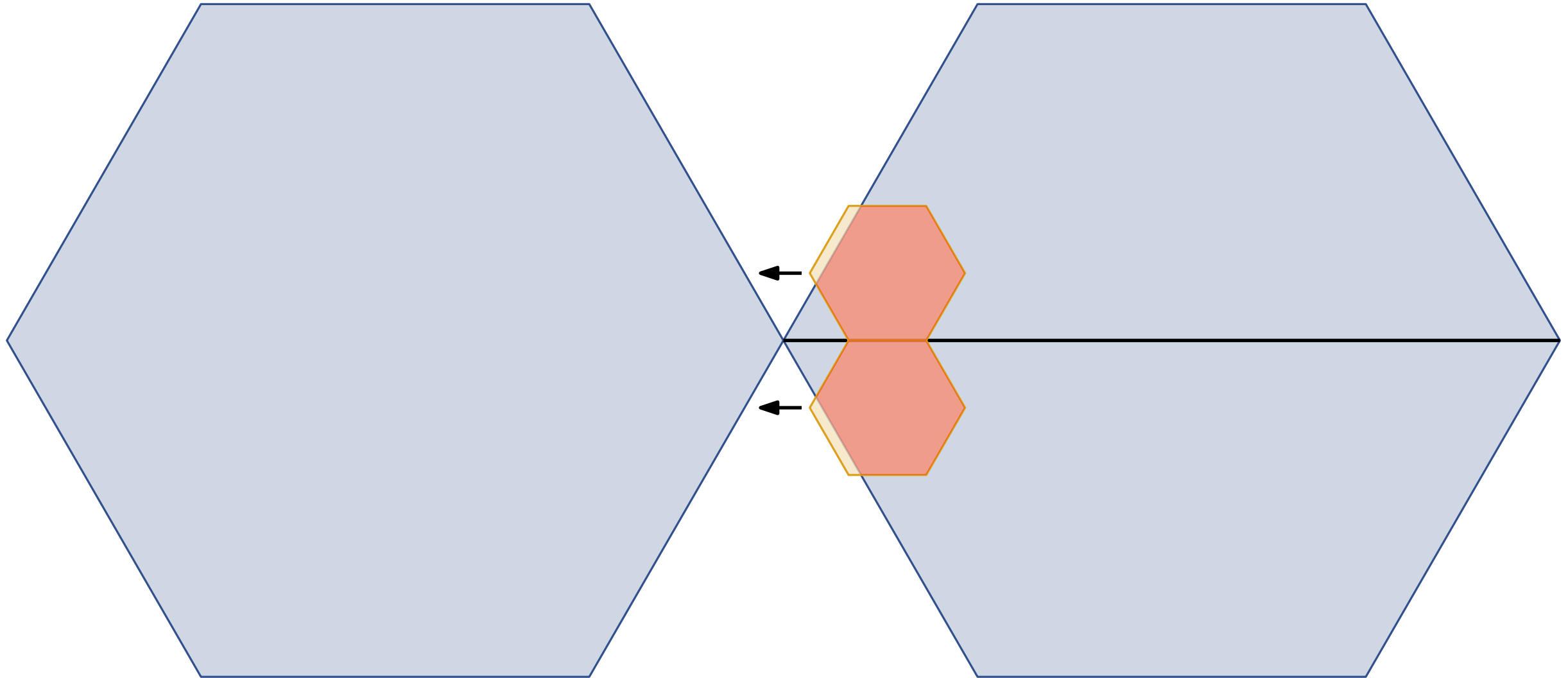
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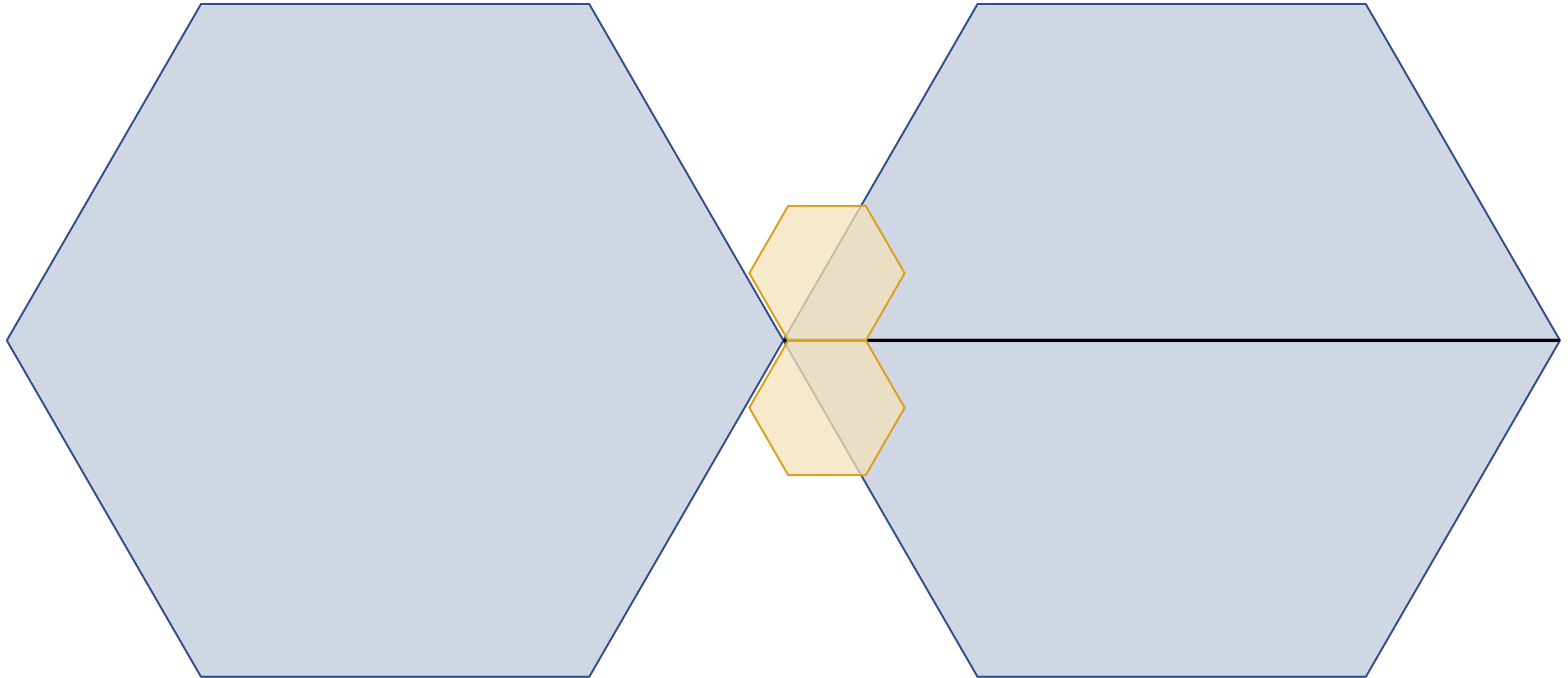
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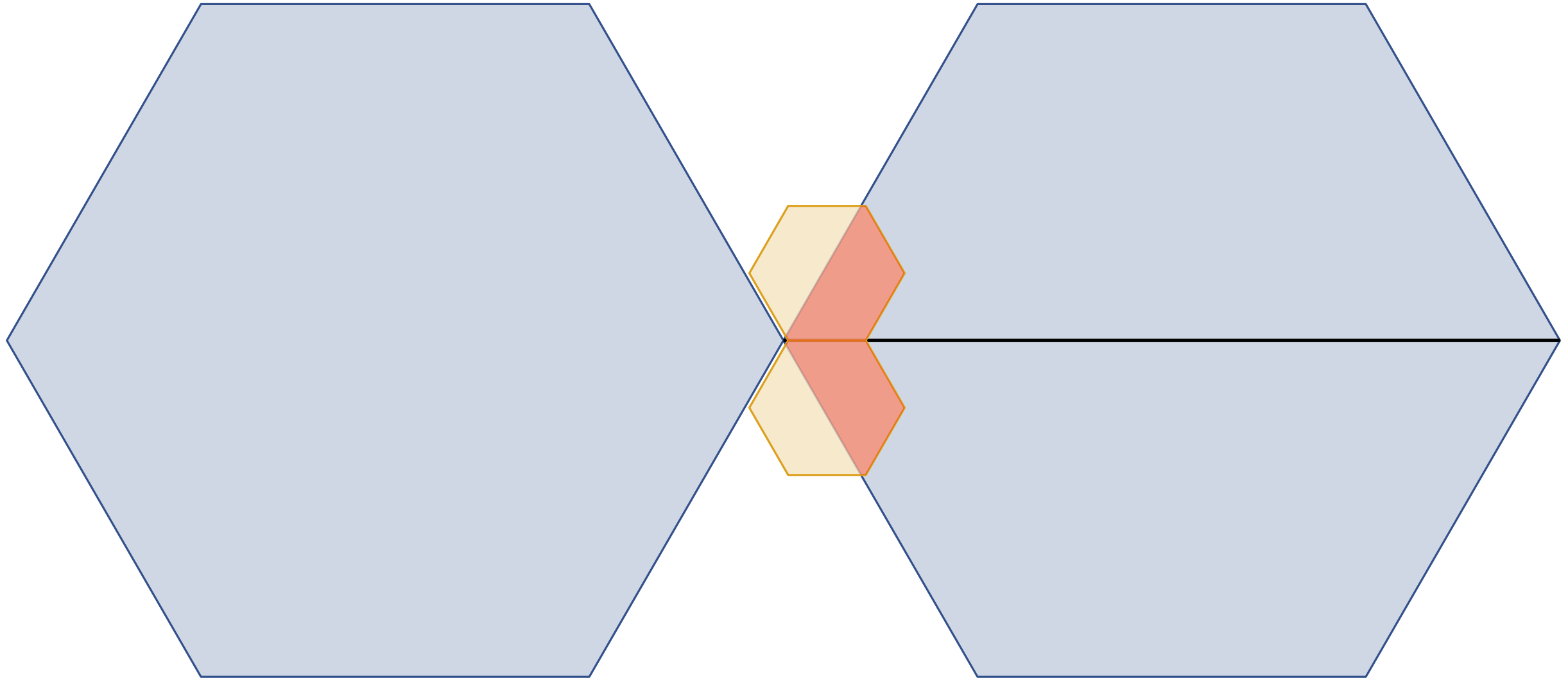
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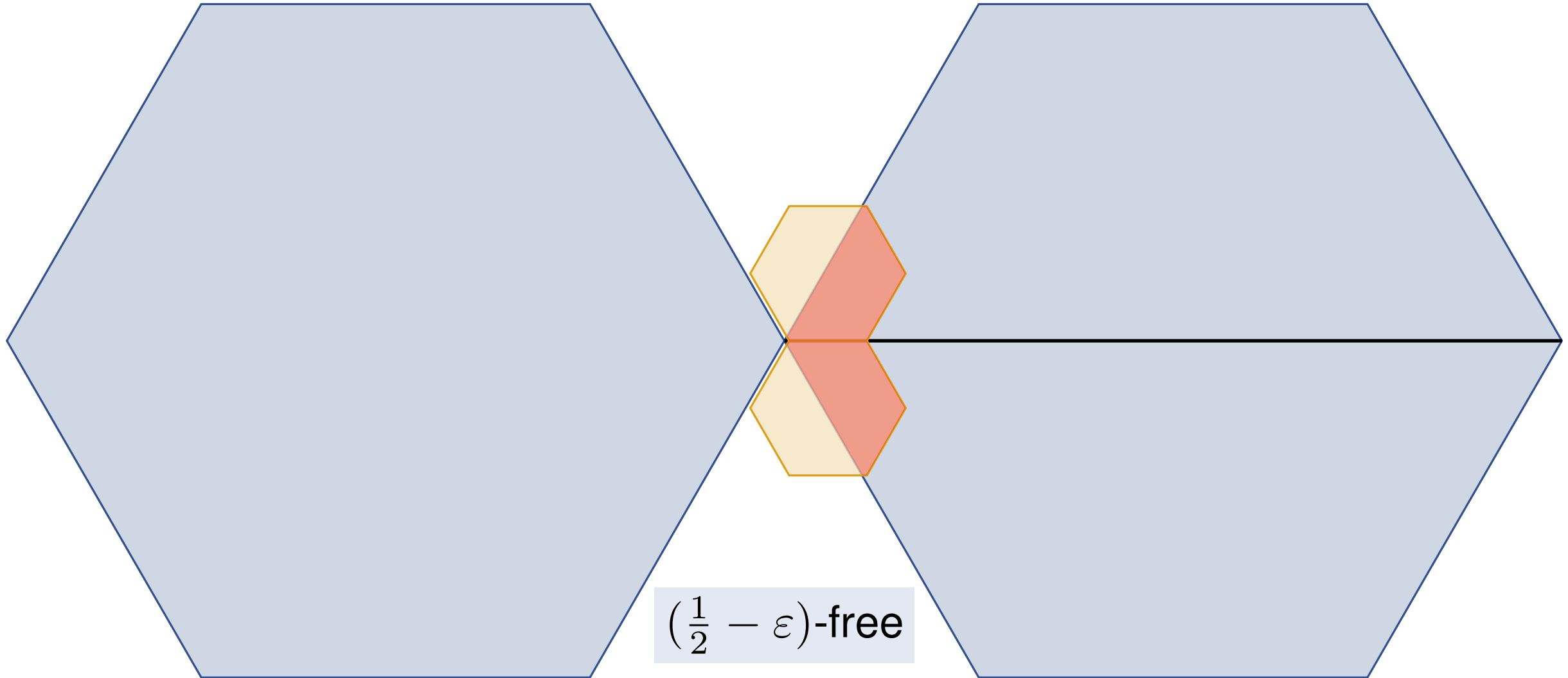
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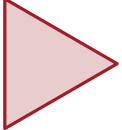


Independent Edges Between Cells: Hexagons



$(\frac{1}{2} - \varepsilon)$ -free

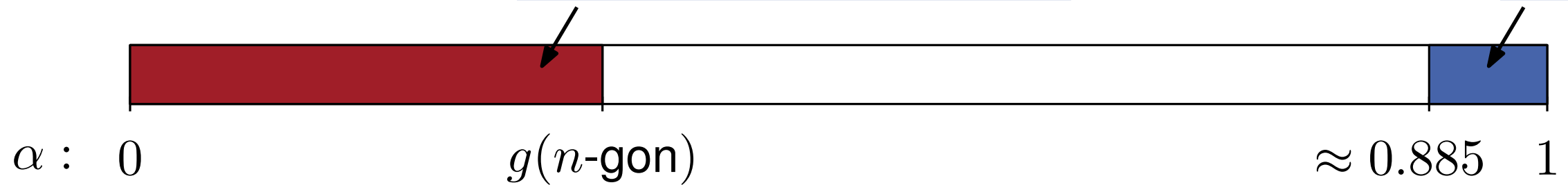
Our Results for Regular n -gons

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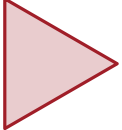
■ For even $n \geq 6$:

no linear local treewidth

planar



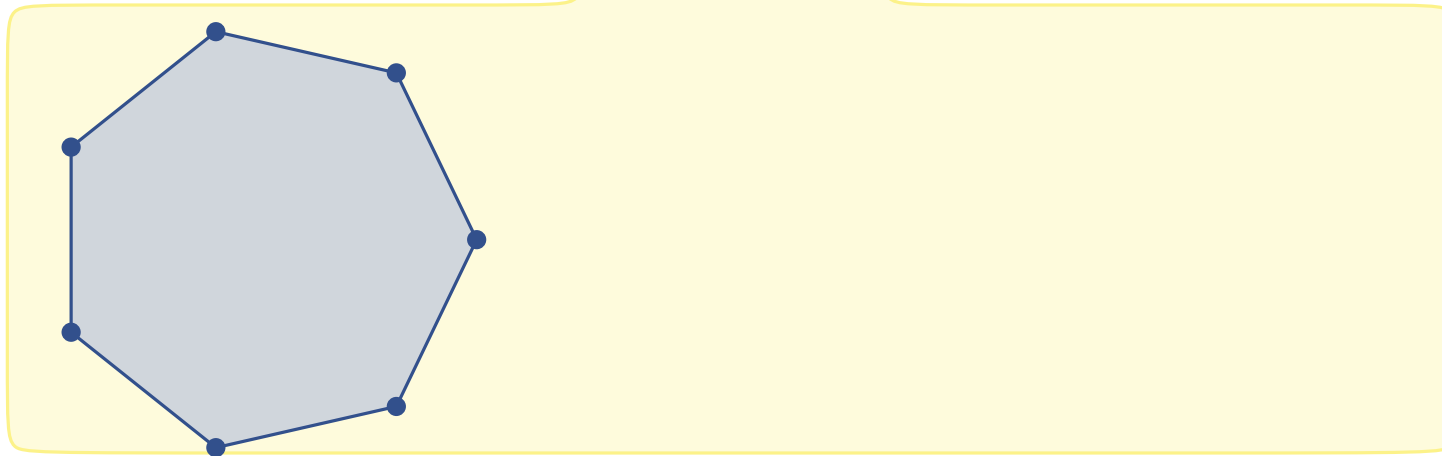
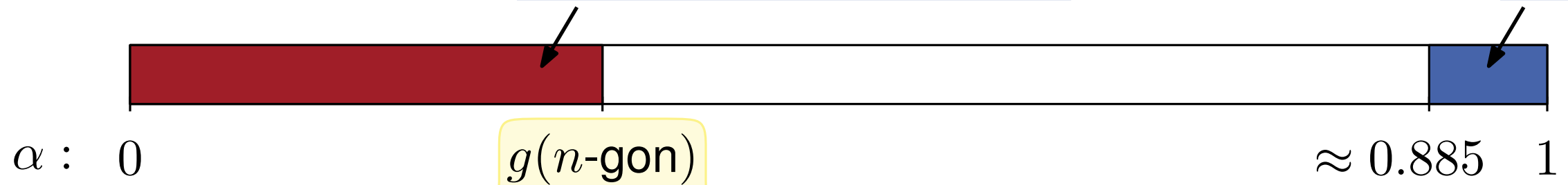
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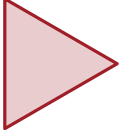
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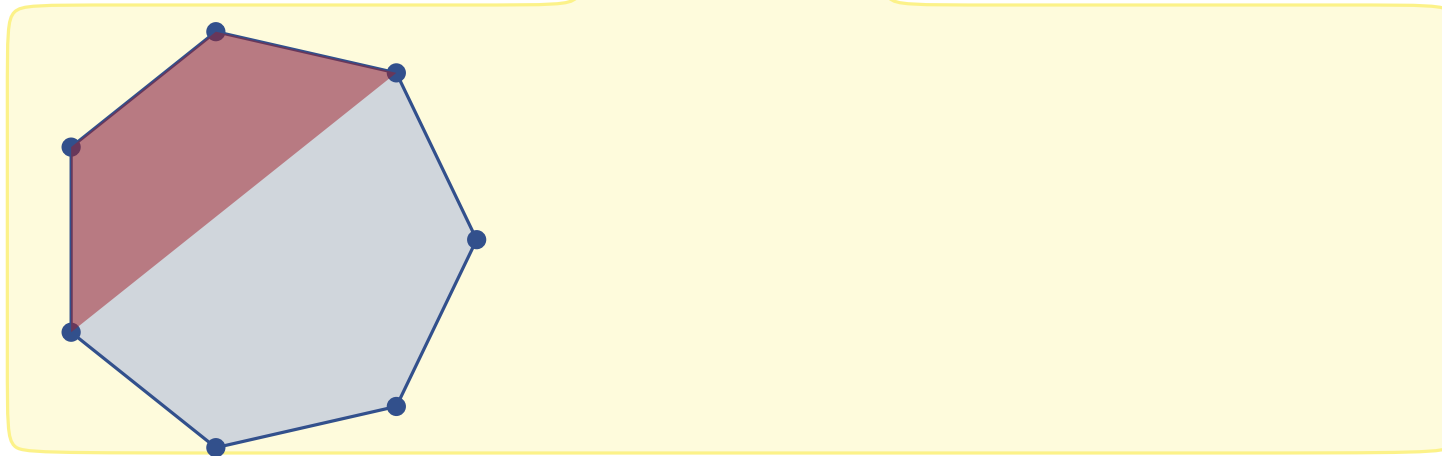
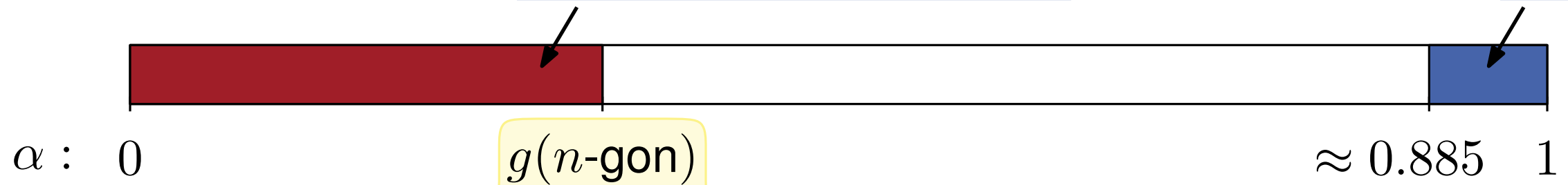
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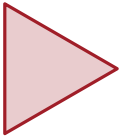
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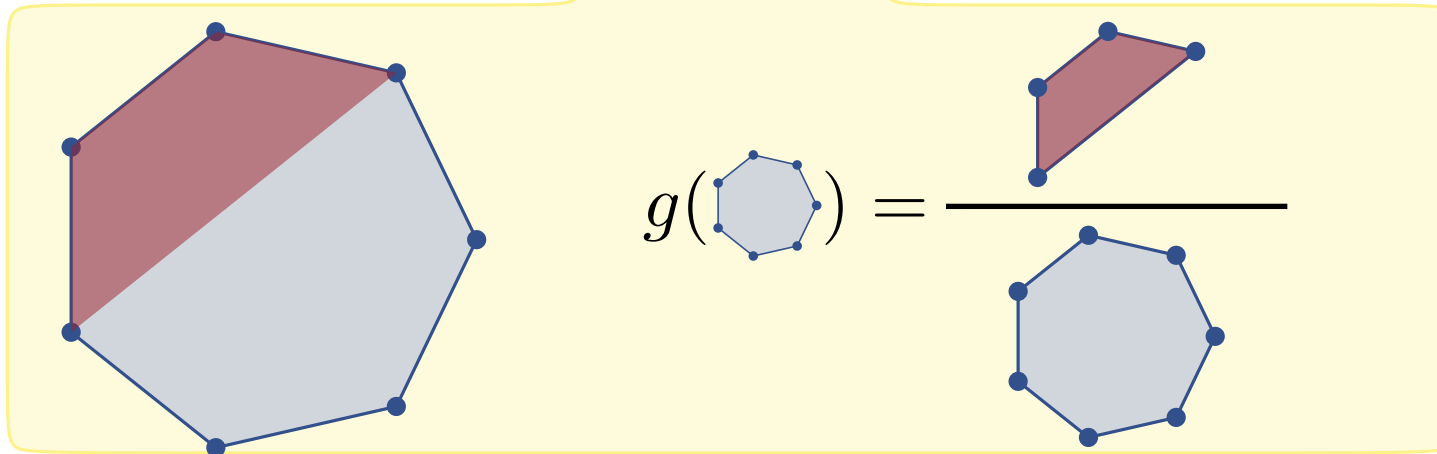
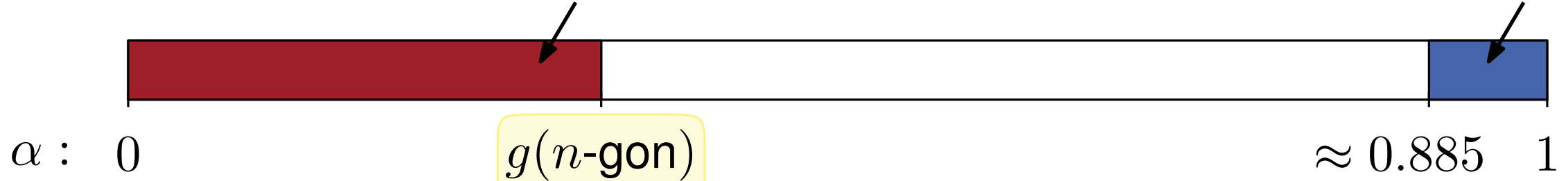
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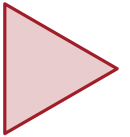
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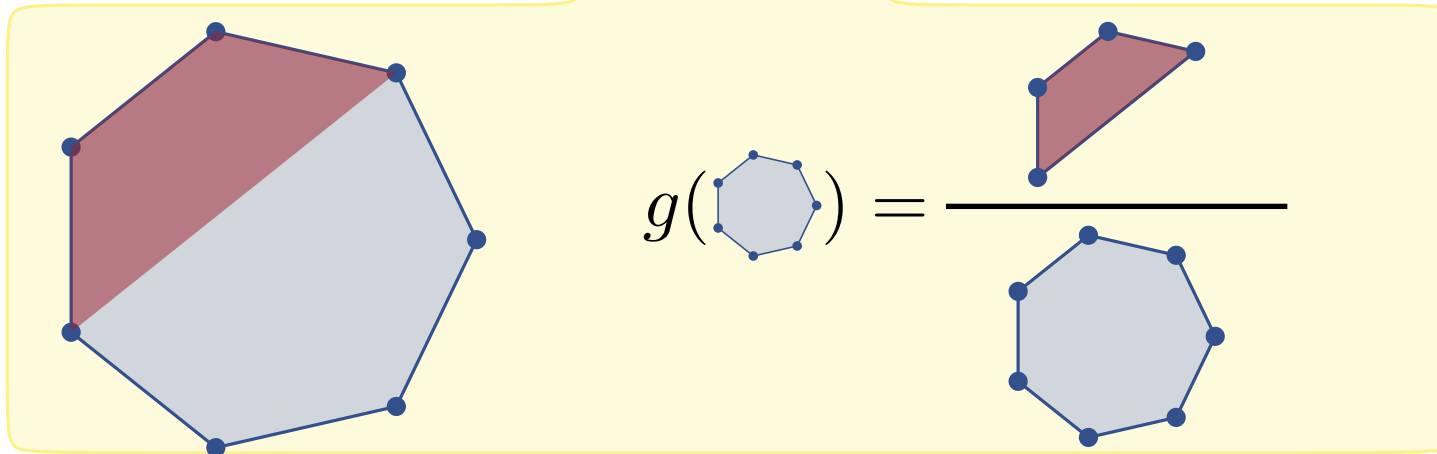
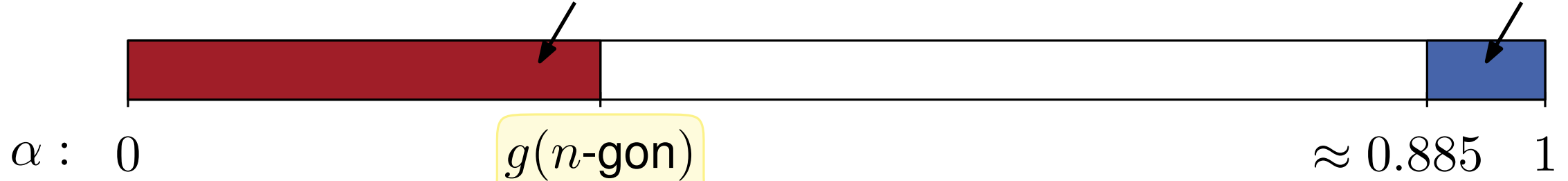
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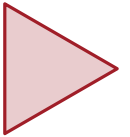
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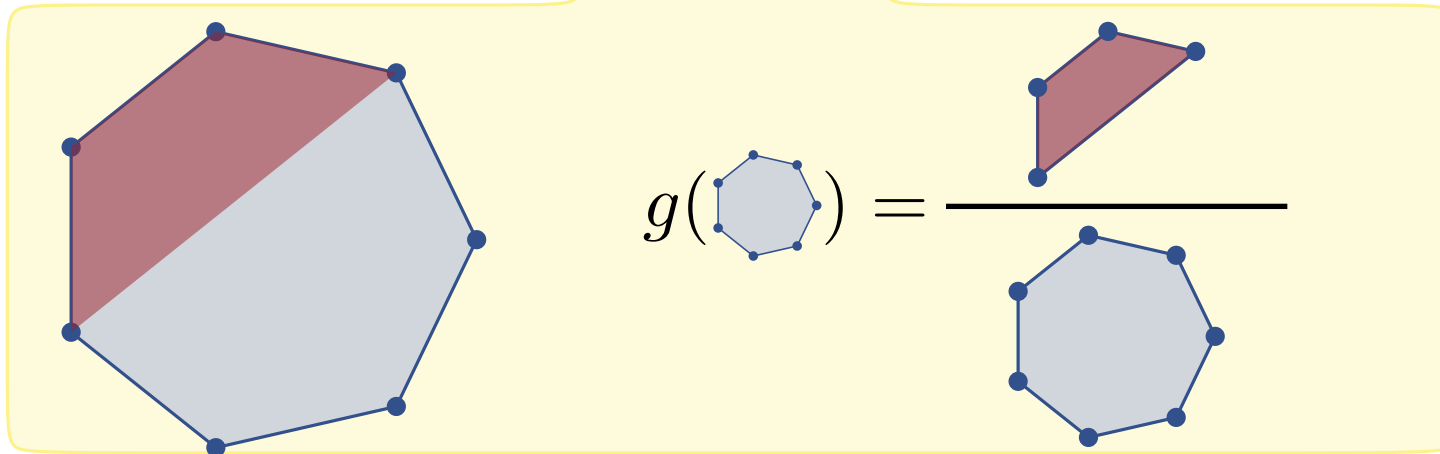
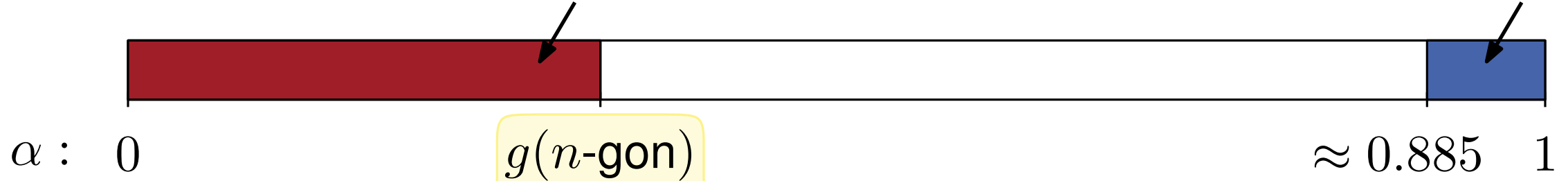
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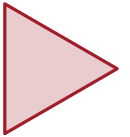
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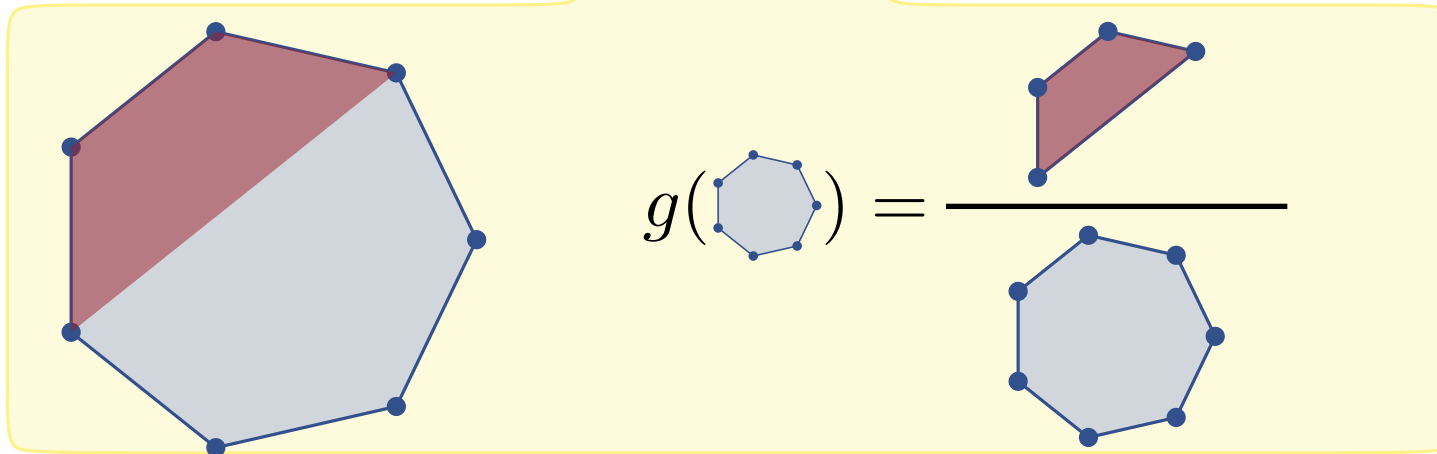
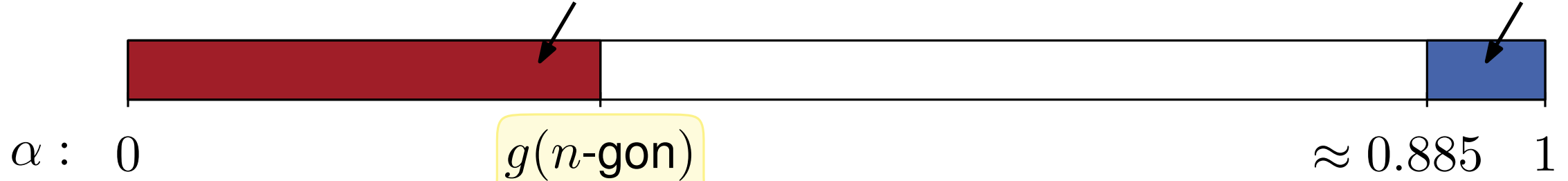
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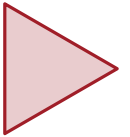


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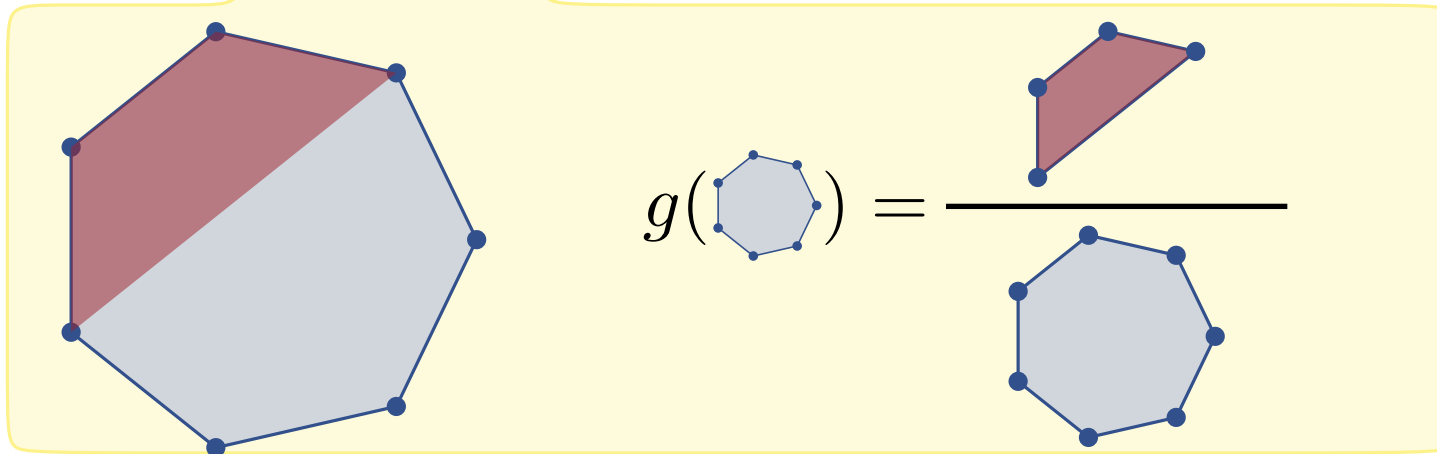
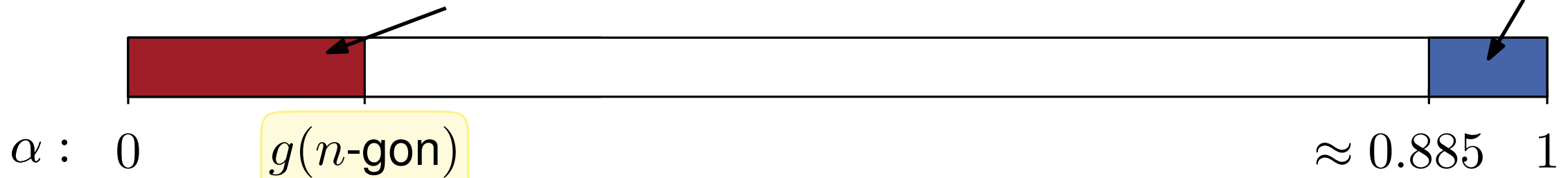
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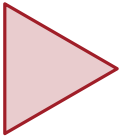


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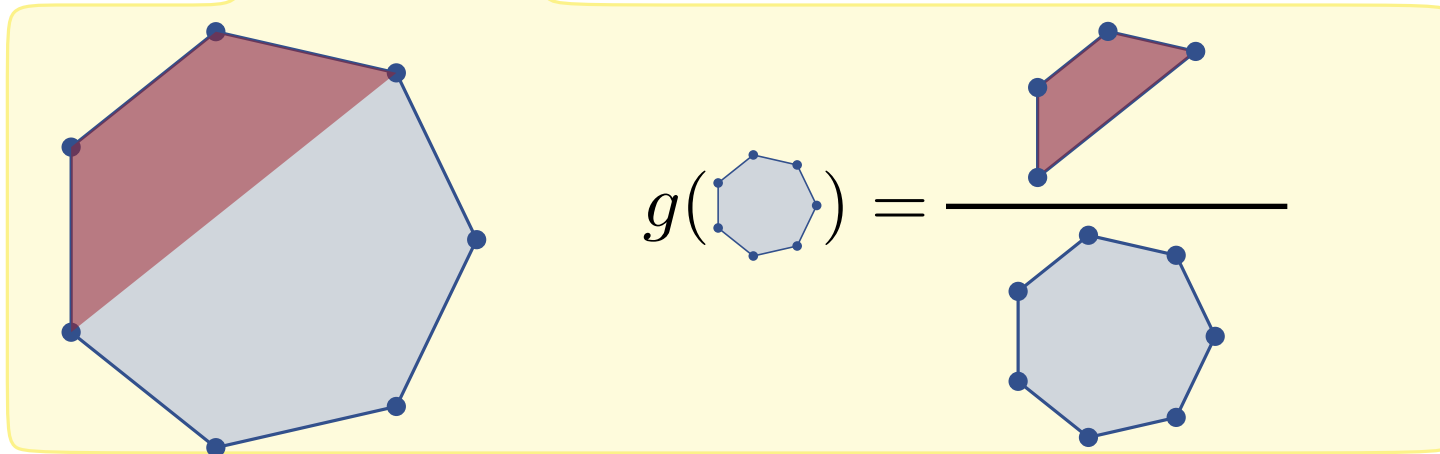
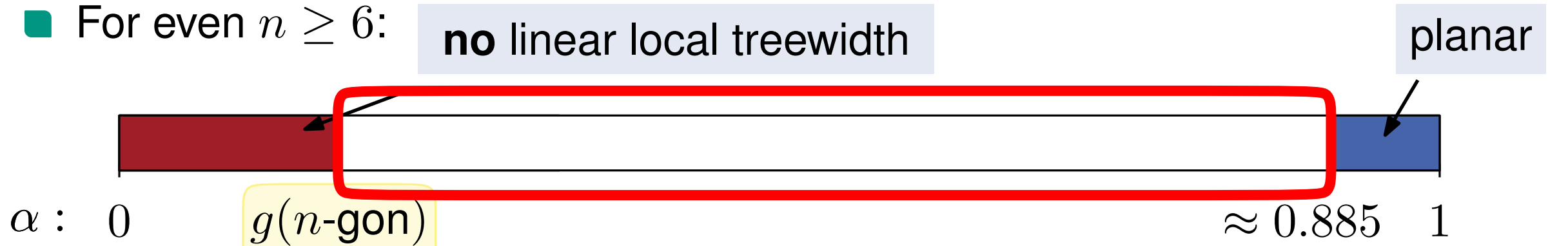
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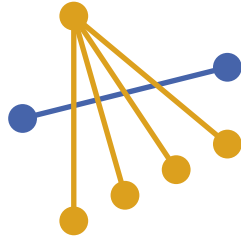
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k -Independent Crossing Drawings

k -independent crossing: no edge is crossed by more than k independent edges.

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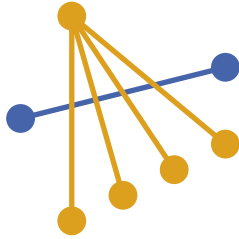
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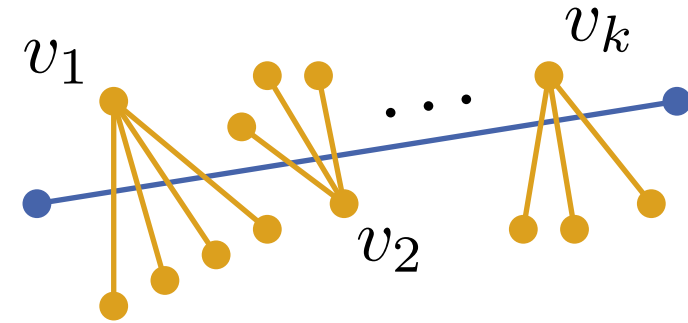
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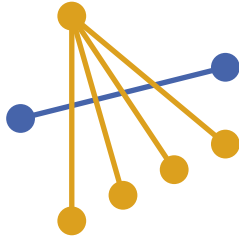
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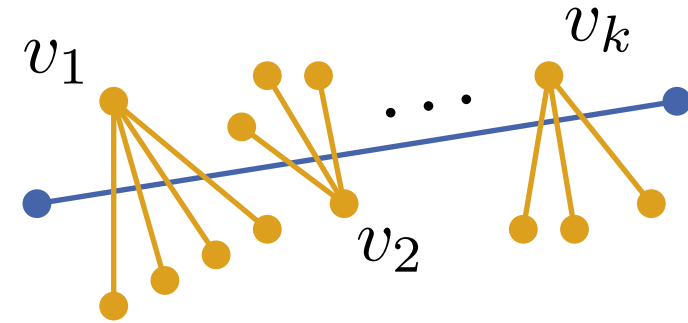
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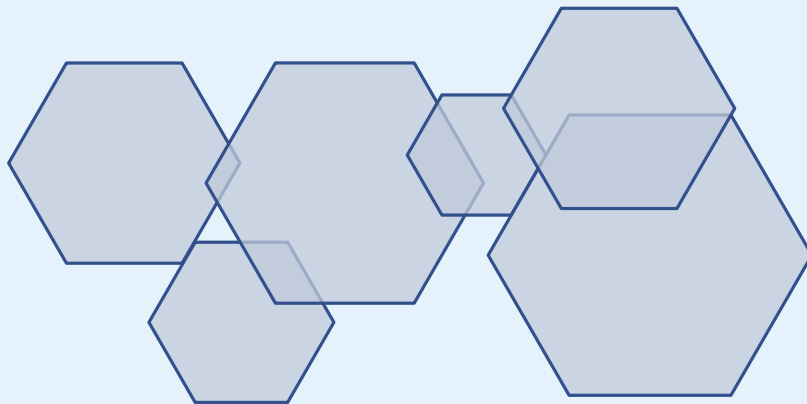


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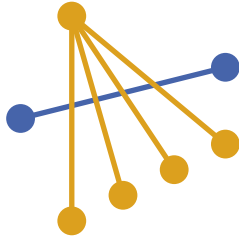
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canonical drawings

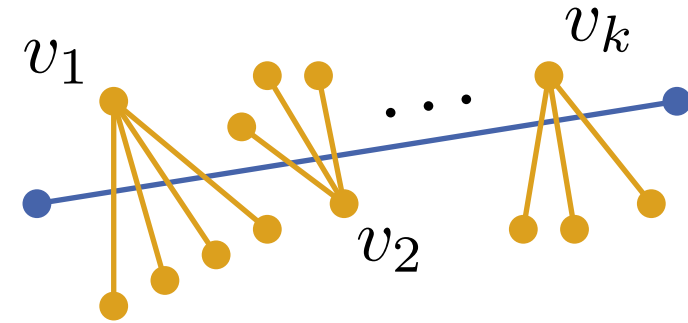


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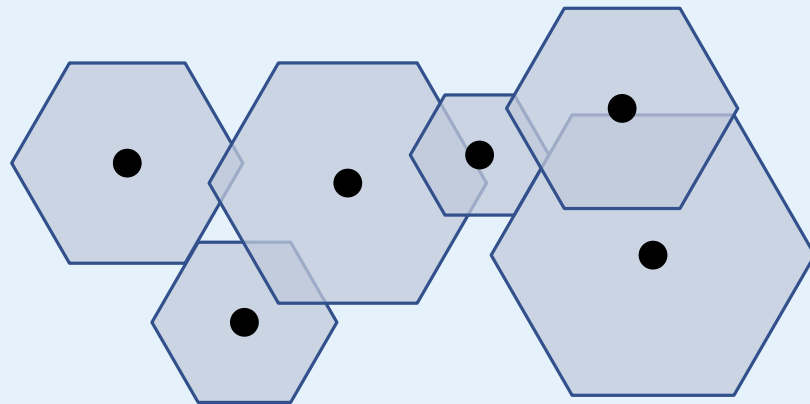


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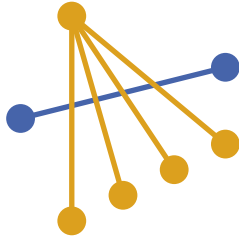
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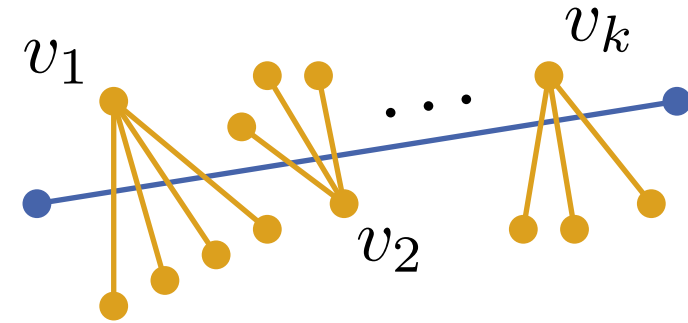


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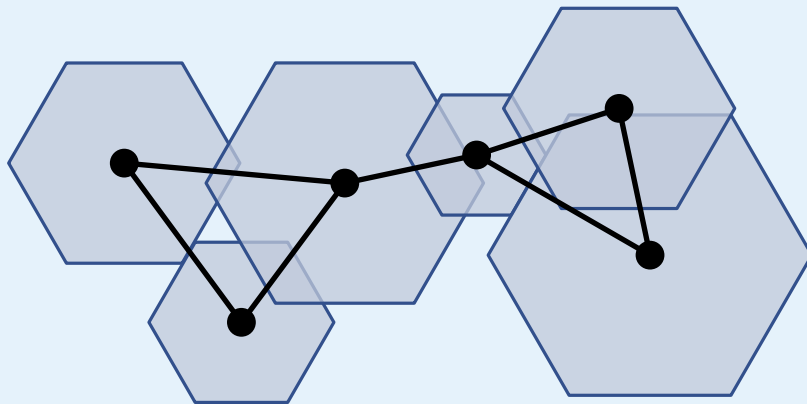


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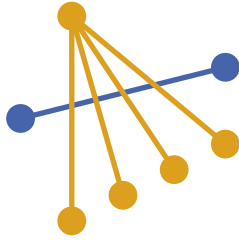
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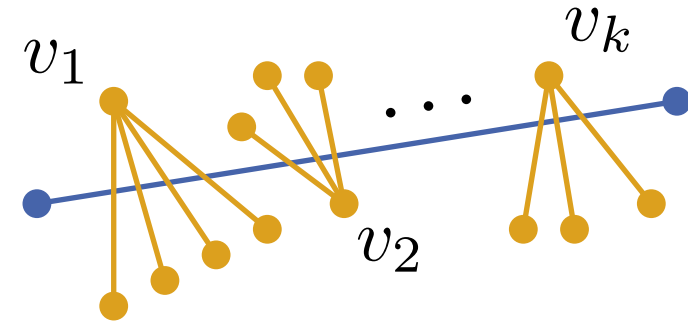


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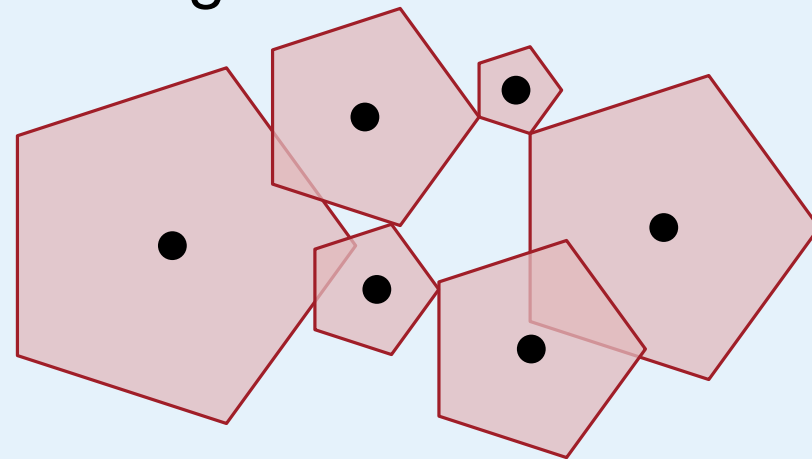
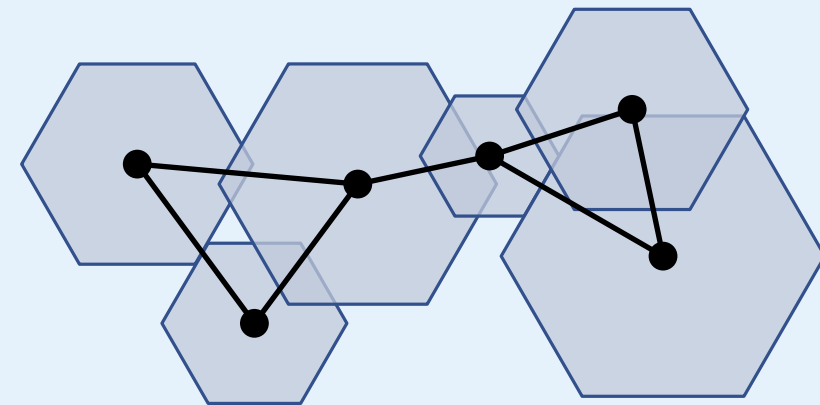


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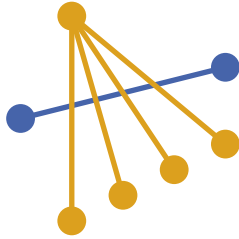
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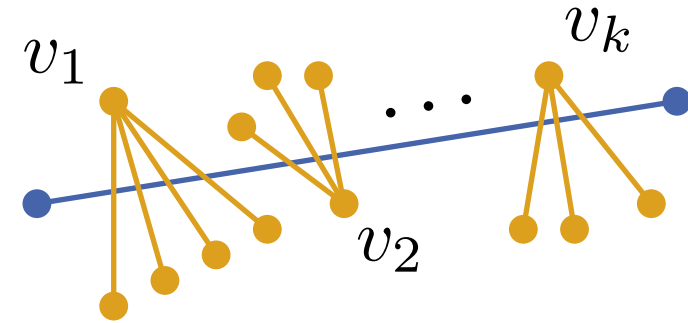


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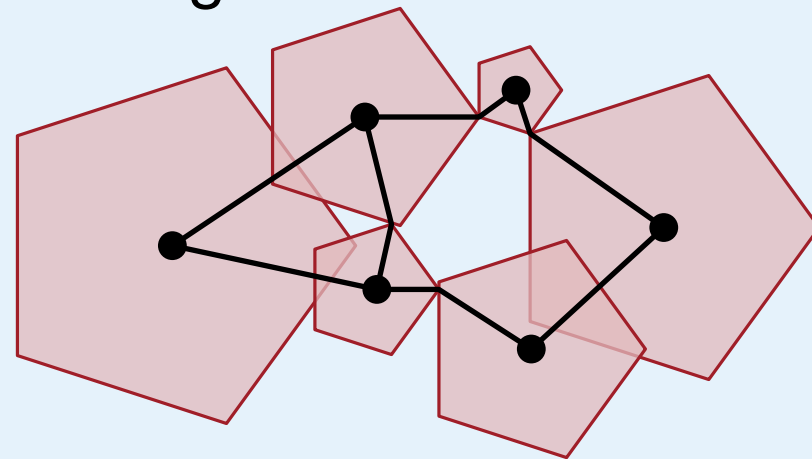
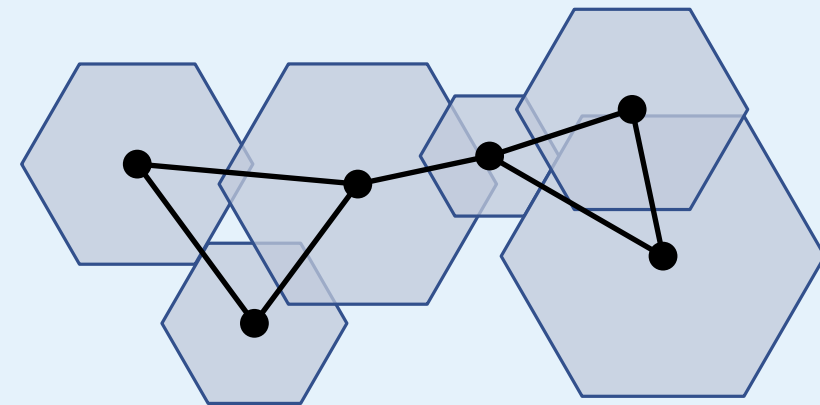


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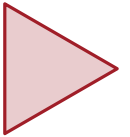


k -independent crossing

canonical drawings



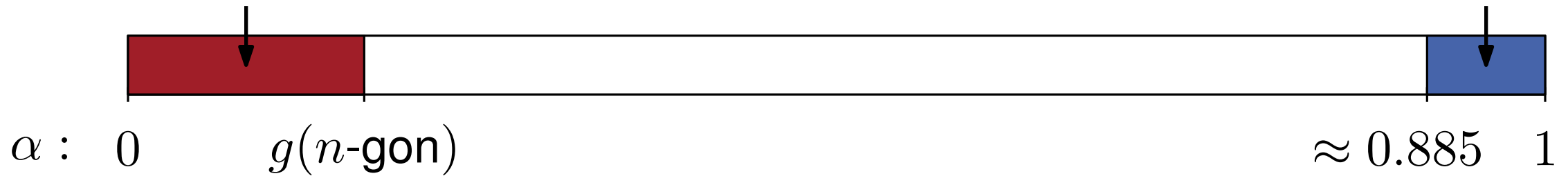
Conclusion

■ For  and  : **no** product structure for $\alpha < 1$.

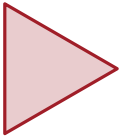
■ For even $n \geq 6$:

no product structure

product structure



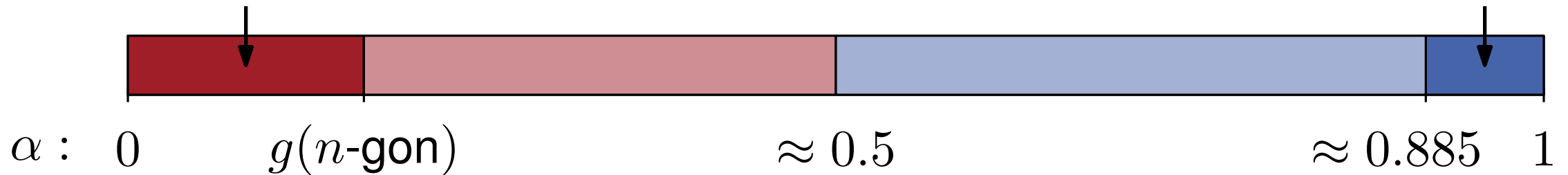
Conclusion

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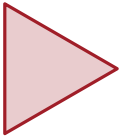
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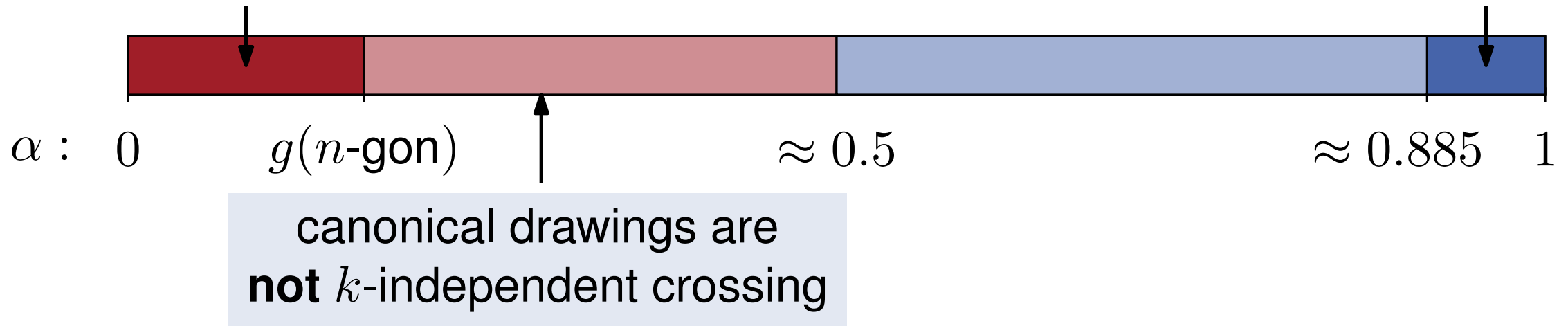
Conclusion

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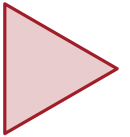
■ For even $n \geq 6$:

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product structure



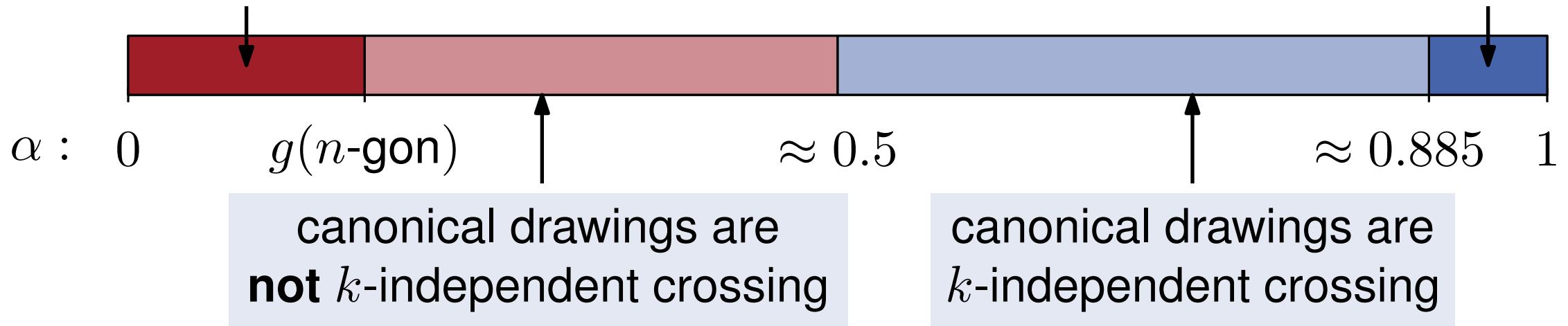
Conclusion

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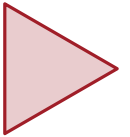
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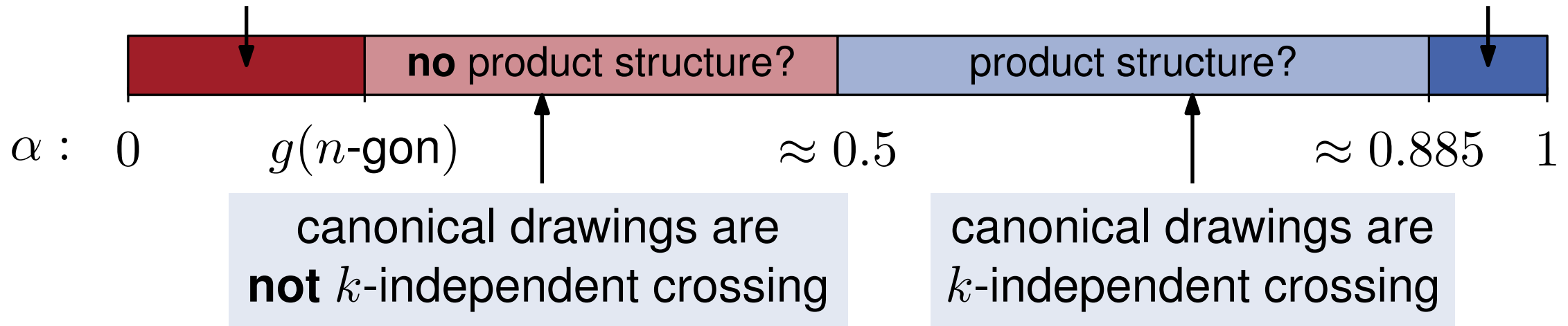
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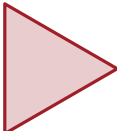
■ For even $n \geq 6$:

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product structure



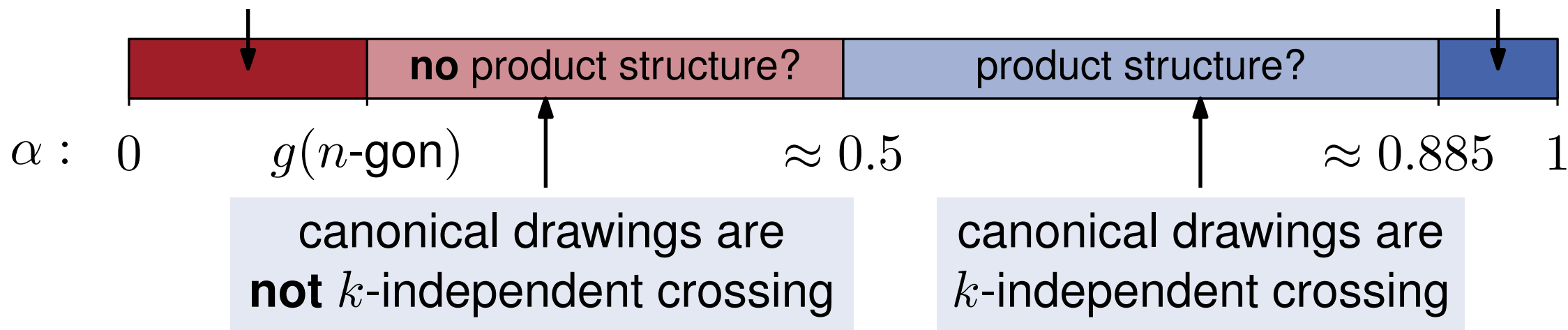
Conclusion

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■ For even $n \geq 6$:

no product structure

product structure



Question: Do k -independent crossing graphs have product structure?